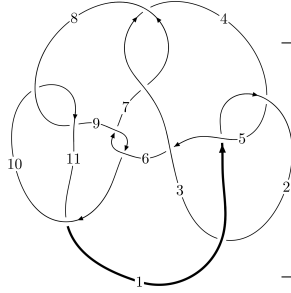
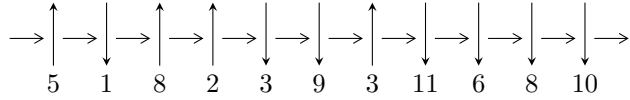


# 11n<sub>7</sub> (K11n<sub>7</sub>)



A knot diagram<sup>1</sup>

## Linearized knot diagram



## Solving Sequence

$$9,11 \xrightarrow{c_8} 3,8 \xrightarrow{c_3} 4 \xrightarrow{c_7} 7 \xrightarrow{c_6} 6 \xrightarrow{c_5} 5 \xrightarrow{c_{10}} 10 \xrightarrow{c_{11}} 1 \xrightarrow{c_2} 2 \longrightarrow c_1, c_4, c_9$$

## Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$I_1^u = \langle 2.20194 \times 10^{21} u^{38} + 4.46582 \times 10^{22} u^{37} + \dots + 2.15629 \times 10^{22} b + 5.77763 \times 10^{22},$$

$$- 5.60651 \times 10^{22} u^{38} - 2.01892 \times 10^{23} u^{37} + \dots + 2.15629 \times 10^{22} a + 8.89136 \times 10^{22}, u^{39} + 3u^{38} + \dots - 5u -$$

$$I_2^u = \langle u^2 a + b, u^2 a + a^2 + 2au + 3u^2 + a + 5u + 4, u^3 + u^2 - 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 45 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle 2.20 \times 10^{21} u^{38} + 4.47 \times 10^{22} u^{37} + \dots + 2.16 \times 10^{22} b + 5.78 \times 10^{22}, -5.61 \times 10^{22} u^{38} - 2.02 \times 10^{23} u^{37} + \dots + 2.16 \times 10^{22} a + 8.89 \times 10^{22}, u^{39} + 3u^{38} + \dots - 5u - 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_9 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_3 &= \begin{pmatrix} 2.60007u^{38} + 9.36292u^{37} + \dots - 11.3955u - 4.12344 \\ -0.102117u^{38} - 2.07106u^{37} + \dots - 13.0171u - 2.67943 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 2.79441u^{38} + 10.0298u^{37} + \dots - 13.9989u - 5.24015 \\ -0.0584579u^{38} - 2.06978u^{37} + \dots - 13.6305u - 2.76324 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -0.700760u^{38} - 0.594268u^{37} + \dots + 7.97882u - 0.0611499 \\ -1.25362u^{38} - 2.81386u^{37} + \dots + 0.0129788u - 0.500639 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -1.95438u^{38} - 3.40813u^{37} + \dots + 7.99180u - 0.561789 \\ -1.25362u^{38} - 2.81386u^{37} + \dots + 0.0129788u - 0.500639 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 2.47112u^{38} + 9.86388u^{37} + \dots + 8.27156u + 1.66377 \\ -0.721787u^{38} - 4.52792u^{37} + \dots - 15.7237u - 2.45051 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} u \\ -u^3 + u \end{pmatrix} \\ a_1 &= \begin{pmatrix} -u^3 \\ u^5 - u^3 + u \end{pmatrix} \\ a_2 &= \begin{pmatrix} 2.46841u^{38} + 9.39037u^{37} + \dots - 9.44573u - 3.72104 \\ -0.0315650u^{38} - 2.27311u^{37} + \dots - 14.5271u - 2.54332 \end{pmatrix} \\ a_2 &= \begin{pmatrix} 2.46841u^{38} + 9.39037u^{37} + \dots - 9.44573u - 3.72104 \\ -0.0315650u^{38} - 2.27311u^{37} + \dots - 14.5271u - 2.54332 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = \frac{95167190231219974262615}{10781474718762665439818} u^{38} + \frac{642665286688782560331753}{21562949437525330879636} u^{37} + \dots + \frac{910083121628952116105487}{10781474718762665439818} u + \frac{469851565658388329096693}{21562949437525330879636}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_4$	$u^{39} + 4u^{38} + \dots + 10u - 1$
$c_2$	$u^{39} + 22u^{38} + \dots + 170u - 1$
$c_3, c_7$	$u^{39} + 3u^{38} + \dots + 160u + 64$
$c_5$	$u^{39} - 4u^{38} + \dots + 602u - 49$
$c_6, c_9$	$u^{39} - 3u^{38} + \dots - 3u + 1$
$c_8, c_{10}$	$u^{39} - 3u^{38} + \dots - 5u + 1$
$c_{11}$	$u^{39} + 23u^{38} + \dots + u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$y^{39} + 22y^{38} + \dots + 170y - 1$
$c_2$	$y^{39} - 6y^{38} + \dots + 31510y - 1$
$c_3, c_7$	$y^{39} + 35y^{38} + \dots - 23552y - 4096$
$c_5$	$y^{39} - 34y^{38} + \dots + 391706y - 2401$
$c_6, c_9$	$y^{39} + 9y^{38} + \dots + y - 1$
$c_8, c_{10}$	$y^{39} - 23y^{38} + \dots + y - 1$
$c_{11}$	$y^{39} - 11y^{38} + \dots + 117y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.174715 + 0.953666I$ $a = -0.107736 - 0.141147I$ $b = -0.224524 + 1.376020I$	$-5.68977 + 0.80789I$	$-5.63151 - 0.39749I$
$u = 0.174715 - 0.953666I$ $a = -0.107736 + 0.141147I$ $b = -0.224524 - 1.376020I$	$-5.68977 - 0.80789I$	$-5.63151 + 0.39749I$
$u = -0.113785 + 1.039480I$ $a = 0.1112140 + 0.0706545I$ $b = -0.41499 + 1.53589I$	$-4.49350 - 8.17612I$	$-3.77298 + 5.44747I$
$u = -0.113785 - 1.039480I$ $a = 0.1112140 - 0.0706545I$ $b = -0.41499 - 1.53589I$	$-4.49350 + 8.17612I$	$-3.77298 - 5.44747I$
$u = -0.906304 + 0.258793I$ $a = -0.59831 + 2.09555I$ $b = -0.938219 - 0.467153I$	$0.05191 + 4.16636I$	$-0.57665 - 9.00427I$
$u = -0.906304 - 0.258793I$ $a = -0.59831 - 2.09555I$ $b = -0.938219 + 0.467153I$	$0.05191 - 4.16636I$	$-0.57665 + 9.00427I$
$u = 0.913889 + 0.058300I$ $a = 0.77201 + 4.31604I$ $b = -0.20598 - 3.29592I$	$-1.32570 - 2.15384I$	$-38.3073 + 0.3658I$
$u = 0.913889 - 0.058300I$ $a = 0.77201 - 4.31604I$ $b = -0.20598 + 3.29592I$	$-1.32570 + 2.15384I$	$-38.3073 - 0.3658I$
$u = 0.814464 + 0.380892I$ $a = 0.328778 + 0.693706I$ $b = -0.352686 - 1.052600I$	$-1.92828 + 0.12066I$	$-7.15424 - 0.12690I$
$u = 0.814464 - 0.380892I$ $a = 0.328778 - 0.693706I$ $b = -0.352686 + 1.052600I$	$-1.92828 - 0.12066I$	$-7.15424 + 0.12690I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.062003 + 0.891851I$ $a = 0.073492 - 0.130422I$ $b = 0.43523 - 1.38427I$	$-1.45248 - 3.13609I$	$-0.74981 + 2.49452I$
$u = -0.062003 - 0.891851I$ $a = 0.073492 + 0.130422I$ $b = 0.43523 + 1.38427I$	$-1.45248 + 3.13609I$	$-0.74981 - 2.49452I$
$u = -0.791534 + 0.793494I$ $a = -0.286108 + 0.284239I$ $b = 0.033088 + 0.170270I$	$2.88333 + 1.52566I$	$-2.95623 - 6.42875I$
$u = -0.791534 - 0.793494I$ $a = -0.286108 - 0.284239I$ $b = 0.033088 - 0.170270I$	$2.88333 - 1.52566I$	$-2.95623 + 6.42875I$
$u = -1.105650 + 0.283891I$ $a = -0.916031 - 0.529536I$ $b = -0.320477 + 0.011103I$	$-3.35360 + 5.46941I$	$-6.70822 - 8.69559I$
$u = -1.105650 - 0.283891I$ $a = -0.916031 + 0.529536I$ $b = -0.320477 - 0.011103I$	$-3.35360 - 5.46941I$	$-6.70822 + 8.69559I$
$u = 1.155090 + 0.139104I$ $a = -0.289265 - 1.321470I$ $b = 0.71983 + 1.54185I$	$-2.82585 - 1.96097I$	$-4.21009 + 0.40138I$
$u = 1.155090 - 0.139104I$ $a = -0.289265 + 1.321470I$ $b = 0.71983 - 1.54185I$	$-2.82585 + 1.96097I$	$-4.21009 - 0.40138I$
$u = 0.833700$ $a = 0.604067$ $b = -0.694607$	$-1.20362$	$-8.91670$
$u = -0.952533 + 0.800887I$ $a = 0.358525 + 0.042382I$ $b = 0.117335 - 0.110652I$	$2.42328 + 4.44150I$	$-7.41017 - 1.05267I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.952533 - 0.800887I$ $a = 0.358525 - 0.042382I$ $b = 0.117335 + 0.110652I$	$2.42328 - 4.44150I$	$-7.41017 + 1.05267I$
$u = -0.670244 + 0.249117I$ $a = 0.35712 + 1.40517I$ $b = 0.408266 + 0.138519I$	$1.33536 + 1.46808I$	$4.04275 - 4.37387I$
$u = -0.670244 - 0.249117I$ $a = 0.35712 - 1.40517I$ $b = 0.408266 - 0.138519I$	$1.33536 - 1.46808I$	$4.04275 + 4.37387I$
$u = 1.254360 + 0.453217I$ $a = 1.01660 + 1.37116I$ $b = 0.06649 - 1.63950I$	$-5.43179 - 1.52389I$	0
$u = 1.254360 - 0.453217I$ $a = 1.01660 - 1.37116I$ $b = 0.06649 + 1.63950I$	$-5.43179 + 1.52389I$	0
$u = -1.261920 + 0.500458I$ $a = -0.67622 + 1.81078I$ $b = -0.79327 - 1.68180I$	$-5.09332 + 8.17367I$	$0. - 5.17214I$
$u = -1.261920 - 0.500458I$ $a = -0.67622 - 1.81078I$ $b = -0.79327 + 1.68180I$	$-5.09332 - 8.17367I$	$0. + 5.17214I$
$u = -1.317290 + 0.384349I$ $a = 0.50231 - 1.81838I$ $b = 0.58706 + 1.52850I$	$-10.41510 + 3.75787I$	0
$u = -1.317290 - 0.384349I$ $a = 0.50231 + 1.81838I$ $b = 0.58706 - 1.52850I$	$-10.41510 - 3.75787I$	0
$u = 1.261720 + 0.574659I$ $a = -1.09075 - 1.20453I$ $b = -0.04542 + 1.54404I$	$-8.99304 - 6.36082I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.261720 - 0.574659I$ $a = -1.09075 + 1.20453I$ $b = -0.04542 - 1.54404I$	$-8.99304 + 6.36082I$	0
$u = -1.30473 + 0.56143I$ $a = 0.71828 - 1.70677I$ $b = 0.73324 + 1.82635I$	$-8.1954 + 13.8902I$	0
$u = -1.30473 - 0.56143I$ $a = 0.71828 + 1.70677I$ $b = 0.73324 - 1.82635I$	$-8.1954 - 13.8902I$	0
$u = 1.37975 + 0.41298I$ $a = -0.83835 - 1.29118I$ $b = -0.16526 + 1.61657I$	$-9.33600 + 3.03011I$	0
$u = 1.37975 - 0.41298I$ $a = -0.83835 + 1.29118I$ $b = -0.16526 - 1.61657I$	$-9.33600 - 3.03011I$	0
$u = -0.415565 + 0.222377I$ $a = 0.82602 - 1.70438I$ $b = 0.738838 - 0.443010I$	$1.15178 - 1.50599I$	$2.56109 + 2.72315I$
$u = -0.415565 - 0.222377I$ $a = 0.82602 + 1.70438I$ $b = 0.738838 + 0.443010I$	$1.15178 + 1.50599I$	$2.56109 - 2.72315I$
$u = 0.030712 + 0.352609I$ $a = 2.43638 - 1.81010I$ $b = -0.531247 - 0.445633I$	$-0.39510 - 2.82136I$	$0.57403 + 4.29661I$
$u = 0.030712 - 0.352609I$ $a = 2.43638 + 1.81010I$ $b = -0.531247 + 0.445633I$	$-0.39510 + 2.82136I$	$0.57403 - 4.29661I$



$$\text{II. } I_2^u = \langle u^2a + b, u^2a + a^2 + 2au + 3u^2 + a + 5u + 4, u^3 + u^2 - 1 \rangle$$

(i) Arc colorings

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} a \\ -u^2a \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} a \\ -u^2a \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} a + 2u + 2 \\ -u^2a - u^2 - u - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u^2 + u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^2 - 1 \\ u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 2u^2a \\ -au \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 2u^2a \\ -au \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-7u^2a - 3au + 3u^2 + 8a + u - 2$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_5$	$(u^2 + u + 1)^3$
$c_3, c_7$	$u^6$
$c_4$	$(u^2 - u + 1)^3$
$c_6$	$(u^3 - u^2 + 2u - 1)^2$
$c_8$	$(u^3 + u^2 - 1)^2$
$c_9, c_{11}$	$(u^3 + u^2 + 2u + 1)^2$
$c_{10}$	$(u^3 - u^2 + 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$ $c_5$	$(y^2 + y + 1)^3$
$c_3, c_7$	$y^6$
$c_6, c_9, c_{11}$	$(y^3 + 3y^2 + 2y - 1)^2$
$c_8, c_{10}$	$(y^3 - y^2 + 2y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.877439 + 0.744862I$		
$a = 0.111778 - 0.558770I$	$3.02413 + 4.85801I$	$2.65209 - 7.50333I$
$b = 0.706350 + 0.266290I$		
$u = -0.877439 + 0.744862I$		
$a = 0.428020 + 0.376187I$	$3.02413 + 0.79824I$	$-0.92725 + 3.21674I$
$b = -0.583789 + 0.478572I$		
$u = -0.877439 - 0.744862I$		
$a = 0.111778 + 0.558770I$	$3.02413 - 4.85801I$	$2.65209 + 7.50333I$
$b = 0.706350 - 0.266290I$		
$u = -0.877439 - 0.744862I$		
$a = 0.428020 - 0.376187I$	$3.02413 - 0.79824I$	$-0.92725 - 3.21674I$
$b = -0.583789 - 0.478572I$		
$u = 0.754878$		
$a = -1.53980 + 2.66701I$	$-1.11345 + 2.02988I$	$-2.22484 + 4.65789I$
$b = 0.87744 - 1.51977I$		
$u = 0.754878$		
$a = -1.53980 - 2.66701I$	$-1.11345 - 2.02988I$	$-2.22484 - 4.65789I$
$b = 0.87744 + 1.51977I$		

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u^2 + u + 1)^3)(u^{39} + 4u^{38} + \dots + 10u - 1)$
$c_2$	$((u^2 + u + 1)^3)(u^{39} + 22u^{38} + \dots + 170u - 1)$
$c_3, c_7$	$u^6(u^{39} + 3u^{38} + \dots + 160u + 64)$
$c_4$	$((u^2 - u + 1)^3)(u^{39} + 4u^{38} + \dots + 10u - 1)$
$c_5$	$((u^2 + u + 1)^3)(u^{39} - 4u^{38} + \dots + 602u - 49)$
$c_6$	$((u^3 - u^2 + 2u - 1)^2)(u^{39} - 3u^{38} + \dots - 3u + 1)$
$c_8$	$((u^3 + u^2 - 1)^2)(u^{39} - 3u^{38} + \dots - 5u + 1)$
$c_9$	$((u^3 + u^2 + 2u + 1)^2)(u^{39} - 3u^{38} + \dots - 3u + 1)$
$c_{10}$	$((u^3 - u^2 + 1)^2)(u^{39} - 3u^{38} + \dots - 5u + 1)$
$c_{11}$	$((u^3 + u^2 + 2u + 1)^2)(u^{39} + 23u^{38} + \dots + u + 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$((y^2 + y + 1)^3)(y^{39} + 22y^{38} + \dots + 170y - 1)$
$c_2$	$((y^2 + y + 1)^3)(y^{39} - 6y^{38} + \dots + 31510y - 1)$
$c_3, c_7$	$y^6(y^{39} + 35y^{38} + \dots - 23552y - 4096)$
$c_5$	$((y^2 + y + 1)^3)(y^{39} - 34y^{38} + \dots + 391706y - 2401)$
$c_6, c_9$	$((y^3 + 3y^2 + 2y - 1)^2)(y^{39} + 9y^{38} + \dots + y - 1)$
$c_8, c_{10}$	$((y^3 - y^2 + 2y - 1)^2)(y^{39} - 23y^{38} + \dots + y - 1)$
$c_{11}$	$((y^3 + 3y^2 + 2y - 1)^2)(y^{39} - 11y^{38} + \dots + 117y - 1)$