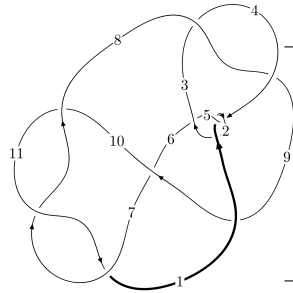
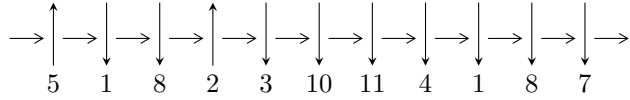


11n<sub>16</sub> (K11n<sub>16</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$7, 11 \xrightarrow{c_7} 3, 8 \xrightarrow{c_3} 4 \xrightarrow{c_{11}} 1 \xrightarrow{c_2} 2 \xrightarrow{c_{10}} 10 \xrightarrow{c_6} 6 \xrightarrow{c_5} 5 \xrightarrow{c_9} 9 \longrightarrow c_1, c_4, c_8$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 2u^{23} + 7u^{22} + \dots + 2b - 5u, -3u^{23} - 11u^{22} + \dots + 2a + 8, u^{24} + 3u^{23} + \dots - 5u - 1 \rangle$$

$$I_2^u = \langle -u^2a + b, u^2a + a^2 + u^2 + a - u + 2, u^3 - u^2 + 2u - 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 30 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\langle 2u^{23} + 7u^{22} + \dots + 2b - 5u, -3u^{23} - 11u^{22} + \dots + 2a + 8, u^{24} + 3u^{23} + \dots - 5u - 1 \rangle$$

I.  $I_1^u =$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} \frac{3}{2}u^{23} + \frac{11}{2}u^{22} + \dots - \frac{33}{2}u - 4 \\ -u^{23} - \frac{7}{2}u^{22} + \dots + \frac{21}{2}u^2 + \frac{5}{2}u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} \frac{3}{2}u^{23} + \frac{9}{2}u^{22} + \dots - \frac{25}{2}u - 3 \\ -\frac{1}{2}u^{22} - u^{21} + \dots - \frac{5}{2}u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 2u^{23} + 6u^{22} + \dots - \frac{27}{2}u - \frac{7}{2} \\ -\frac{3}{2}u^{23} - 4u^{22} + \dots - \frac{1}{2}u - \frac{1}{2} \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^4 - u^2 + 1 \\ -u^6 - 2u^4 - u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} \frac{1}{2}u^{23} + \frac{3}{2}u^{22} + \dots - \frac{15}{2}u + 1 \\ -\frac{1}{2}u^{22} - u^{21} + \dots + \frac{7}{2}u^2 - \frac{1}{2}u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^5 + 2u^3 + u \\ -u^5 - u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^5 + 2u^3 + u \\ -u^5 - u^3 + u \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= -2u^{23} - \frac{9}{2}u^{22} - \frac{45}{2}u^{21} - 40u^{20} - 105u^{19} - \frac{307}{2}u^{18} - \frac{527}{2}u^{17} - 325u^{16} - \frac{757}{2}u^{15} - \frac{803}{2}u^{14} - \frac{589}{2}u^{13} - \frac{531}{2}u^{12} - 90u^{11} - \frac{75}{2}u^{10} + 3u^9 + \frac{129}{2}u^8 - 35u^7 + \frac{15}{2}u^6 - \frac{89}{2}u^5 - 57u^4 - 11u^3 - \frac{67}{2}u^2 - \frac{3}{2}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_4$	$u^{24} + 4u^{23} + \dots + 8u + 1$
$c_2$	$u^{24} + 16u^{23} + \dots - 16u + 1$
$c_3, c_8$	$u^{24} - u^{23} + \dots - 96u - 64$
$c_5$	$u^{24} - 4u^{23} + \dots + 2u + 1$
$c_6$	$u^{24} + 3u^{23} + \dots + u - 1$
$c_7, c_{10}, c_{11}$	$u^{24} - 3u^{23} + \dots + 5u - 1$
$c_9$	$u^{24} - 13u^{23} + \dots - 995u + 563$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$y^{24} + 16y^{23} + \dots - 16y + 1$
$c_2$	$y^{24} - 12y^{23} + \dots - 612y + 1$
$c_3, c_8$	$y^{24} - 35y^{23} + \dots - 13312y + 4096$
$c_5$	$y^{24} - 40y^{23} + \dots - 16y + 1$
$c_6$	$y^{24} - 33y^{23} + \dots - 11y + 1$
$c_7, c_{10}, c_{11}$	$y^{24} + 19y^{23} + \dots - 11y + 1$
$c_9$	$y^{24} - 53y^{23} + \dots + 17132945y + 316969$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.977245 + 0.071776I$ $a = 0.150461 + 0.477664I$ $b = -1.86833 + 0.85025I$	$-13.8937 + 5.6522I$	$-11.88129 - 3.05170I$
$u = -0.977245 - 0.071776I$ $a = 0.150461 - 0.477664I$ $b = -1.86833 - 0.85025I$	$-13.8937 - 5.6522I$	$-11.88129 + 3.05170I$
$u = -0.944342$ $a = -0.374599$ $b = 1.57977$	$-9.62200$	$-9.45700$
$u = -0.132356 + 1.101640I$ $a = 0.224192 - 1.262680I$ $b = -1.38202 + 0.85732I$	$2.09684 + 3.39237I$	$-6.49952 - 2.22048I$
$u = -0.132356 - 1.101640I$ $a = 0.224192 + 1.262680I$ $b = -1.38202 - 0.85732I$	$2.09684 - 3.39237I$	$-6.49952 + 2.22048I$
$u = 0.369901 + 1.056050I$ $a = 0.19239 - 1.75435I$ $b = 0.509437 + 0.688724I$	$-1.33599 - 3.11324I$	$-9.44737 + 3.66544I$
$u = 0.369901 - 1.056050I$ $a = 0.19239 + 1.75435I$ $b = 0.509437 - 0.688724I$	$-1.33599 + 3.11324I$	$-9.44737 - 3.66544I$
$u = 0.023030 + 1.170740I$ $a = 0.00332 + 1.52505I$ $b = 0.53462 - 1.45060I$	$3.34786 - 1.42933I$	$-3.02808 + 3.24576I$
$u = 0.023030 - 1.170740I$ $a = 0.00332 - 1.52505I$ $b = 0.53462 + 1.45060I$	$3.34786 + 1.42933I$	$-3.02808 - 3.24576I$
$u = 0.736962 + 0.245534I$ $a = 0.482708 + 0.172356I$ $b = 1.141730 - 0.517295I$	$-3.71809 - 1.00013I$	$-12.92204 + 1.61108I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.736962 - 0.245534I$ $a = 0.482708 - 0.172356I$ $b = 1.141730 + 0.517295I$	$-3.71809 + 1.00013I$	$-12.92204 - 1.61108I$
$u = 0.149866 + 1.301080I$ $a = 0.468754 + 1.001100I$ $b = -0.632329 - 1.109160I$	$3.26690 - 2.11293I$	$-4.50894 + 4.47286I$
$u = 0.149866 - 1.301080I$ $a = 0.468754 - 1.001100I$ $b = -0.632329 + 1.109160I$	$3.26690 + 2.11293I$	$-4.50894 - 4.47286I$
$u = -0.521270 + 1.255460I$ $a = 1.48874 - 0.97432I$ $b = -1.105310 - 0.534231I$	$-10.25040 - 0.34153I$	$-9.34191 - 0.16934I$
$u = -0.521270 - 1.255460I$ $a = 1.48874 + 0.97432I$ $b = -1.105310 + 0.534231I$	$-10.25040 + 0.34153I$	$-9.34191 + 0.16934I$
$u = -0.461477 + 1.300210I$ $a = -0.98110 + 1.48411I$ $b = 1.37119 - 0.77637I$	$-5.57948 + 5.01306I$	$-6.18016 - 2.85769I$
$u = -0.461477 - 1.300210I$ $a = -0.98110 - 1.48411I$ $b = 1.37119 + 0.77637I$	$-5.57948 - 5.01306I$	$-6.18016 + 2.85769I$
$u = 0.24692 + 1.39353I$ $a = -1.57305 + 0.00181I$ $b = 2.02058 - 0.67462I$	$1.55911 - 4.48321I$	$-9.00126 + 3.05253I$
$u = 0.24692 - 1.39353I$ $a = -1.57305 - 0.00181I$ $b = 2.02058 + 0.67462I$	$1.55911 + 4.48321I$	$-9.00126 - 3.05253I$
$u = -0.45937 + 1.35651I$ $a = 1.05212 - 2.06998I$ $b = -2.35956 + 1.45257I$	$-9.4212 + 10.7764I$	$-8.42021 - 5.67335I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.45937 - 1.35651I$ $a = 1.05212 + 2.06998I$ $b = -2.35956 - 1.45257I$	$-9.4212 - 10.7764I$	$-8.42021 + 5.67335I$
$u = 0.450904$ $a = 0.305459$ $b = -0.393799$	$-0.785516$	$-12.5270$
$u = -0.228245 + 0.158994I$ $a = 0.02603 - 2.87156I$ $b = -0.322979 - 0.586238I$	$-0.34648 - 1.75564I$	$-2.27719 + 2.42480I$
$u = -0.228245 - 0.158994I$ $a = 0.02603 + 2.87156I$ $b = -0.322979 + 0.586238I$	$-0.34648 + 1.75564I$	$-2.27719 - 2.42480I$

$$\text{II. } I_2^u = \langle -u^2a + b, u^2a + a^2 + u^2 + a - u + 2, u^3 - u^2 + 2u - 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} a \\ u^2a \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} a \\ u^2a \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -au + 2a \\ u^2a + au - a \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u^2 - u + 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ -u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^2 + a + u + 1 \\ u^2a - 2u + 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-5u^2a + 3au - 5u^2 - 4a + 5u - 16$



(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_5$	$(u^2 + u + 1)^3$
$c_3, c_8$	$u^6$
$c_4$	$(u^2 - u + 1)^3$
$c_6, c_9$	$(u^3 + u^2 - 1)^2$
$c_7$	$(u^3 - u^2 + 2u - 1)^2$
$c_{10}, c_{11}$	$(u^3 + u^2 + 2u + 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$ $c_5$	$(y^2 + y + 1)^3$
$c_3, c_8$	$y^6$
$c_6, c_9$	$(y^3 - y^2 + 2y - 1)^2$
$c_7, c_{10}, c_{11}$	$(y^3 + 3y^2 + 2y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.215080 + 1.307140I$ $a = 0.818128 + 0.292480I$ $b = -1.52448 - 0.02619I$	$3.02413 - 0.79824I$	$-6.43615 - 0.68567I$
$u = 0.215080 + 1.307140I$ $a = -0.155769 - 0.854759I$ $b = 0.73956 + 1.33333I$	$3.02413 - 4.85801I$	$-2.88198 + 6.08229I$
$u = 0.215080 - 1.307140I$ $a = 0.818128 - 0.292480I$ $b = -1.52448 + 0.02619I$	$3.02413 + 0.79824I$	$-6.43615 + 0.68567I$
$u = 0.215080 - 1.307140I$ $a = -0.155769 + 0.854759I$ $b = 0.73956 - 1.33333I$	$3.02413 + 4.85801I$	$-2.88198 - 6.08229I$
$u = 0.569840$ $a = -0.662359 + 1.147240I$ $b = -0.215080 + 0.372529I$	$-1.11345 + 2.02988I$	$-12.18187 - 4.49037I$
$u = 0.569840$ $a = -0.662359 - 1.147240I$ $b = -0.215080 - 0.372529I$	$-1.11345 - 2.02988I$	$-12.18187 + 4.49037I$

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u^2 + u + 1)^3)(u^{24} + 4u^{23} + \dots + 8u + 1)$
$c_2$	$((u^2 + u + 1)^3)(u^{24} + 16u^{23} + \dots - 16u + 1)$
$c_3, c_8$	$u^6(u^{24} - u^{23} + \dots - 96u - 64)$
$c_4$	$((u^2 - u + 1)^3)(u^{24} + 4u^{23} + \dots + 8u + 1)$
$c_5$	$((u^2 + u + 1)^3)(u^{24} - 4u^{23} + \dots + 2u + 1)$
$c_6$	$((u^3 + u^2 - 1)^2)(u^{24} + 3u^{23} + \dots + u - 1)$
$c_7$	$((u^3 - u^2 + 2u - 1)^2)(u^{24} - 3u^{23} + \dots + 5u - 1)$
$c_9$	$((u^3 + u^2 - 1)^2)(u^{24} - 13u^{23} + \dots - 995u + 563)$
$c_{10}, c_{11}$	$((u^3 + u^2 + 2u + 1)^2)(u^{24} - 3u^{23} + \dots + 5u - 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$((y^2 + y + 1)^3)(y^{24} + 16y^{23} + \dots - 16y + 1)$
$c_2$	$((y^2 + y + 1)^3)(y^{24} - 12y^{23} + \dots - 612y + 1)$
$c_3, c_8$	$y^6(y^{24} - 35y^{23} + \dots - 13312y + 4096)$
$c_5$	$((y^2 + y + 1)^3)(y^{24} - 40y^{23} + \dots - 16y + 1)$
$c_6$	$((y^3 - y^2 + 2y - 1)^2)(y^{24} - 33y^{23} + \dots - 11y + 1)$
$c_7, c_{10}, c_{11}$	$((y^3 + 3y^2 + 2y - 1)^2)(y^{24} + 19y^{23} + \dots - 11y + 1)$
$c_9$	$((y^3 - y^2 + 2y - 1)^2)(y^{24} - 53y^{23} + \dots + 1.71329 \times 10^7 y + 316969)$