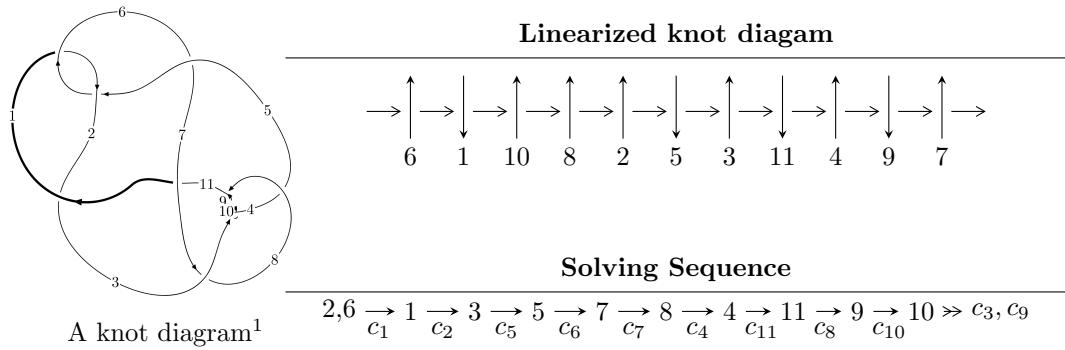


## $11a_{121}$ ( $K11a_{121}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$\begin{aligned} I_1^u &= \langle u^{11} + 2u^9 + 4u^7 + 4u^5 - u^4 + 3u^3 - u^2 + 2u - 1 \rangle \\ I_2^u &= \langle u^{48} - u^{47} + \dots + 2u + 1 \rangle \end{aligned}$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 59 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle u^{11} + 2u^9 + 4u^7 + 4u^5 - u^4 + 3u^3 - u^2 + 2u - 1 \rangle$$

(i) Arc colorings

$$\begin{aligned}
a_2 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\
a_6 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\
a_1 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\
a_3 &= \begin{pmatrix} u^2 + 1 \\ u^4 \end{pmatrix} \\
a_5 &= \begin{pmatrix} -u \\ u \end{pmatrix} \\
a_7 &= \begin{pmatrix} -u^3 \\ u^3 + u \end{pmatrix} \\
a_8 &= \begin{pmatrix} u^9 + 2u^7 + 3u^5 + 2u^3 + u \\ -u^9 - 2u^7 - 3u^5 + u^4 - 2u^3 + u^2 - u + 1 \end{pmatrix} \\
a_4 &= \begin{pmatrix} u^8 - u^7 + u^6 - 2u^5 + 2u^4 - 2u^3 + u^2 - 2u \\ -u^9 - u^8 - u^7 - u^6 - u^5 - 2u^4 - u^2 + u \end{pmatrix} \\
a_{11} &= \begin{pmatrix} -u^8 - u^6 - u^4 + 1 \\ u^8 + 2u^6 + 2u^4 + 2u^2 \end{pmatrix} \\
a_9 &= \begin{pmatrix} u^{10} + u^9 + u^8 + 2u^7 + u^6 + 3u^5 + 2u^3 - u^2 + u \\ -u^{10} - u^9 - 2u^8 - 2u^7 - 2u^6 - 3u^5 - u^4 - 2u^3 + u^2 - u + 1 \end{pmatrix} \\
a_{10} &= \begin{pmatrix} u^{10} + 2u^8 + u^7 + 3u^6 + u^5 + 2u^4 + u^3 + u^2 + u \\ -u^8 - u^7 - u^6 - u^5 - u^4 - u^3 - u + 1 \end{pmatrix} \\
a_{10} &= \begin{pmatrix} u^{10} + 2u^8 + u^7 + 3u^6 + u^5 + 2u^4 + u^3 + u^2 + u \\ -u^8 - u^7 - u^6 - u^5 - u^4 - u^3 - u + 1 \end{pmatrix}
\end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $4u^{10} + 4u^9 + 4u^8 + 8u^7 + 12u^6 + 16u^5 + 8u^4 + 8u^3 + 4u^2 + 8u + 6$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_5$ $c_9$	$u^{11} + 2u^9 + 4u^7 + 4u^5 - u^4 + 3u^3 - u^2 + 2u - 1$
$c_2, c_6, c_8$ $c_{10}$	$u^{11} + 4u^{10} + \dots + 2u - 1$
$c_4, c_{11}$	$u^{11} + 2u^9 - 2u^8 + 10u^7 + 12u^5 - 3u^4 + 5u^3 - u^2 - 1$
$c_7$	$u^{11} - 7u^{10} + \dots + 28u - 8$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_5$ $c_9$	$y^{11} + 4y^{10} + \cdots + 2y - 1$
$c_2, c_6, c_8$ $c_{10}$	$y^{11} + 8y^{10} + \cdots + 22y - 1$
$c_4, c_{11}$	$y^{11} + 4y^{10} + \cdots - 2y - 1$
$c_7$	$y^{11} - 3y^{10} + \cdots + 48y - 64$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.111009 + 1.030810I$	$-5.93919 - 3.55367I$	$-6.35449 + 4.86751I$
$u = -0.111009 - 1.030810I$	$-5.93919 + 3.55367I$	$-6.35449 - 4.86751I$
$u = 0.594105 + 0.723647I$	$1.48764 + 1.96750I$	$4.49213 - 3.23948I$
$u = 0.594105 - 0.723647I$	$1.48764 - 1.96750I$	$4.49213 + 3.23948I$
$u = -0.817015 + 0.707633I$	$6.68078 + 3.13136I$	$8.76083 - 0.56604I$
$u = -0.817015 - 0.707633I$	$6.68078 - 3.13136I$	$8.76083 + 0.56604I$
$u = -0.617277 + 0.966546I$	$-0.07920 - 7.68222I$	$0.97285 + 8.49443I$
$u = -0.617277 - 0.966546I$	$-0.07920 + 7.68222I$	$0.97285 - 8.49443I$
$u = 0.729012 + 1.011350I$	$4.8176 + 14.7555I$	$5.24582 - 10.31160I$
$u = 0.729012 - 1.011350I$	$4.8176 - 14.7555I$	$5.24582 + 10.31160I$
$u = 0.444369$	0.869046	11.7660

$$\text{II. } I_2^u = \langle u^{48} - u^{47} + \cdots + 2u + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_2 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_1 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_3 &= \begin{pmatrix} u^2 + 1 \\ u^4 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -u \\ u \end{pmatrix} \\ a_7 &= \begin{pmatrix} -u^3 \\ u^3 + u \end{pmatrix} \\ a_8 &= \begin{pmatrix} u^9 + 2u^7 + 3u^5 + 2u^3 + u \\ u^{11} + u^9 + 2u^7 + u^5 + u^3 + u \end{pmatrix} \\ a_4 &= \begin{pmatrix} -u^{21} - 4u^{19} + \cdots - 2u^3 - u \\ -u^{23} - 3u^{21} + \cdots - 2u^3 + u \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -u^8 - u^6 - u^4 + 1 \\ u^8 + 2u^6 + 2u^4 + 2u^2 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -u^{27} - 4u^{25} + \cdots + 10u^5 + 3u^3 \\ u^{27} + 5u^{25} + \cdots - u^3 + u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -u^{46} - 7u^{44} + \cdots - 4u^4 + 1 \\ u^{46} + 8u^{44} + \cdots + 4u^4 + u^2 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -u^{46} - 7u^{44} + \cdots - 4u^4 + 1 \\ u^{46} + 8u^{44} + \cdots + 4u^4 + u^2 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

$$\begin{aligned} \text{(iii) Cusp Shapes} &= 4u^{45} + 28u^{43} + 132u^{41} + 448u^{39} + 1224u^{37} + 2772u^{35} + 5348u^{33} + \\ &8916u^{31} + 12948u^{29} - 4u^{28} + 16456u^{27} - 20u^{26} + 18292u^{25} - 68u^{24} + 17704u^{23} - 164u^{22} + \\ &14776u^{21} - 308u^{20} + 10428u^{19} - 468u^{18} + 6020u^{17} - 576u^{16} + 2644u^{15} - 580u^{14} + \\ &720u^{13} - 468u^{12} - 288u^{10} - 88u^9 - 124u^8 - 4u^7 - 24u^6 + 36u^5 + 8u^4 + 24u^3 + 4u^2 + 4u + 2 \end{aligned}$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_5$ $c_9$	$u^{48} - u^{47} + \cdots + 2u + 1$
$c_2, c_6, c_8$ $c_{10}$	$u^{48} + 15u^{47} + \cdots + 8u^3 + 1$
$c_4, c_{11}$	$u^{48} + 5u^{47} + \cdots + 12u + 1$
$c_7$	$(u^{24} + 3u^{23} + \cdots + 18u + 7)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_5$ $c_9$	$y^{48} + 15y^{47} + \cdots + 8y^3 + 1$
$c_2, c_6, c_8$ $c_{10}$	$y^{48} + 35y^{47} + \cdots + 88y^2 + 1$
$c_4, c_{11}$	$y^{48} - 5y^{47} + \cdots - 24y + 1$
$c_7$	$(y^{24} - 9y^{23} + \cdots - 212y + 49)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.447030 + 0.894068I$	$0.85406 + 3.28062I$	$1.88284 - 1.76353I$
$u = -0.447030 - 0.894068I$	$0.85406 - 3.28062I$	$1.88284 + 1.76353I$
$u = -0.037970 + 1.018320I$	$-3.47428 + 2.08425I$	$-3.81787 - 2.59078I$
$u = -0.037970 - 1.018320I$	$-3.47428 - 2.08425I$	$-3.81787 + 2.59078I$
$u = 0.103335 + 0.964930I$	$-2.07060 + 1.71275I$	$0.95839 - 4.38827I$
$u = 0.103335 - 0.964930I$	$-2.07060 - 1.71275I$	$0.95839 + 4.38827I$
$u = 0.709249 + 0.753994I$	$1.54659 + 2.07802I$	$3.74247 - 4.14356I$
$u = 0.709249 - 0.753994I$	$1.54659 - 2.07802I$	$3.74247 + 4.14356I$
$u = 0.161802 + 1.028080I$	$0.15229 + 3.45771I$	$1.61918 - 3.33537I$
$u = 0.161802 - 1.028080I$	$0.15229 - 3.45771I$	$1.61918 + 3.33537I$
$u = 0.786969 + 0.691947I$	$0.15229 - 3.45771I$	$1.61918 + 3.33537I$
$u = 0.786969 - 0.691947I$	$0.15229 + 3.45771I$	$1.61918 - 3.33537I$
$u = -0.156596 + 1.043700I$	$-0.78809 - 9.12338I$	$-0.18249 + 8.13527I$
$u = -0.156596 - 1.043700I$	$-0.78809 + 9.12338I$	$-0.18249 - 8.13527I$
$u = -0.779513 + 0.728650I$	$3.78730 + 1.05884I$	$9.33375 - 1.03697I$
$u = -0.779513 - 0.728650I$	$3.78730 - 1.05884I$	$9.33375 + 1.03697I$
$u = 0.820160 + 0.698926I$	$5.77023 - 8.94227I$	$7.03302 + 5.48937I$
$u = 0.820160 - 0.698926I$	$5.77023 + 8.94227I$	$7.03302 - 5.48937I$
$u = -0.559504 + 0.928720I$	$-3.47428 - 2.08425I$	$-3.81787 + 2.59078I$
$u = -0.559504 - 0.928720I$	$-3.47428 + 2.08425I$	$-3.81787 - 2.59078I$
$u = 0.357761 + 0.828361I$	$1.54659 + 2.07802I$	$3.74247 - 4.14356I$
$u = 0.357761 - 0.828361I$	$1.54659 - 2.07802I$	$3.74247 + 4.14356I$
$u = -0.798379 + 0.782289I$	$7.98533$	$10.04300 + 0.I$
$u = -0.798379 - 0.782289I$	$7.98533$	$10.04300 + 0.I$
$u = 0.795531 + 0.794799I$	$7.45278 + 5.81585I$	$8.97012 - 5.48927I$
$u = 0.795531 - 0.794799I$	$7.45278 - 5.81585I$	$8.97012 + 5.48927I$
$u = 0.644764 + 0.924836I$	$0.94545 + 3.01303I$	$3.90717 - 2.47987I$
$u = 0.644764 - 0.924836I$	$0.94545 - 3.01303I$	$3.90717 + 2.47987I$
$u = 0.684868 + 0.970999I$	$0.85406 + 3.28062I$	$1.88284 - 1.76353I$
$u = 0.684868 - 0.970999I$	$0.85406 - 3.28062I$	$1.88284 + 1.76353I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.750786 + 0.945298I$	6.98909	$8.15485 + 0.I$
$u = 0.750786 - 0.945298I$	6.98909	$8.15485 + 0.I$
$u = -0.748039 + 0.955471I$	$7.45278 - 5.81585I$	$8.97012 + 5.48927I$
$u = -0.748039 - 0.955471I$	$7.45278 + 5.81585I$	$8.97012 - 5.48927I$
$u = -0.718495 + 0.983429I$	$3.01107 - 6.72706I$	$7.45449 + 6.34172I$
$u = -0.718495 - 0.983429I$	$3.01107 + 6.72706I$	$7.45449 - 6.34172I$
$u = 0.712082 + 1.003140I$	$-0.78809 + 9.12338I$	$0. - 8.13527I$
$u = 0.712082 - 1.003140I$	$-0.78809 - 9.12338I$	$0. + 8.13527I$
$u = -0.730704 + 1.006040I$	$5.77023 - 8.94227I$	$7.03302 + 5.48937I$
$u = -0.730704 - 1.006040I$	$5.77023 + 8.94227I$	$7.03302 - 5.48937I$
$u = -0.520871 + 0.529700I$	$0.94545 + 3.01303I$	$3.90717 - 2.47987I$
$u = -0.520871 - 0.529700I$	$0.94545 - 3.01303I$	$3.90717 + 2.47987I$
$u = -0.619099 + 0.144052I$	$3.01107 - 6.72706I$	$7.45449 + 6.34172I$
$u = -0.619099 - 0.144052I$	$3.01107 + 6.72706I$	$7.45449 - 6.34172I$
$u = 0.605322 + 0.114770I$	$3.78730 + 1.05884I$	$9.33375 - 1.03697I$
$u = 0.605322 - 0.114770I$	$3.78730 - 1.05884I$	$9.33375 + 1.03697I$
$u = -0.516429 + 0.228211I$	$-2.07060 - 1.71275I$	$0.95839 + 4.38827I$
$u = -0.516429 - 0.228211I$	$-2.07060 + 1.71275I$	$0.95839 - 4.38827I$

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_5$ $c_9$	$(u^{11} + 2u^9 + \dots + 2u - 1)(u^{48} - u^{47} + \dots + 2u + 1)$
$c_2, c_6, c_8$ $c_{10}$	$(u^{11} + 4u^{10} + \dots + 2u - 1)(u^{48} + 15u^{47} + \dots + 8u^3 + 1)$
$c_4, c_{11}$	$(u^{11} + 2u^9 - 2u^8 + 10u^7 + 12u^5 - 3u^4 + 5u^3 - u^2 - 1)$ $\cdot (u^{48} + 5u^{47} + \dots + 12u + 1)$
$c_7$	$(u^{11} - 7u^{10} + \dots + 28u - 8)(u^{24} + 3u^{23} + \dots + 18u + 7)^2$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_5$ $c_9$	$(y^{11} + 4y^{10} + \dots + 2y - 1)(y^{48} + 15y^{47} + \dots + 8y^3 + 1)$
$c_2, c_6, c_8$ $c_{10}$	$(y^{11} + 8y^{10} + \dots + 22y - 1)(y^{48} + 35y^{47} + \dots + 88y^2 + 1)$
$c_4, c_{11}$	$(y^{11} + 4y^{10} + \dots - 2y - 1)(y^{48} - 5y^{47} + \dots - 24y + 1)$
$c_7$	$(y^{11} - 3y^{10} + \dots + 48y - 64)(y^{24} - 9y^{23} + \dots - 212y + 49)^2$