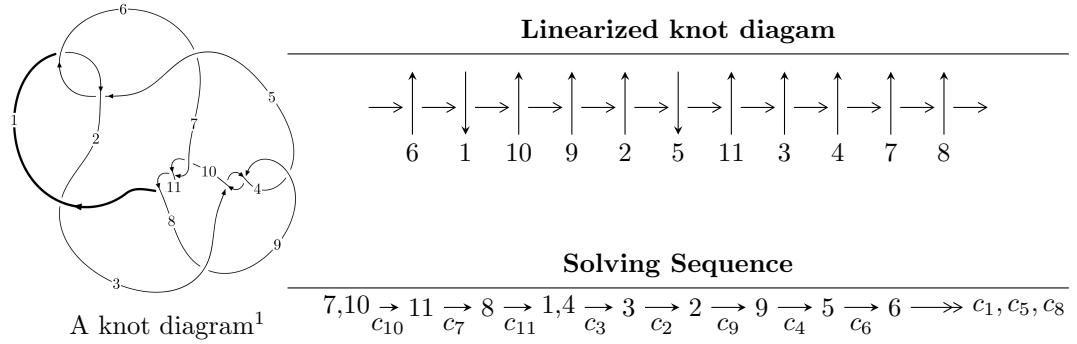


## $11a_{143}$ ( $K11a_{143}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$\begin{aligned}
 I_1^u &= \langle 3.31268 \times 10^{32} u^{49} - 5.56961 \times 10^{32} u^{48} + \dots + 3.84136 \times 10^{32} b + 1.21137 \times 10^{33}, \\
 &\quad - 1.01160 \times 10^{33} u^{49} - 2.15416 \times 10^{33} u^{48} + \dots + 4.60963 \times 10^{33} a + 6.11980 \times 10^{33}, \\
 &\quad u^{50} - 3u^{49} + \dots - 14u - 3 \rangle \\
 I_2^u &= \langle -2a^3 + 3a^2 + 5b - 15a + 7, a^4 - 2a^3 + 7a^2 - 6a + 3, u + 1 \rangle \\
 I_3^u &= \langle b, a^2 - a + 1, u - 1 \rangle
 \end{aligned}$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 56 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle 3.31 \times 10^{32}u^{49} - 5.57 \times 10^{32}u^{48} + \dots + 3.84 \times 10^{32}b + 1.21 \times 10^{33}, -1.01 \times 10^{33}u^{49} - 2.15 \times 10^{33}u^{48} + \dots + 4.61 \times 10^{33}a + 6.12 \times 10^{33}, u^{50} - 3u^{49} + \dots - 14u - 3 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_7 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_8 &= \begin{pmatrix} u \\ -u^3 + u \end{pmatrix} \\ a_1 &= \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 0.219454u^{49} + 0.467318u^{48} + \dots + 9.86130u - 1.32761 \\ -0.862372u^{49} + 1.44991u^{48} + \dots - 16.7135u - 3.15351 \end{pmatrix} \\ a_3 &= \begin{pmatrix} 1.08183u^{49} - 0.982587u^{48} + \dots + 26.5748u + 1.82589 \\ -0.862372u^{49} + 1.44991u^{48} + \dots - 16.7135u - 3.15351 \end{pmatrix} \\ a_2 &= \begin{pmatrix} 0.247278u^{49} + 0.359922u^{48} + \dots + 11.7803u - 0.445043 \\ -0.895841u^{49} + 1.30207u^{48} + \dots - 19.0363u - 3.62861 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -0.694954u^{49} + 1.84791u^{48} + \dots + 28.4151u + 4.77905 \\ 0.141172u^{49} - 0.0191976u^{48} + \dots + 5.14402u - 0.584566 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -0.562523u^{49} + 0.817800u^{48} + \dots - 8.66416u + 1.58746 \\ 0.649198u^{49} - 0.790264u^{48} + \dots + 15.0431u + 2.83582 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -0.152066u^{49} + 0.970436u^{48} + \dots + 28.0155u + 3.66927 \\ -0.384959u^{49} + 0.691554u^{48} + \dots - 5.39208u - 2.02124 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -0.152066u^{49} + 0.970436u^{48} + \dots + 28.0155u + 3.66927 \\ -0.384959u^{49} + 0.691554u^{48} + \dots - 5.39208u - 2.02124 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $-0.874649u^{49} + 2.02419u^{48} + \dots + 4.43493u + 1.54316$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_5$	$u^{50} - 2u^{49} + \cdots - 3u + 3$
$c_2, c_6$	$u^{50} + 16u^{49} + \cdots - 39u + 9$
$c_3, c_4, c_9$	$u^{50} - u^{49} + \cdots + 16u - 4$
$c_7, c_{10}, c_{11}$	$u^{50} - 3u^{49} + \cdots - 14u - 3$
$c_8$	$u^{50} + u^{49} + \cdots + 928u - 404$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_5$	$y^{50} + 16y^{49} + \cdots - 39y + 9$
$c_2, c_6$	$y^{50} + 40y^{49} + \cdots - 11439y + 81$
$c_3, c_4, c_9$	$y^{50} + 45y^{49} + \cdots - 480y^2 + 16$
$c_7, c_{10}, c_{11}$	$y^{50} - 49y^{49} + \cdots + 68y + 9$
$c_8$	$y^{50} - 15y^{49} + \cdots + 470400y + 163216$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.768044 + 0.620254I$		
$a = 0.51382 + 1.55754I$	$0.52020 - 1.74042I$	$8.32117 + 2.63326I$
$b = 0.223518 + 1.133800I$		
$u = -0.768044 - 0.620254I$		
$a = 0.51382 - 1.55754I$	$0.52020 + 1.74042I$	$8.32117 - 2.63326I$
$b = 0.223518 - 1.133800I$		
$u = -0.357982 + 0.888739I$		
$a = -0.66589 - 2.42275I$	$-1.38805 - 9.13876I$	$5.39526 + 7.47528I$
$b = 0.310740 - 1.355660I$		
$u = -0.357982 - 0.888739I$		
$a = -0.66589 + 2.42275I$	$-1.38805 + 9.13876I$	$5.39526 - 7.47528I$
$b = 0.310740 + 1.355660I$		
$u = -0.419643 + 0.836664I$		
$a = 0.70010 + 2.28634I$	$-0.58057 - 3.35428I$	$6.95050 + 2.72855I$
$b = -0.299889 + 1.309250I$		
$u = -0.419643 - 0.836664I$		
$a = 0.70010 - 2.28634I$	$-0.58057 + 3.35428I$	$6.95050 - 2.72855I$
$b = -0.299889 - 1.309250I$		
$u = -0.875258 + 0.621898I$		
$a = -0.48983 - 1.56500I$	$0.20741 + 3.87448I$	$7.86992 - 3.23394I$
$b = -0.261961 - 1.228410I$		
$u = -0.875258 - 0.621898I$		
$a = -0.48983 + 1.56500I$	$0.20741 - 3.87448I$	$7.86992 + 3.23394I$
$b = -0.261961 + 1.228410I$		
$u = 0.600873 + 0.702881I$		
$a = -0.263588 - 0.464164I$	$3.72925 - 0.33634I$	$12.06779 - 0.57902I$
$b = -0.718050 - 0.066541I$		
$u = 0.600873 - 0.702881I$		
$a = -0.263588 + 0.464164I$	$3.72925 + 0.33634I$	$12.06779 + 0.57902I$
$b = -0.718050 + 0.066541I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.494891 + 0.774626I$		
$a = 0.302543 + 0.581565I$	$3.36565 + 5.33408I$	$10.62323 - 6.45202I$
$b = 0.737047 + 0.149487I$		
$u = 0.494891 - 0.774626I$		
$a = 0.302543 - 0.581565I$	$3.36565 - 5.33408I$	$10.62323 + 6.45202I$
$b = 0.737047 - 0.149487I$		
$u = -1.065360 + 0.257655I$		
$a = -0.23062 - 1.52209I$	$-4.48476 + 0.36744I$	$2.34065 + 0.74088I$
$b = -0.10488 - 1.42170I$		
$u = -1.065360 - 0.257655I$		
$a = -0.23062 + 1.52209I$	$-4.48476 - 0.36744I$	$2.34065 - 0.74088I$
$b = -0.10488 + 1.42170I$		
$u = 1.100360 + 0.172393I$		
$a = -0.0409123 + 0.0182444I$	$1.27025 + 1.19184I$	$7.00000 + 2.50368I$
$b = -0.313724 + 0.372597I$		
$u = 1.100360 - 0.172393I$		
$a = -0.0409123 - 0.0182444I$	$1.27025 - 1.19184I$	$7.00000 - 2.50368I$
$b = -0.313724 - 0.372597I$		
$u = -0.207647 + 0.672129I$		
$a = -1.26448 - 2.57161I$	$-6.96148 - 3.84491I$	$-1.20333 + 4.74598I$
$b = 0.182493 - 1.383300I$		
$u = -0.207647 - 0.672129I$		
$a = -1.26448 + 2.57161I$	$-6.96148 + 3.84491I$	$-1.20333 - 4.74598I$
$b = 0.182493 + 1.383300I$		
$u = -1.349830 + 0.119644I$		
$a = 0.951187 + 0.404966I$	$2.86347 - 3.60406I$	0
$b = -0.680112 + 0.135570I$		
$u = -1.349830 - 0.119644I$		
$a = 0.951187 - 0.404966I$	$2.86347 + 3.60406I$	0
$b = -0.680112 - 0.135570I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.419371 + 0.489432I$		
$a = 1.23676 + 1.66984I$	$-3.33666 - 1.69681I$	$6.02735 + 3.86873I$
$b = -0.103698 + 1.289300I$		
$u = -0.419371 - 0.489432I$		
$a = 1.23676 - 1.66984I$	$-3.33666 + 1.69681I$	$6.02735 - 3.86873I$
$b = -0.103698 - 1.289300I$		
$u = 1.352170 + 0.098819I$		
$a = 1.161170 + 0.144436I$	$-0.313966 - 0.436878I$	0
$b = -0.211969 - 1.214280I$		
$u = 1.352170 - 0.098819I$		
$a = 1.161170 - 0.144436I$	$-0.313966 + 0.436878I$	0
$b = -0.211969 + 1.214280I$		
$u = -1.356110 + 0.045936I$		
$a = -0.03253 - 1.71582I$	$-0.83159 - 2.75739I$	0
$b = -0.02262 - 1.56889I$		
$u = -1.356110 - 0.045936I$		
$a = -0.03253 + 1.71582I$	$-0.83159 + 2.75739I$	0
$b = -0.02262 + 1.56889I$		
$u = 1.391060 + 0.243928I$		
$a = 1.57875 - 0.80925I$	$-1.84682 + 7.14521I$	0
$b = -0.287890 - 1.351540I$		
$u = 1.391060 - 0.243928I$		
$a = 1.57875 + 0.80925I$	$-1.84682 - 7.14521I$	0
$b = -0.287890 + 1.351540I$		
$u = -1.43839$		
$a = -0.748101$	6.46721	0
$b = 0.770058$		
$u = 1.43734 + 0.14823I$		
$a = -1.093440 + 0.493494I$	$2.58460 + 3.94905I$	0
$b = 0.323552 + 1.255700I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.43734 - 0.14823I$		
$a = -1.093440 - 0.493494I$	$2.58460 - 3.94905I$	0
$b = 0.323552 - 1.255700I$		
$u = -0.513376 + 0.156185I$		
$a = 0.12350 + 1.97974I$	$0.74464 - 2.36364I$	$3.62478 + 4.11961I$
$b = 0.024574 + 0.485591I$		
$u = -0.513376 - 0.156185I$		
$a = 0.12350 - 1.97974I$	$0.74464 + 2.36364I$	$3.62478 - 4.11961I$
$b = 0.024574 - 0.485591I$		
$u = 0.099189 + 0.524649I$		
$a = -0.042705 + 1.015670I$	$-1.63114 + 1.42356I$	$2.31879 - 5.63109I$
$b = 0.469409 + 0.309538I$		
$u = 0.099189 - 0.524649I$		
$a = -0.042705 - 1.015670I$	$-1.63114 - 1.42356I$	$2.31879 + 5.63109I$
$b = 0.469409 - 0.309538I$		
$u = 1.48543 + 0.34428I$		
$a = 1.24716 - 1.34114I$	$4.5437 + 13.6084I$	0
$b = -0.36507 - 1.42866I$		
$u = 1.48543 - 0.34428I$		
$a = 1.24716 + 1.34114I$	$4.5437 - 13.6084I$	0
$b = -0.36507 + 1.42866I$		
$u = 1.51636 + 0.16091I$		
$a = 0.098166 + 0.420372I$	$7.88001 + 4.14120I$	0
$b = -0.558023 + 0.923611I$		
$u = 1.51636 - 0.16091I$		
$a = 0.098166 - 0.420372I$	$7.88001 - 4.14120I$	0
$b = -0.558023 - 0.923611I$		
$u = 1.50169 + 0.30522I$		
$a = -1.16719 + 1.21068I$	$5.64838 + 7.50037I$	0
$b = 0.37957 + 1.39957I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.50169 - 0.30522I$		
$a = -1.16719 - 1.21068I$	$5.64838 - 7.50037I$	0
$b = 0.37957 - 1.39957I$		
$u = 1.53335 + 0.09779I$		
$a = -0.209409 - 0.465882I$	$8.31731 - 1.99153I$	0
$b = 0.526883 - 0.998341I$		
$u = 1.53335 - 0.09779I$		
$a = -0.209409 + 0.465882I$	$8.31731 + 1.99153I$	0
$b = 0.526883 + 0.998341I$		
$u = -1.51832 + 0.26912I$		
$a = 0.407229 + 0.580854I$	$9.92580 - 9.13602I$	0
$b = -0.874042 + 0.265626I$		
$u = -1.51832 - 0.26912I$		
$a = 0.407229 - 0.580854I$	$9.92580 + 9.13602I$	0
$b = -0.874042 - 0.265626I$		
$u = -1.53487 + 0.21619I$		
$a = -0.418285 - 0.467881I$	$10.74210 - 2.95976I$	0
$b = 0.882710 - 0.212600I$		
$u = -1.53487 - 0.21619I$		
$a = -0.418285 + 0.467881I$	$10.74210 + 2.95976I$	0
$b = 0.882710 + 0.212600I$		
$u = 0.377548$		
$a = 0.538429$	0.630546	15.8700
$b = -0.387989$		
$u = -0.096486 + 0.258092I$		
$a = -4.46333 - 1.70481I$	$-5.03824 + 1.88230I$	$-0.03756 - 2.83434I$
$b = 0.050400 - 1.397800I$		
$u = -0.096486 - 0.258092I$		
$a = -4.46333 + 1.70481I$	$-5.03824 - 1.88230I$	$-0.03756 + 2.83434I$
$b = 0.050400 + 1.397800I$		

$$\text{II. } I_2^u = \langle -2a^3 + 3a^2 + 5b - 15a + 7, a^4 - 2a^3 + 7a^2 - 6a + 3, u + 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} a \\ \frac{2}{5}a^3 - \frac{3}{5}a^2 + 3a - \frac{7}{5} \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -\frac{2}{5}a^3 + \frac{3}{5}a^2 - 2a + \frac{7}{5} \\ \frac{2}{5}a^3 - \frac{3}{5}a^2 + 3a - \frac{7}{5} \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -\frac{2}{5}a^3 + \frac{3}{5}a^2 - 2a + \frac{7}{5} \\ \frac{4}{5}a^3 - \frac{6}{5}a^2 + 5a - \frac{14}{5} \end{pmatrix}$$

$$a_9 = \begin{pmatrix} \frac{1}{5}a^3 + \frac{1}{5}a^2 + a - \frac{1}{5} \\ -2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} \frac{2}{5}a^3 - \frac{3}{5}a^2 + 2a - \frac{7}{5} \\ -\frac{2}{5}a^3 + \frac{3}{5}a^2 - 3a + \frac{7}{5} \end{pmatrix}$$

$$a_6 = \begin{pmatrix} \frac{2}{5}a^3 - \frac{3}{5}a^2 + 2a - \frac{2}{5} \\ -\frac{1}{5}a^3 - \frac{1}{5}a^2 - a - \frac{9}{5} \end{pmatrix}$$

$$a_6 = \begin{pmatrix} \frac{2}{5}a^3 - \frac{3}{5}a^2 + 2a - \frac{2}{5} \\ -\frac{1}{5}a^3 - \frac{1}{5}a^2 - a - \frac{9}{5} \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-\frac{8}{5}a^3 + \frac{12}{5}a^2 - 8a + \frac{48}{5}$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$(u^2 - u + 1)^2$
$c_2, c_5, c_6$	$(u^2 + u + 1)^2$
$c_3, c_4, c_8$ $c_9$	$(u^2 + 2)^2$
$c_7$	$(u - 1)^4$
$c_{10}, c_{11}$	$(u + 1)^4$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_5$ $c_6$	$(y^2 + y + 1)^2$
$c_3, c_4, c_8$ $c_9$	$(y + 2)^4$
$c_7, c_{10}, c_{11}$	$(y - 1)^4$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.00000$		
$a = 0.500000 + 0.548188I$	$-3.28987 + 2.02988I$	$6.00000 - 3.46410I$
$b = 1.414210I$		
$u = -1.00000$		
$a = 0.500000 - 0.548188I$	$-3.28987 - 2.02988I$	$6.00000 + 3.46410I$
$b = -1.414210I$		
$u = -1.00000$		
$a = 0.50000 + 2.28024I$	$-3.28987 - 2.02988I$	$6.00000 + 3.46410I$
$b = 1.414210I$		
$u = -1.00000$		
$a = 0.50000 - 2.28024I$	$-3.28987 + 2.02988I$	$6.00000 - 3.46410I$
$b = -1.414210I$		

$$\text{III. } I_3^u = \langle b, a^2 - a + 1, u - 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} a \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} a \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a \\ -a \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} a \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} a-1 \\ 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} a-1 \\ 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $4a + 10$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_6$	$u^2 + u + 1$
$c_3, c_4, c_8$ $c_9$	$u^2$
$c_5$	$u^2 - u + 1$
$c_7$	$(u + 1)^2$
$c_{10}, c_{11}$	$(u - 1)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_5$ $c_6$	$y^2 + y + 1$
$c_3, c_4, c_8$ $c_9$	$y^2$
$c_7, c_{10}, c_{11}$	$(y - 1)^2$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$		
$a = 0.500000 + 0.866025I$	$1.64493 - 2.02988I$	$12.00000 + 3.46410I$
$b = 0$		
$u = 1.00000$		
$a = 0.500000 - 0.866025I$	$1.64493 + 2.02988I$	$12.00000 - 3.46410I$
$b = 0$		

#### IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u^2 - u + 1)^2)(u^2 + u + 1)(u^{50} - 2u^{49} + \cdots - 3u + 3)$
$c_2, c_6$	$((u^2 + u + 1)^3)(u^{50} + 16u^{49} + \cdots - 39u + 9)$
$c_3, c_4, c_9$	$u^2(u^2 + 2)^2(u^{50} - u^{49} + \cdots + 16u - 4)$
$c_5$	$(u^2 - u + 1)(u^2 + u + 1)^2(u^{50} - 2u^{49} + \cdots - 3u + 3)$
$c_7$	$((u - 1)^4)(u + 1)^2(u^{50} - 3u^{49} + \cdots - 14u - 3)$
$c_8$	$u^2(u^2 + 2)^2(u^{50} + u^{49} + \cdots + 928u - 404)$
$c_{10}, c_{11}$	$((u - 1)^2)(u + 1)^4(u^{50} - 3u^{49} + \cdots - 14u - 3)$

## V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_5$	$((y^2 + y + 1)^3)(y^{50} + 16y^{49} + \dots - 39y + 9)$
$c_2, c_6$	$((y^2 + y + 1)^3)(y^{50} + 40y^{49} + \dots - 11439y + 81)$
$c_3, c_4, c_9$	$y^2(y + 2)^4(y^{50} + 45y^{49} + \dots - 480y^2 + 16)$
$c_7, c_{10}, c_{11}$	$((y - 1)^6)(y^{50} - 49y^{49} + \dots + 68y + 9)$
$c_8$	$y^2(y + 2)^4(y^{50} - 15y^{49} + \dots + 470400y + 163216)$