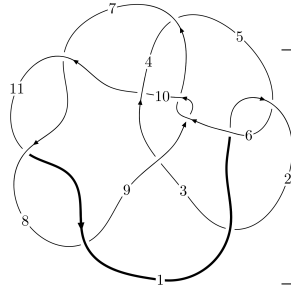
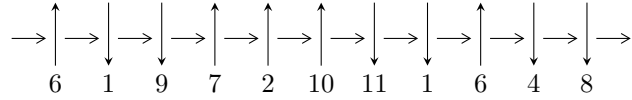


11n₈₂ (K11n₈₂)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$1,6 \xrightarrow{c_1} 2 \xrightarrow{c_2} 3,9 \xrightarrow{c_9} 10 \xrightarrow{c_6} 7 \xrightarrow{c_5} 5 \xrightarrow{c_4} 4 \xrightarrow{c_8} 8 \xrightarrow{c_{11}} 11 \rightsquigarrow c_3, c_7, c_{10}$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle -30181087379u^{14} - 63482369835u^{13} + \dots + 286209328348b - 329512457510, \\ 222459805170u^{14} + 486064128543u^{13} + \dots + 286209328348a + 3182822169919, \\ u^{15} + 2u^{14} + \dots + 10u - 1 \rangle$$

$$I_2^u = \langle b^2 - 2, a - u - 1, u^2 + u + 1 \rangle$$

$$I_3^u = \langle b, a + u + 1, u^2 + u + 1 \rangle$$

* 3 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 21 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -3.02 \times 10^{10}u^{14} - 6.35 \times 10^{10}u^{13} + \dots + 2.86 \times 10^{11}b - 3.30 \times 10^{11}, 2.22 \times 10^{11}u^{14} + 4.86 \times 10^{11}u^{13} + \dots + 2.86 \times 10^{11}a + 3.18 \times 10^{12}, u^{15} + 2u^{14} + \dots + 10u - 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -0.777263u^{14} - 1.69828u^{13} + \dots - 20.7871u - 11.1206 \\ 0.105451u^{14} + 0.221804u^{13} + \dots + 3.04137u + 1.15130 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -0.777263u^{14} - 1.69828u^{13} + \dots - 20.7871u - 11.1206 \\ 0.0983887u^{14} + 0.190365u^{13} + \dots + 2.38106u + 1.29506 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1.21619u^{14} + 2.44009u^{13} + \dots + 22.7698u + 12.4895 \\ -0.0983778u^{14} - 0.210858u^{13} + \dots - 1.81717u - 1.45285 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -1.42791u^{14} - 2.95841u^{13} + \dots - 31.0375u - 14.0034 \\ 0.156497u^{14} + 0.304479u^{13} + \dots + 2.72370u + 1.69949 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -0.671811u^{14} - 1.47648u^{13} + \dots - 17.7458u - 9.96931 \\ 0.105451u^{14} + 0.221804u^{13} + \dots + 3.04137u + 1.15130 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1.29506u^{14} + 2.68850u^{13} + \dots + 27.7863u + 15.3316 \\ -0.150085u^{14} - 0.291905u^{13} + \dots - 3.03487u - 1.79788 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1.29506u^{14} + 2.68850u^{13} + \dots + 27.7863u + 15.3316 \\ -0.150085u^{14} - 0.291905u^{13} + \dots - 3.03487u - 1.79788 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= -\frac{127706987601}{286209328348}u^{14} - \frac{268342154629}{286209328348}u^{13} + \dots - \frac{2023089158227}{286209328348}u - \frac{132460189755}{71552332087}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_5	$u^{15} - 2u^{14} + \dots + 10u + 1$
c_2	$u^{15} + 26u^{14} + \dots + 130u - 1$
c_3	$u^{15} - 27u^{13} + \dots - 294u + 181$
c_4	$u^{15} + 2u^{14} + \dots - 26u - 29$
c_6, c_9	$u^{15} - 3u^{14} + \dots + 11u + 7$
c_7, c_8, c_{11}	$u^{15} + u^{14} + \dots - 12u + 4$
c_{10}	$u^{15} + 2u^{14} + \dots + 2u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_5	$y^{15} + 26y^{14} + \dots + 130y - 1$
c_2	$y^{15} - 70y^{14} + \dots + 19426y - 1$
c_3	$y^{15} - 54y^{14} + \dots + 330786y - 32761$
c_4	$y^{15} + 18y^{14} + \dots - 5646y - 841$
c_6, c_9	$y^{15} + y^{14} + \dots - 61y - 49$
c_7, c_8, c_{11}	$y^{15} - 25y^{14} + \dots + 112y - 16$
c_{10}	$y^{15} + 2y^{14} + \dots + 10y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.803098 + 0.748670I$		
$a = 0.646315 + 0.226464I$	$0.89161 - 2.83187I$	$-3.17067 + 6.54660I$
$b = -0.574139 - 0.064590I$		
$u = -0.803098 - 0.748670I$		
$a = 0.646315 - 0.226464I$	$0.89161 + 2.83187I$	$-3.17067 - 6.54660I$
$b = -0.574139 + 0.064590I$		
$u = 0.289457 + 0.470166I$		
$a = -1.237560 - 0.324915I$	$-1.172960 - 0.777601I$	$-6.04145 + 2.77158I$
$b = 0.565034 + 0.450274I$		
$u = 0.289457 - 0.470166I$		
$a = -1.237560 + 0.324915I$	$-1.172960 + 0.777601I$	$-6.04145 - 2.77158I$
$b = 0.565034 - 0.450274I$		
$u = -0.231441 + 0.401782I$		
$a = -1.51486 - 1.67785I$	$1.80414 - 1.09347I$	$2.23827 - 2.22165I$
$b = -0.280610 + 0.385572I$		
$u = -0.231441 - 0.401782I$		
$a = -1.51486 + 1.67785I$	$1.80414 + 1.09347I$	$2.23827 + 2.22165I$
$b = -0.280610 - 0.385572I$		
$u = 0.31482 + 1.53771I$		
$a = 0.672510 + 0.519039I$	$-7.20728 - 4.71372I$	$-5.60542 + 4.01319I$
$b = -1.36446 - 0.54656I$		
$u = 0.31482 - 1.53771I$		
$a = 0.672510 - 0.519039I$	$-7.20728 + 4.71372I$	$-5.60542 - 4.01319I$
$b = -1.36446 + 0.54656I$		
$u = -0.70342 + 1.47150I$		
$a = -0.520487 + 0.299718I$	$-6.05090 - 1.57623I$	$-5.49718 + 1.52700I$
$b = 1.49730 - 0.27028I$		
$u = -0.70342 - 1.47150I$		
$a = -0.520487 - 0.299718I$	$-6.05090 + 1.57623I$	$-5.49718 - 1.52700I$
$b = 1.49730 + 0.27028I$		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.0846656$ $a = -13.3666$ $b = 1.46557$	-3.38897	-2.51440
$u = 0.44610 + 2.10573I$ $a = 0.766270 - 0.413924I$ $b = -1.95777 + 0.08885I$	$-19.5760 + 1.0165I$	$-5.21772 + 0.08752I$
$u = 0.44610 - 2.10573I$ $a = 0.766270 + 0.413924I$ $b = -1.95777 - 0.08885I$	$-19.5760 - 1.0165I$	$-5.21772 - 0.08752I$
$u = -0.35476 + 2.19036I$ $a = -0.628878 - 0.529570I$ $b = 1.88186 + 0.21032I$	$-18.8095 - 8.6900I$	$-4.44865 + 3.93161I$
$u = -0.35476 - 2.19036I$ $a = -0.628878 + 0.529570I$ $b = 1.88186 - 0.21032I$	$-18.8095 + 8.6900I$	$-4.44865 - 3.93161I$

$$\text{II. } I_2^u = \langle b^2 - 2, a - u - 1, u^2 + u + 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u + 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u \\ u + 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u + 1 \\ b \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u + 1 \\ b + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u - 1 \\ -b \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u \\ u + 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} b - u + 1 \\ -bu - u + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} b + u + 1 \\ b \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -bu - b - 1 \\ -2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -bu - b - 1 \\ -2 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $4u$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2, c_{10}	$(u^2 + u + 1)^2$
c_3	$u^4 - 2u^3 + 5u^2 + 2u + 1$
c_4	$u^4 + 2u^3 + 5u^2 - 2u + 1$
c_5	$(u^2 - u + 1)^2$
c_6	$(u - 1)^4$
c_7, c_8, c_{11}	$(u^2 - 2)^2$
c_9	$(u + 1)^4$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_5 c_{10}	$(y^2 + y + 1)^2$
c_3, c_4	$y^4 + 6y^3 + 35y^2 + 6y + 1$
c_6, c_9	$(y - 1)^4$
c_7, c_8, c_{11}	$(y - 2)^4$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.500000 + 0.866025I$ $a = 0.500000 + 0.866025I$ $b = 1.41421$	$-3.28987 - 2.02988I$	$-2.00000 + 3.46410I$
$u = -0.500000 + 0.866025I$ $a = 0.500000 + 0.866025I$ $b = -1.41421$	$-3.28987 - 2.02988I$	$-2.00000 + 3.46410I$
$u = -0.500000 - 0.866025I$ $a = 0.500000 - 0.866025I$ $b = 1.41421$	$-3.28987 + 2.02988I$	$-2.00000 - 3.46410I$
$u = -0.500000 - 0.866025I$ $a = 0.500000 - 0.866025I$ $b = -1.41421$	$-3.28987 + 2.02988I$	$-2.00000 - 3.46410I$

$$\text{III. } I_3^u = \langle b, a + u + 1, u^2 + u + 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u + 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u \\ u + 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u - 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u - 1 \\ -u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u - 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u \\ u + 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u + 1 \\ u + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u - 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $4u + 2$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2, c_3 c_4	$u^2 + u + 1$
c_5, c_{10}	$u^2 - u + 1$
c_6	$(u + 1)^2$
c_7, c_8, c_{11}	u^2
c_9	$(u - 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_3 c_4, c_5, c_{10}	$y^2 + y + 1$
c_6, c_9	$(y - 1)^2$
c_7, c_8, c_{11}	y^2

(vi) Complex Volumes and Cusp Shapes

Solutions to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.500000 + 0.866025I$ $a = -0.500000 - 0.866025I$ $b = 0$	$1.64493 - 2.02988I$	$0. + 3.46410I$
$u = -0.500000 - 0.866025I$ $a = -0.500000 + 0.866025I$ $b = 0$	$1.64493 + 2.02988I$	$0. - 3.46410I$

IV. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$((u^2 + u + 1)^3)(u^{15} - 2u^{14} + \dots + 10u + 1)$
c_2	$((u^2 + u + 1)^3)(u^{15} + 26u^{14} + \dots + 130u - 1)$
c_3	$(u^2 + u + 1)(u^4 - 2u^3 + \dots + 2u + 1)(u^{15} - 27u^{13} + \dots - 294u + 181)$
c_4	$(u^2 + u + 1)(u^4 + 2u^3 + \dots - 2u + 1)(u^{15} + 2u^{14} + \dots - 26u - 29)$
c_5	$((u^2 - u + 1)^3)(u^{15} - 2u^{14} + \dots + 10u + 1)$
c_6	$((u - 1)^4)(u + 1)^2(u^{15} - 3u^{14} + \dots + 11u + 7)$
c_7, c_8, c_{11}	$u^2(u^2 - 2)^2(u^{15} + u^{14} + \dots - 12u + 4)$
c_9	$((u - 1)^2)(u + 1)^4(u^{15} - 3u^{14} + \dots + 11u + 7)$
c_{10}	$(u^2 - u + 1)(u^2 + u + 1)^2(u^{15} + 2u^{14} + \dots + 2u - 1)$

V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1, c_5	$((y^2 + y + 1)^3)(y^{15} + 26y^{14} + \dots + 130y - 1)$
c_2	$((y^2 + y + 1)^3)(y^{15} - 70y^{14} + \dots + 19426y - 1)$
c_3	$(y^2 + y + 1)(y^4 + 6y^3 + 35y^2 + 6y + 1)$ $\cdot (y^{15} - 54y^{14} + \dots + 330786y - 32761)$
c_4	$(y^2 + y + 1)(y^4 + 6y^3 + \dots + 6y + 1)(y^{15} + 18y^{14} + \dots - 5646y - 841)$
c_6, c_9	$((y - 1)^6)(y^{15} + y^{14} + \dots - 61y - 49)$
c_7, c_8, c_{11}	$y^2(y - 2)^4(y^{15} - 25y^{14} + \dots + 112y - 16)$
c_{10}	$((y^2 + y + 1)^3)(y^{15} + 2y^{14} + \dots + 10y - 1)$