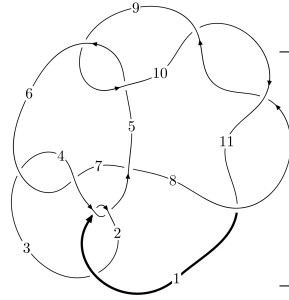
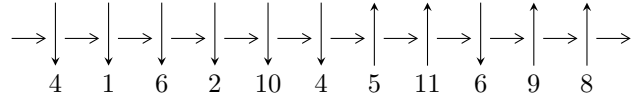


11n<sub>29</sub> (K11n<sub>29</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$5,10 \xrightarrow{c_5} 2,6 \xrightarrow{c_4} 4 \xrightarrow{c_6} 7 \xrightarrow{c_1} 1 \xrightarrow{c_3} 3 \xrightarrow{c_9} 9 \xrightarrow{c_{10}} 11 \xrightarrow{c_8} 8 \longrightarrow c_2, c_7, c_{11}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle u^{27} - u^{26} + \dots + b + 2u, u^{25} - u^{24} + \dots + a - 2, u^{29} - 2u^{28} + \dots + 3u - 1 \rangle$$

$$I_2^u = \langle b + 1, -u^2 + a - u, u^4 + u^3 + u^2 + 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 33 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I_1^u = \langle u^{27} - u^{26} + \dots + b + 2u, u^{25} - u^{24} + \dots + a - 2, u^{29} - 2u^{28} + \dots + 3u - 1 \rangle \quad \text{I.}$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^{25} + u^{24} + \dots - 3u + 2 \\ -u^{27} + u^{26} + \dots + 2u^2 - 2u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^{27} + u^{26} + \dots - 4u + 3 \\ -u^{27} + u^{26} + \dots + u^2 - u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^7 - 2u^3 \\ u^7 + u^5 + 2u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^7 - 2u^3 \\ -u^9 - u^7 - 3u^5 - 2u^3 - u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^{28} - 3u^{27} + \dots - 8u + 4 \\ -u^{28} - u^{27} + \dots - 6u^3 - u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^3 \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^5 + u \\ u^7 + u^5 + 2u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^5 + u \\ u^7 + u^5 + 2u^3 + u \end{pmatrix}$$

(ii) Obstruction class = -1

$$\begin{aligned} \text{(iii) Cusp Shapes} &= -4u^{28} + 4u^{27} - 19u^{26} + 14u^{25} - 67u^{24} + 43u^{23} - 162u^{22} + 82u^{21} - \\ &317u^{20} + 116u^{19} - 481u^{18} + 100u^{17} - 607u^{16} + 2u^{15} - 600u^{14} - 158u^{13} - 488u^{12} - \\ &304u^{11} - 310u^{10} - 342u^9 - 172u^8 - 265u^7 - 92u^6 - 122u^5 - 65u^4 - 24u^3 - 29u^2 + 4u - 7 \end{aligned}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_4$	$u^{29} - 5u^{28} + \dots - 5u + 1$
$c_2$	$u^{29} + 9u^{28} + \dots + 13u + 1$
$c_3, c_6$	$u^{29} - u^{28} + \dots + 8u + 16$
$c_5, c_9$	$u^{29} + 2u^{28} + \dots + 3u + 1$
$c_7$	$u^{29} + 2u^{28} + \dots + 3u + 1$
$c_8, c_{10}, c_{11}$	$u^{29} - 8u^{28} + \dots + 3u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$y^{29} - 9y^{28} + \dots + 13y - 1$
$c_2$	$y^{29} + 27y^{28} + \dots - 111y - 1$
$c_3, c_6$	$y^{29} + 27y^{28} + \dots - 2752y - 256$
$c_5, c_9$	$y^{29} + 8y^{28} + \dots + 3y - 1$
$c_7$	$y^{29} - 32y^{28} + \dots + 3y - 1$
$c_8, c_{10}, c_{11}$	$y^{29} + 28y^{28} + \dots + 123y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.231265 + 1.046420I$		
$a = -1.57334 - 1.28254I$	$7.61033 - 0.10509I$	$1.75140 - 0.82130I$
$b = 0.858634 + 0.959440I$		
$u = -0.231265 - 1.046420I$		
$a = -1.57334 + 1.28254I$	$7.61033 + 0.10509I$	$1.75140 + 0.82130I$
$b = 0.858634 - 0.959440I$		
$u = -0.312663 + 1.045390I$		
$a = -0.10596 + 2.52791I$	$7.11886 + 6.67995I$	$0.53493 - 6.07824I$
$b = 1.014760 - 0.890779I$		
$u = -0.312663 - 1.045390I$		
$a = -0.10596 - 2.52791I$	$7.11886 - 6.67995I$	$0.53493 + 6.07824I$
$b = 1.014760 + 0.890779I$		
$u = 0.822501 + 0.730493I$		
$a = 0.512567 - 0.480050I$	$0.636180 - 0.689036I$	$-3.76307 + 1.94423I$
$b = 0.633017 + 0.915825I$		
$u = 0.822501 - 0.730493I$		
$a = 0.512567 + 0.480050I$	$0.636180 + 0.689036I$	$-3.76307 - 1.94423I$
$b = 0.633017 - 0.915825I$		
$u = 0.194951 + 0.848946I$		
$a = 0.90551 + 1.74398I$	$1.06975 - 1.85093I$	$1.30743 + 5.79968I$
$b = -0.405971 - 0.466803I$		
$u = 0.194951 - 0.848946I$		
$a = 0.90551 - 1.74398I$	$1.06975 + 1.85093I$	$1.30743 - 5.79968I$
$b = -0.405971 + 0.466803I$		
$u = 0.450225 + 0.741417I$		
$a = 0.877674 - 0.501097I$	$-0.03811 - 1.72919I$	$-0.45461 + 4.60784I$
$b = 0.282831 + 0.220896I$		
$u = 0.450225 - 0.741417I$		
$a = 0.877674 + 0.501097I$	$-0.03811 + 1.72919I$	$-0.45461 - 4.60784I$
$b = 0.282831 - 0.220896I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.788076 + 0.837379I$		
$a = 0.263911 + 0.556243I$	$-4.79824 + 0.50805I$	$-6.89911 - 0.01309I$
$b = -0.840182 - 0.602881I$		
$u = -0.788076 - 0.837379I$		
$a = 0.263911 - 0.556243I$	$-4.79824 - 0.50805I$	$-6.89911 + 0.01309I$
$b = -0.840182 + 0.602881I$		
$u = 0.882629 + 0.776302I$		
$a = 0.523074 + 0.300180I$	$-0.78075 + 5.57785I$	$-5.50657 - 2.77090I$
$b = 1.103310 - 0.772041I$		
$u = 0.882629 - 0.776302I$		
$a = 0.523074 - 0.300180I$	$-0.78075 - 5.57785I$	$-5.50657 + 2.77090I$
$b = 1.103310 + 0.772041I$		
$u = 0.784724 + 0.886082I$		
$a = -1.19979 + 1.01167I$	$-6.30586 - 2.95151I$	$-5.76823 + 2.64939I$
$b = -1.337190 - 0.029086I$		
$u = 0.784724 - 0.886082I$		
$a = -1.19979 - 1.01167I$	$-6.30586 + 2.95151I$	$-5.76823 - 2.64939I$
$b = -1.337190 + 0.029086I$		
$u = -0.767855 + 0.926785I$		
$a = -0.44228 - 1.68632I$	$-4.52351 + 5.35315I$	$-5.93805 - 5.66710I$
$b = -0.771267 + 0.660663I$		
$u = -0.767855 - 0.926785I$		
$a = -0.44228 + 1.68632I$	$-4.52351 - 5.35315I$	$-5.93805 + 5.66710I$
$b = -0.771267 - 0.660663I$		
$u = 0.750471 + 0.994480I$		
$a = -0.996828 + 0.026809I$	$1.43095 - 5.20261I$	$-2.56531 + 3.25116I$
$b = 0.648434 - 1.004480I$		
$u = 0.750471 - 0.994480I$		
$a = -0.996828 - 0.026809I$	$1.43095 + 5.20261I$	$-2.56531 - 3.25116I$
$b = 0.648434 + 1.004480I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.866458 + 0.916553I$		
$a = 0.906367 + 0.416512I$	$-7.73749 + 3.20954I$	$-0.41591 - 2.86957I$
$b = 0.675975 - 0.021605I$		
$u = -0.866458 - 0.916553I$		
$a = 0.906367 - 0.416512I$	$-7.73749 - 3.20954I$	$-0.41591 + 2.86957I$
$b = 0.675975 + 0.021605I$		
$u = -0.719374 + 0.070912I$		
$a = 0.523981 - 0.369051I$	$3.96205 - 3.12839I$	$-4.70122 + 2.58517I$
$b = 0.914734 + 0.838366I$		
$u = -0.719374 - 0.070912I$		
$a = 0.523981 + 0.369051I$	$3.96205 + 3.12839I$	$-4.70122 - 2.58517I$
$b = 0.914734 - 0.838366I$		
$u = 0.793942 + 1.004110I$		
$a = 1.14222 - 1.86384I$	$-0.06814 - 11.79740I$	$-4.44971 + 7.37898I$
$b = 1.130840 + 0.799307I$		
$u = 0.793942 - 1.004110I$		
$a = 1.14222 + 1.86384I$	$-0.06814 + 11.79740I$	$-4.44971 - 7.37898I$
$b = 1.130840 - 0.799307I$		
$u = -0.146225 + 0.649247I$		
$a = 0.11069 - 2.17375I$	$-1.181700 + 0.773921I$	$-1.52981 + 2.72477I$
$b = -1.073810 + 0.142900I$		
$u = -0.146225 - 0.649247I$		
$a = 0.11069 + 2.17375I$	$-1.181700 - 0.773921I$	$-1.52981 - 2.72477I$
$b = -1.073810 - 0.142900I$		
$u = 0.304949$		
$a = 1.10441$	$-1.01334$	$-10.2040$
$b = -0.668226$		

$$\text{II. } I_2^u = \langle b + 1, -u^2 + a - u, u^4 + u^3 + u^2 + 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^2 + u \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^2 + u + 1 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^2 + u + 1 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^3 \\ u^3 + u^2 + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $5u^2 + 6u - 7$



(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$(u - 1)^4$
$c_2, c_4$	$(u + 1)^4$
$c_3, c_6$	$u^4$
$c_5$	$u^4 + u^3 + u^2 + 1$
$c_7, c_{10}, c_{11}$	$u^4 - u^3 + 3u^2 - 2u + 1$
$c_8$	$u^4 + u^3 + 3u^2 + 2u + 1$
$c_9$	$u^4 - u^3 + u^2 + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y - 1)^4$
$c_3, c_6$	$y^4$
$c_5, c_9$	$y^4 + y^3 + 3y^2 + 2y + 1$
$c_7, c_8, c_{10}$ $c_{11}$	$y^4 + 5y^3 + 7y^2 + 2y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.351808 + 0.720342I$ $a = -0.043315 + 1.227190I$ $b = -1.00000$	$-1.43393 - 1.41510I$	$-6.86477 + 6.85627I$
$u = 0.351808 - 0.720342I$ $a = -0.043315 - 1.227190I$ $b = -1.00000$	$-1.43393 + 1.41510I$	$-6.86477 - 6.85627I$
$u = -0.851808 + 0.911292I$ $a = -0.956685 - 0.641200I$ $b = -1.00000$	$-8.43568 + 3.16396I$	$-12.63523 - 2.29471I$
$u = -0.851808 - 0.911292I$ $a = -0.956685 + 0.641200I$ $b = -1.00000$	$-8.43568 - 3.16396I$	$-12.63523 + 2.29471I$

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u - 1)^4)(u^{29} - 5u^{28} + \dots - 5u + 1)$
$c_2$	$((u + 1)^4)(u^{29} + 9u^{28} + \dots + 13u + 1)$
$c_3, c_6$	$u^4(u^{29} - u^{28} + \dots + 8u + 16)$
$c_4$	$((u + 1)^4)(u^{29} - 5u^{28} + \dots - 5u + 1)$
$c_5$	$(u^4 + u^3 + u^2 + 1)(u^{29} + 2u^{28} + \dots + 3u + 1)$
$c_7$	$(u^4 - u^3 + 3u^2 - 2u + 1)(u^{29} + 2u^{28} + \dots + 3u + 1)$
$c_8$	$(u^4 + u^3 + 3u^2 + 2u + 1)(u^{29} - 8u^{28} + \dots + 3u + 1)$
$c_9$	$(u^4 - u^3 + u^2 + 1)(u^{29} + 2u^{28} + \dots + 3u + 1)$
$c_{10}, c_{11}$	$(u^4 - u^3 + 3u^2 - 2u + 1)(u^{29} - 8u^{28} + \dots + 3u + 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$((y - 1)^4)(y^{29} - 9y^{28} + \dots + 13y - 1)$
$c_2$	$((y - 1)^4)(y^{29} + 27y^{28} + \dots - 111y - 1)$
$c_3, c_6$	$y^4(y^{29} + 27y^{28} + \dots - 2752y - 256)$
$c_5, c_9$	$(y^4 + y^3 + 3y^2 + 2y + 1)(y^{29} + 8y^{28} + \dots + 3y - 1)$
$c_7$	$(y^4 + 5y^3 + 7y^2 + 2y + 1)(y^{29} - 32y^{28} + \dots + 3y - 1)$
$c_8, c_{10}, c_{11}$	$(y^4 + 5y^3 + 7y^2 + 2y + 1)(y^{29} + 28y^{28} + \dots + 123y - 1)$