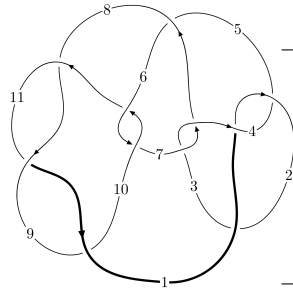
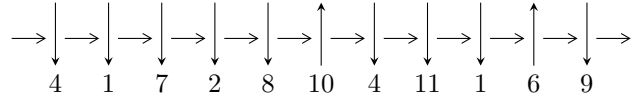


# 11n<sub>27</sub> (K11n<sub>27</sub>)



A knot diagram<sup>1</sup>

## Linearized knot diagram



## Solving Sequence

$$8,11 \xrightarrow{c_8} 9 \xrightarrow{c_{11}} 1,4 \xrightarrow{c_1} 2 \xrightarrow{c_9} 10 \xrightarrow{c_7} 7 \xrightarrow{c_3} 3 \xrightarrow{c_6} 6 \xrightarrow{c_5} 5 \longrightarrow c_2, c_4, c_{10}$$

## Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$I_1^u = \langle 2085u^{15} - 3383u^{14} + \dots + 4922b + 953, -953u^{15} + 5897u^{14} + \dots + 4922a + 34271, \\ u^{16} - 4u^{15} + \dots - 10u + 1 \rangle$$

$$I_2^u = \langle b, -u^2 + a - u + 1, u^5 + u^4 - 2u^3 - u^2 + u - 1 \rangle$$

$$I_3^u = \langle b - a - 1, a^2 + a - 1, u - 1 \rangle$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 23 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle 2085u^{15} - 3383u^{14} + \dots + 4922b + 953, -953u^{15} + 5897u^{14} + \dots + 4922a + 34271, u^{16} - 4u^{15} + \dots - 10u + 1 \rangle$$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.193620u^{15} - 1.19809u^{14} + \dots - 13.7284u - 6.96282 \\ -0.423608u^{15} + 0.687322u^{14} + \dots - 4.02662u - 0.193620 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.108899u^{15} - 0.139374u^{14} + \dots - 12.8663u - 4.79846 \\ -0.576392u^{15} + 1.31268u^{14} + \dots - 4.97338u + 0.193620 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.878505u^{15} - 2.34579u^{14} + \dots - 4.05607u - 3.47664 \\ 1.00264u^{15} - 2.16640u^{14} + \dots + 3.58818u - 0.728769 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0.0534336u^{15} - 0.366315u^{14} + \dots - 11.4854u - 4.89740 \\ 0.340309u^{15} - 0.439456u^{14} + \dots - 2.29277u - 0.129825 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0.136936u^{15} - 0.626981u^{14} + \dots - 5.58228u - 3.01463 \\ -0.576392u^{15} + 1.31268u^{14} + \dots - 4.97338u + 0.193620 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -0.439456u^{15} + 0.685697u^{14} + \dots - 10.5557u - 2.82101 \\ -0.576392u^{15} + 1.31268u^{14} + \dots - 4.97338u + 0.193620 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -0.439456u^{15} + 0.685697u^{14} + \dots - 10.5557u - 2.82101 \\ -0.576392u^{15} + 1.31268u^{14} + \dots - 4.97338u + 0.193620 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = \frac{2411}{2461}u^{15} - \frac{4233}{2461}u^{14} + \dots + \frac{28620}{2461}u - \frac{24444}{2461}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_4$	$u^{16} - 7u^{15} + \dots + 3u + 1$
$c_2$	$u^{16} + 29u^{15} + \dots + 17u + 1$
$c_3, c_7$	$u^{16} + 2u^{15} + \dots + 72u^2 - 32$
$c_5$	$u^{16} - 3u^{15} + \dots + u - 1$
$c_6, c_{10}$	$u^{16} - 2u^{15} + \dots - 20u - 4$
$c_8, c_9, c_{11}$	$u^{16} - 4u^{15} + \dots - 10u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$y^{16} - 29y^{15} + \dots - 17y + 1$
$c_2$	$y^{16} - 77y^{15} + \dots - 1761y + 1$
$c_3, c_7$	$y^{16} - 36y^{15} + \dots - 4608y + 1024$
$c_5$	$y^{16} - 37y^{15} + \dots - 11y + 1$
$c_6, c_{10}$	$y^{16} + 18y^{15} + \dots - 168y + 16$
$c_8, c_9, c_{11}$	$y^{16} - 20y^{15} + \dots - 146y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.852448 + 0.278896I$ $a = 0.25417 - 1.55665I$ $b = 0.434441 + 0.614956I$	$-3.23204 + 0.76102I$	$-14.1078 + 3.1845I$
$u = -0.852448 - 0.278896I$ $a = 0.25417 + 1.55665I$ $b = 0.434441 - 0.614956I$	$-3.23204 - 0.76102I$	$-14.1078 - 3.1845I$
$u = -1.11713$ $a = 1.01314$ $b = 0.393183$	$-2.15355$	$-1.76420$
$u = 0.727902$ $a = 1.19391$ $b = 1.74112$	$-10.0599$	$-3.26620$
$u = -0.665595 + 1.107720I$ $a = 0.109829 - 0.996426I$ $b = -2.57424 + 0.30502I$	$-16.5506 + 3.5813I$	$-12.12116 - 2.15994I$
$u = -0.665595 - 1.107720I$ $a = 0.109829 + 0.996426I$ $b = -2.57424 - 0.30502I$	$-16.5506 - 3.5813I$	$-12.12116 + 2.15994I$
$u = -0.374592 + 0.413898I$ $a = 0.238036 - 0.835224I$ $b = -0.289006 + 0.411875I$	$-0.428790 + 1.166930I$	$-5.36023 - 5.57896I$
$u = -0.374592 - 0.413898I$ $a = 0.238036 + 0.835224I$ $b = -0.289006 - 0.411875I$	$-0.428790 - 1.166930I$	$-5.36023 + 5.57896I$
$u = 1.49641 + 0.19521I$ $a = -0.467729 - 0.212663I$ $b = -0.140592 - 0.934027I$	$-6.69050 - 3.49798I$	$-9.87558 + 1.25665I$
$u = 1.49641 - 0.19521I$ $a = -0.467729 + 0.212663I$ $b = -0.140592 + 0.934027I$	$-6.69050 + 3.49798I$	$-9.87558 - 1.25665I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.70971$ $a = 2.04995$ $b = 2.70628$	-19.0073	-12.9680
$u = 1.67172 + 0.41923I$ $a = -1.56150 + 0.78878I$ $b = -2.44091 - 0.95623I$	$15.4222 - 9.3337I$	$-13.42948 + 3.49093I$
$u = 1.67172 - 0.41923I$ $a = -1.56150 - 0.78878I$ $b = -2.44091 + 0.95623I$	$15.4222 + 9.3337I$	$-13.42948 - 3.49093I$
$u = 1.73172 + 0.08246I$ $a = 1.31289 - 0.53629I$ $b = 1.88369 - 1.19369I$	$-12.66300 - 2.31460I$	$-13.80105 + 1.17558I$
$u = 1.73172 - 0.08246I$ $a = 1.31289 + 0.53629I$ $b = 1.88369 + 1.19369I$	$-12.66300 + 2.31460I$	$-13.80105 - 1.17558I$
$u = 0.0844975$ $a = -8.02839$ $b = -0.587345$	-1.09573	-8.61160

$$\text{II. } I_2^u = \langle b, -u^2 + a - u + 1, u^5 + u^4 - 2u^3 - u^2 + u - 1 \rangle$$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^2 + u - 1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^2 - 1 \\ -u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^2 + u - 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^3 + 2u \\ u^3 - u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u \\ u^3 - u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u \\ u^3 - u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $2u^4 - 3u^3 - 2u^2 + 8u - 14$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$(u - 1)^5$
$c_2, c_4$	$(u + 1)^5$
$c_3, c_7$	$u^5$
$c_5$	$u^5 - 3u^4 + 4u^3 - u^2 - u + 1$
$c_6$	$u^5 - u^4 + 2u^3 - u^2 + u - 1$
$c_8, c_9$	$u^5 + u^4 - 2u^3 - u^2 + u - 1$
$c_{10}$	$u^5 + u^4 + 2u^3 + u^2 + u + 1$
$c_{11}$	$u^5 - u^4 - 2u^3 + u^2 + u + 1$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y - 1)^5$
$c_3, c_7$	$y^5$
$c_5$	$y^5 - y^4 + 8y^3 - 3y^2 + 3y - 1$
$c_6, c_{10}$	$y^5 + 3y^4 + 4y^3 + y^2 - y - 1$
$c_8, c_9, c_{11}$	$y^5 - 5y^4 + 8y^3 - 3y^2 - y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.21774$ $a = 1.70062$ $b = 0$	-4.04602	-8.24330
$u = 0.309916 + 0.549911I$ $a = -0.896438 + 0.890762I$ $b = 0$	$-1.97403 - 1.53058I$	$-10.50099 + 3.45976I$
$u = 0.309916 - 0.549911I$ $a = -0.896438 - 0.890762I$ $b = 0$	$-1.97403 + 1.53058I$	$-10.50099 - 3.45976I$
$u = -1.41878 + 0.21917I$ $a = -0.453870 - 0.402731I$ $b = 0$	$-7.51750 + 4.40083I$	$-14.3774 - 5.8297I$
$u = -1.41878 - 0.21917I$ $a = -0.453870 + 0.402731I$ $b = 0$	$-7.51750 - 4.40083I$	$-14.3774 + 5.8297I$

$$\text{III. } I_3^u = \langle b - a - 1, a^2 + a - 1, u - 1 \rangle$$

**(i) Arc colorings**

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} a \\ a + 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -2 \\ -a - 2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ -a - 2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} a \\ -a - 2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ -a - 2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -a - 2 \\ -a - 2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -a - 2 \\ -a - 2 \end{pmatrix}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes = -21**

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3$	$u^2 + u - 1$
$c_2$	$u^2 + 3u + 1$
$c_4, c_7$	$u^2 - u - 1$
$c_5$	$u^2 - 3u + 1$
$c_6, c_{10}$	$u^2$
$c_8, c_9$	$(u - 1)^2$
$c_{11}$	$(u + 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_4$ $c_7$	$y^2 - 3y + 1$
$c_2, c_5$	$y^2 - 7y + 1$
$c_6, c_{10}$	$y^2$
$c_8, c_9, c_{11}$	$(y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$ $a = 0.618034$ $b = 1.61803$	-10.5276	-21.0000
$u = 1.00000$ $a = -1.61803$ $b = -0.618034$	-2.63189	-21.0000

#### IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u - 1)^5)(u^2 + u - 1)(u^{16} - 7u^{15} + \dots + 3u + 1)$
$c_2$	$((u + 1)^5)(u^2 + 3u + 1)(u^{16} + 29u^{15} + \dots + 17u + 1)$
$c_3$	$u^5(u^2 + u - 1)(u^{16} + 2u^{15} + \dots + 72u^2 - 32)$
$c_4$	$((u + 1)^5)(u^2 - u - 1)(u^{16} - 7u^{15} + \dots + 3u + 1)$
$c_5$	$(u^2 - 3u + 1)(u^5 - 3u^4 + \dots - u + 1)(u^{16} - 3u^{15} + \dots + u - 1)$
$c_6$	$u^2(u^5 - u^4 + \dots + u - 1)(u^{16} - 2u^{15} + \dots - 20u - 4)$
$c_7$	$u^5(u^2 - u - 1)(u^{16} + 2u^{15} + \dots + 72u^2 - 32)$
$c_8, c_9$	$((u - 1)^2)(u^5 + u^4 + \dots + u - 1)(u^{16} - 4u^{15} + \dots - 10u + 1)$
$c_{10}$	$u^2(u^5 + u^4 + \dots + u + 1)(u^{16} - 2u^{15} + \dots - 20u - 4)$
$c_{11}$	$((u + 1)^2)(u^5 - u^4 + \dots + u + 1)(u^{16} - 4u^{15} + \dots - 10u + 1)$

### V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$((y-1)^5)(y^2-3y+1)(y^{16}-29y^{15}+\dots-17y+1)$
$c_2$	$((y-1)^5)(y^2-7y+1)(y^{16}-77y^{15}+\dots-1761y+1)$
$c_3, c_7$	$y^5(y^2-3y+1)(y^{16}-36y^{15}+\dots-4608y+1024)$
$c_5$	$(y^2-7y+1)(y^5-y^4+\dots+3y-1)(y^{16}-37y^{15}+\dots-11y+1)$
$c_6, c_{10}$	$y^2(y^5+3y^4+\dots-y-1)(y^{16}+18y^{15}+\dots-168y+16)$
$c_8, c_9, c_{11}$	$((y-1)^2)(y^5-5y^4+\dots-y-1)(y^{16}-20y^{15}+\dots-146y+1)$