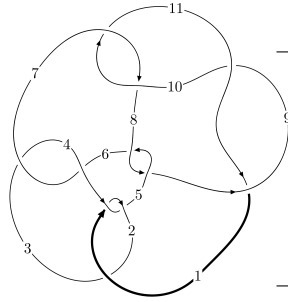
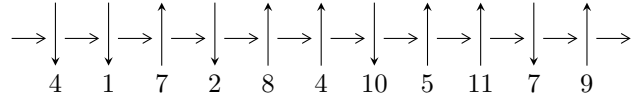


# 11n<sub>32</sub> (K11n<sub>32</sub>)



A knot diagram<sup>1</sup>

## Linearized knot diagram



## Solving Sequence

$$7,10 \xrightarrow{c_7} 8 \xrightarrow{c_{10}} 4,11 \xrightarrow{c_3} 3 \xrightarrow{c_6} 6 \xrightarrow{c_5} 5 \xrightarrow{c_9} 9 \xrightarrow{c_{11}} 1 \xrightarrow{c_2} 2 \longrightarrow c_1, c_4, c_8$$

## Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$I_1^u = \langle 19332758361u^{37} + 38734840795u^{36} + \dots + 237713005774b - 28141164923, \\ -1588415703u^{37} - 117670058213u^{36} + \dots + 237713005774a + 597215892201, \\ u^{38} + 2u^{37} + \dots - 3u + 1 \rangle$$

$$I_2^u = \langle b, -u^3 - 2u^2 + a - 2u, u^4 + u^3 + u^2 + 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 42 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle 1.93 \times 10^{10} u^{37} + 3.87 \times 10^{10} u^{36} + \dots + 2.38 \times 10^{11} b - 2.81 \times 10^{10}, -1.59 \times 10^9 u^{37} - 1.18 \times 10^{11} u^{36} + \dots + 2.38 \times 10^{11} a + 5.97 \times 10^{11}, u^{38} + 2u^{37} + \dots - 3u + 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.00668207u^{37} + 0.495009u^{36} + \dots + 2.86415u - 2.51234 \\ -0.0813281u^{37} - 0.162948u^{36} + \dots + 1.48580u + 0.118383 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0.0880102u^{37} + 0.657957u^{36} + \dots + 1.37835u - 2.63072 \\ -0.0813281u^{37} - 0.162948u^{36} + \dots + 1.48580u + 0.118383 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0.398557u^{37} + 0.370367u^{36} + \dots + 1.42515u - 1.31533 \\ 0.825719u^{37} + 1.65248u^{36} + \dots - 2.59421u + 0.826766 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0.397978u^{37} - 0.632706u^{36} + \dots + 2.34056u - 1.71535 \\ 1.43070u^{37} + 2.85936u^{36} + \dots - 5.59937u + 1.82868 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^3 \\ u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^5 - u \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.196219u^{37} + 0.547563u^{36} + \dots + 2.31038u - 3.08666 \\ 0.243984u^{37} + 0.488844u^{36} + \dots + 0.542588u + 0.644851 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.196219u^{37} + 0.547563u^{36} + \dots + 2.31038u - 3.08666 \\ 0.243984u^{37} + 0.488844u^{36} + \dots + 0.542588u + 0.644851 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= -\frac{159159118679}{118856502887} u^{37} - \frac{28323238958}{118856502887} u^{36} + \dots + \frac{412587165626}{118856502887} u - \frac{634600057867}{118856502887}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_4$	$u^{38} - 5u^{37} + \dots + u + 1$
$c_2$	$u^{38} + 15u^{37} + \dots - 81u + 1$
$c_3, c_6$	$u^{38} + 5u^{37} + \dots + 104u + 16$
$c_5, c_8$	$u^{38} + 2u^{37} + \dots + u + 1$
$c_7, c_{10}$	$u^{38} - 2u^{37} + \dots + 3u + 1$
$c_9, c_{11}$	$u^{38} - 14u^{37} + \dots - 7u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$y^{38} - 15y^{37} + \cdots + 81y + 1$
$c_2$	$y^{38} + 21y^{37} + \cdots - 2859y + 1$
$c_3, c_6$	$y^{38} - 27y^{37} + \cdots - 320y + 256$
$c_5, c_8$	$y^{38} + 10y^{37} + \cdots + 7y + 1$
$c_7, c_{10}$	$y^{38} + 14y^{37} + \cdots + 7y + 1$
$c_9, c_{11}$	$y^{38} + 22y^{37} + \cdots + 179y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.832670 + 0.614929I$ $a = -0.103257 - 0.153512I$ $b = -1.139290 - 0.198092I$	$0.789901 + 0.872417I$	$0.203682 - 1.029460I$
$u = 0.832670 - 0.614929I$ $a = -0.103257 + 0.153512I$ $b = -1.139290 + 0.198092I$	$0.789901 - 0.872417I$	$0.203682 + 1.029460I$
$u = 0.524709 + 0.798298I$ $a = 1.72507 + 2.99817I$ $b = -0.278602 + 0.363866I$	$-1.79987 - 1.63683I$	$0.6342 + 22.3814I$
$u = 0.524709 - 0.798298I$ $a = 1.72507 - 2.99817I$ $b = -0.278602 - 0.363866I$	$-1.79987 + 1.63683I$	$0.6342 - 22.3814I$
$u = -0.878464 + 0.565928I$ $a = -0.118175 - 0.080326I$ $b = 1.32611 - 0.72615I$	$-0.48850 - 8.10053I$	$-2.17285 + 4.60397I$
$u = -0.878464 - 0.565928I$ $a = -0.118175 + 0.080326I$ $b = 1.32611 + 0.72615I$	$-0.48850 + 8.10053I$	$-2.17285 - 4.60397I$
$u = -0.628453 + 0.715455I$ $a = -1.32808 + 0.68300I$ $b = 0.55366 + 1.35876I$	$-3.24288 - 0.91080I$	$-5.85440 + 2.87226I$
$u = -0.628453 - 0.715455I$ $a = -1.32808 - 0.68300I$ $b = 0.55366 - 1.35876I$	$-3.24288 + 0.91080I$	$-5.85440 - 2.87226I$
$u = -0.638347 + 0.845542I$ $a = -1.27115 + 1.10932I$ $b = 1.52004 - 0.19492I$	$-4.60338 + 2.49292I$	$-7.66096 - 3.58742I$
$u = -0.638347 - 0.845542I$ $a = -1.27115 - 1.10932I$ $b = 1.52004 + 0.19492I$	$-4.60338 - 2.49292I$	$-7.66096 + 3.58742I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.842903 + 0.381952I$ $a = -0.152164 - 0.103068I$ $b = 1.156070 - 0.287792I$	$0.57801 - 4.07433I$	$-1.00107 + 5.21688I$
$u = 0.842903 - 0.381952I$ $a = -0.152164 + 0.103068I$ $b = 1.156070 + 0.287792I$	$0.57801 + 4.07433I$	$-1.00107 - 5.21688I$
$u = 0.563322 + 0.919944I$ $a = -0.76392 - 1.40999I$ $b = -0.162866 - 0.630461I$	$-1.35379 - 2.75023I$	$-1.67570 - 2.67847I$
$u = 0.563322 - 0.919944I$ $a = -0.76392 + 1.40999I$ $b = -0.162866 + 0.630461I$	$-1.35379 + 2.75023I$	$-1.67570 + 2.67847I$
$u = 0.361485 + 0.817539I$ $a = -0.685289 - 0.170023I$ $b = 0.230395 + 0.298664I$	$0.31225 - 1.54508I$	$2.23777 + 4.87383I$
$u = 0.361485 - 0.817539I$ $a = -0.685289 + 0.170023I$ $b = 0.230395 - 0.298664I$	$0.31225 + 1.54508I$	$2.23777 - 4.87383I$
$u = -0.628379 + 0.944326I$ $a = 1.065350 + 0.455542I$ $b = 0.26079 - 1.59013I$	$-2.54932 + 5.85938I$	$-3.38157 - 9.01726I$
$u = -0.628379 - 0.944326I$ $a = 1.065350 - 0.455542I$ $b = 0.26079 + 1.59013I$	$-2.54932 - 5.85938I$	$-3.38157 + 9.01726I$
$u = -0.060400 + 1.136280I$ $a = 2.28811 - 0.57277I$ $b = -1.53818 + 0.08244I$	$7.11789 - 0.13853I$	$5.96603 - 0.12241I$
$u = -0.060400 - 1.136280I$ $a = 2.28811 + 0.57277I$ $b = -1.53818 - 0.08244I$	$7.11789 + 0.13853I$	$5.96603 + 0.12241I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.724985 + 0.458617I$ $a = -0.059958 - 0.272456I$ $b = -1.32367 + 0.54173I$	$1.89024 - 2.00477I$	$0.55164 + 1.57531I$
$u = -0.724985 - 0.458617I$ $a = -0.059958 + 0.272456I$ $b = -1.32367 - 0.54173I$	$1.89024 + 2.00477I$	$0.55164 - 1.57531I$
$u = 0.068191 + 1.190830I$ $a = -2.23931 + 0.30504I$ $b = 1.45402 - 0.43836I$	$6.16601 - 6.56194I$	$4.09697 + 5.13849I$
$u = 0.068191 - 1.190830I$ $a = -2.23931 - 0.30504I$ $b = 1.45402 + 0.43836I$	$6.16601 + 6.56194I$	$4.09697 - 5.13849I$
$u = 0.019048 + 0.780202I$ $a = -0.406821 - 0.905002I$ $b = -0.275945 + 0.814062I$	$0.77944 - 1.52604I$	$4.36193 + 4.60900I$
$u = 0.019048 - 0.780202I$ $a = -0.406821 + 0.905002I$ $b = -0.275945 - 0.814062I$	$0.77944 + 1.52604I$	$4.36193 - 4.60900I$
$u = -0.619321 + 1.057560I$ $a = 1.77643 - 1.22273I$ $b = -1.62072 - 0.63223I$	$3.58657 + 7.12992I$	$2.46388 - 6.33493I$
$u = -0.619321 - 1.057560I$ $a = 1.77643 + 1.22273I$ $b = -1.62072 + 0.63223I$	$3.58657 - 7.12992I$	$2.46388 + 6.33493I$
$u = 0.593324 + 1.105700I$ $a = -0.99629 - 1.25159I$ $b = 1.233010 + 0.050062I$	$2.77951 - 1.18659I$	$2.30827 - 0.46017I$
$u = 0.593324 - 1.105700I$ $a = -0.99629 + 1.25159I$ $b = 1.233010 - 0.050062I$	$2.77951 + 1.18659I$	$2.30827 + 0.46017I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.876704 + 0.917775I$		
$a = 0.013016 + 0.303072I$	$-8.01967 + 3.23855I$	$7.49106 - 4.17157I$
$b = 0.533786 + 0.030166I$		
$u = -0.876704 - 0.917775I$		
$a = 0.013016 - 0.303072I$	$-8.01967 - 3.23855I$	$7.49106 + 4.17157I$
$b = 0.533786 - 0.030166I$		
$u = 0.701663 + 1.057650I$		
$a = 0.93271 + 1.41473I$	$2.13442 - 6.62776I$	$1.31703 + 5.48212I$
$b = -1.259830 + 0.356568I$		
$u = 0.701663 - 1.057650I$		
$a = 0.93271 - 1.41473I$	$2.13442 + 6.62776I$	$1.31703 - 5.48212I$
$b = -1.259830 - 0.356568I$		
$u = -0.696643 + 1.086410I$		
$a = -1.70797 + 1.24411I$	$1.10073 + 13.93900I$	$-0.18114 - 8.68220I$
$b = 1.43940 + 0.79817I$		
$u = -0.696643 - 1.086410I$		
$a = -1.70797 - 1.24411I$	$1.10073 - 13.93900I$	$-0.18114 + 8.68220I$
$b = 1.43940 - 0.79817I$		
$u = 0.244381 + 0.216056I$		
$a = -2.96831 + 1.33736I$	$-1.88768 - 0.79705I$	$-5.20475 - 0.93842I$
$b = 0.391833 + 0.533554I$		
$u = 0.244381 - 0.216056I$		
$a = -2.96831 - 1.33736I$	$-1.88768 + 0.79705I$	$-5.20475 + 0.93842I$
$b = 0.391833 - 0.533554I$		



$$\text{II. } I_2^u = \langle b, -u^3 - 2u^2 + a - 2u, u^4 + u^3 + u^2 + 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^3 + 2u^2 + 2u \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^3 + 2u^2 + 2u \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^2 + 1 \\ -u^3 - u^2 - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^3 \\ u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^2 - 1 \\ u^3 + u^2 + 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^3 + u^2 + 2u - 1 \\ u^3 + u^2 + 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^3 + u^2 + 2u - 1 \\ u^3 + u^2 + 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-3u^3 + 3u^2 + 8u$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$(u - 1)^4$
$c_2, c_4$	$(u + 1)^4$
$c_3, c_6$	$u^4$
$c_5, c_9$	$u^4 + u^3 + 3u^2 + 2u + 1$
$c_7$	$u^4 + u^3 + u^2 + 1$
$c_8, c_{11}$	$u^4 - u^3 + 3u^2 - 2u + 1$
$c_{10}$	$u^4 - u^3 + u^2 + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y - 1)^4$
$c_3, c_6$	$y^4$
$c_5, c_8, c_9$ $c_{11}$	$y^4 + 5y^3 + 7y^2 + 2y + 1$
$c_7, c_{10}$	$y^4 + y^3 + 3y^2 + 2y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.351808 + 0.720342I$ $a = -0.59074 + 2.34806I$ $b = 0$	$-1.43393 - 1.41510I$	$3.14142 + 7.60220I$
$u = 0.351808 - 0.720342I$ $a = -0.59074 - 2.34806I$ $b = 0$	$-1.43393 + 1.41510I$	$3.14142 - 7.60220I$
$u = -0.851808 + 0.911292I$ $a = -0.409261 - 0.055548I$ $b = 0$	$-8.43568 + 3.16396I$	$-11.64142 - 1.04769I$
$u = -0.851808 - 0.911292I$ $a = -0.409261 + 0.055548I$ $b = 0$	$-8.43568 - 3.16396I$	$-11.64142 + 1.04769I$

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u-1)^4)(u^{38} - 5u^{37} + \dots + u + 1)$
$c_2$	$((u+1)^4)(u^{38} + 15u^{37} + \dots - 81u + 1)$
$c_3, c_6$	$u^4(u^{38} + 5u^{37} + \dots + 104u + 16)$
$c_4$	$((u+1)^4)(u^{38} - 5u^{37} + \dots + u + 1)$
$c_5$	$(u^4 + u^3 + 3u^2 + 2u + 1)(u^{38} + 2u^{37} + \dots + u + 1)$
$c_7$	$(u^4 + u^3 + u^2 + 1)(u^{38} - 2u^{37} + \dots + 3u + 1)$
$c_8$	$(u^4 - u^3 + 3u^2 - 2u + 1)(u^{38} + 2u^{37} + \dots + u + 1)$
$c_9$	$(u^4 + u^3 + 3u^2 + 2u + 1)(u^{38} - 14u^{37} + \dots - 7u + 1)$
$c_{10}$	$(u^4 - u^3 + u^2 + 1)(u^{38} - 2u^{37} + \dots + 3u + 1)$
$c_{11}$	$(u^4 - u^3 + 3u^2 - 2u + 1)(u^{38} - 14u^{37} + \dots - 7u + 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$((y - 1)^4)(y^{38} - 15y^{37} + \dots + 81y + 1)$
$c_2$	$((y - 1)^4)(y^{38} + 21y^{37} + \dots - 2859y + 1)$
$c_3, c_6$	$y^4(y^{38} - 27y^{37} + \dots - 320y + 256)$
$c_5, c_8$	$(y^4 + 5y^3 + 7y^2 + 2y + 1)(y^{38} + 10y^{37} + \dots + 7y + 1)$
$c_7, c_{10}$	$(y^4 + y^3 + 3y^2 + 2y + 1)(y^{38} + 14y^{37} + \dots + 7y + 1)$
$c_9, c_{11}$	$(y^4 + 5y^3 + 7y^2 + 2y + 1)(y^{38} + 22y^{37} + \dots + 179y + 1)$