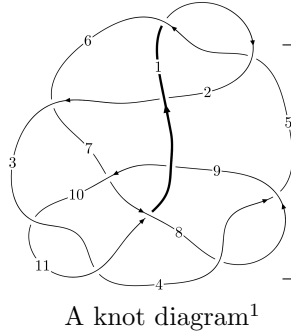
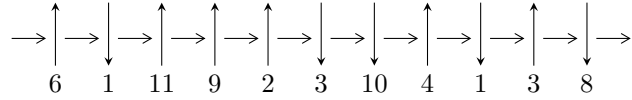


11n₉₂ (K11n₉₂)



Linearized knot diagram



Solving Sequence

$$3, 11 \xrightarrow{c_3} 4, 8 \xrightarrow{c_{11}} 1 \xrightarrow{c_2} 2 \xrightarrow{c_{10}} 10 \xrightarrow{c_7} 7 \xrightarrow{c_6} 6 \xrightarrow{c_5} 5 \xrightarrow{c_9} 9 \rightsquigarrow c_1, c_4, c_8$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle -74u^9 + 28u^8 + 589u^7 - 208u^6 - 1099u^5 + 580u^4 - 535u^3 - 218u^2 + 439b - 447u + 41, \\ -90u^9 - 49u^8 + 835u^7 + 364u^6 - 2357u^5 - 576u^4 + 1485u^3 - 277u^2 + 439a + 453u + 38, \\ u^{10} + u^9 - 8u^8 - 8u^7 + 16u^6 + 16u^5 + 3u^4 - 2u^3 + 2u + 1 \rangle$$

$$I_2^u = \langle -u^6 + u^5 + 3u^4 - 2u^3 - 2u^2 + b + u, u^4 - u^3 - 3u^2 + a + 2u + 2, u^7 - u^6 - 4u^5 + 3u^4 + 5u^3 - 2u^2 - 2u - 2 \rangle$$

$$I_3^u = \langle -2u^3 + 5u^2 + b + 2u - 12, 4u^3 - 11u^2 + 7a - 2u + 23, u^4 - u^3 - 4u^2 + 4u + 7 \rangle$$

* 3 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 21 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -74u^9 + 28u^8 + \cdots + 439b + 41, -90u^9 - 49u^8 + \cdots + 439a + 38, u^{10} + u^9 + \cdots + 2u + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0.205011u^9 + 0.111617u^8 + \cdots - 1.03189u - 0.0865604 \\ 0.168565u^9 - 0.0637813u^8 + \cdots + 1.01822u - 0.0933941 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.931663u^9 - 0.296128u^8 + \cdots - 1.34396u - 0.362187 \\ 0.558087u^9 + 0.248292u^8 + \cdots + 1.35763u + 0.542141 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1.39180u^9 - 0.635535u^8 + \cdots - 1.96128u - 1.32346 \\ 1.29841u^9 + 0.373576u^8 + \cdots + 1.46469u + 2.11845 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.275626u^9 + 0.138952u^8 + \cdots - 0.753986u + 0.239180 \\ 0.0979499u^9 - 0.0911162u^8 + \cdots + 0.740319u - 0.419134 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0.373576u^9 + 0.0478360u^8 + \cdots - 0.0136674u - 0.179954 \\ 0.0979499u^9 - 0.0911162u^8 + \cdots + 0.740319u - 0.419134 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -0.0933941u^9 - 0.261959u^8 + \cdots - 0.496583u - 1.20501 \\ -0.232346u^9 + 0.00683371u^8 + \cdots - 0.430524u - 0.168565 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.205011u^9 + 0.111617u^8 + \cdots - 0.0318907u - 0.0865604 \\ 0.168565u^9 - 0.0637813u^8 + \cdots + 1.01822u - 0.0933941 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.205011u^9 + 0.111617u^8 + \cdots - 0.0318907u - 0.0865604 \\ 0.168565u^9 - 0.0637813u^8 + \cdots + 1.01822u - 0.0933941 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= -\frac{1240}{439}u^9 - \frac{480}{439}u^8 + \frac{9846}{439}u^7 + \frac{3503}{439}u^6 - \frac{18914}{439}u^5 - \frac{5302}{439}u^4 - \frac{7197}{439}u^3 + \frac{1354}{439}u^2 - \frac{490}{439}u - \frac{452}{439}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_5	$u^{10} - 6u^9 + \dots - 10u + 4$
c_2	$u^{10} + 2u^9 + \dots + 20u + 16$
c_3, c_4, c_8 c_{10}	$u^{10} + u^9 - 8u^8 - 8u^7 + 16u^6 + 16u^5 + 3u^4 - 2u^3 + 2u + 1$
c_6	$u^{10} + 12u^9 + \dots + 1072u + 712$
c_7, c_9	$u^{10} + 2u^9 + \dots - 12u + 1$
c_{11}	$u^{10} + 5u^9 + 12u^8 + 15u^7 + 10u^6 + 4u^5 + 6u^4 + 8u^3 + 5u^2 + 3u + 2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_5	$y^{10} + 2y^9 + \dots + 20y + 16$
c_2	$y^{10} + 38y^9 + \dots + 3216y + 256$
c_3, c_4, c_8 c_{10}	$y^{10} - 17y^9 + \dots - 4y + 1$
c_6	$y^{10} + 68y^9 + \dots + 2222848y + 506944$
c_7, c_9	$y^{10} + 46y^9 + \dots - 38y + 1$
c_{11}	$y^{10} - y^9 + 14y^8 - 13y^7 + 54y^6 - 42y^5 + 30y^4 + 12y^3 + y^2 + 11y + 4$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.303786 + 0.554609I$		
$a = -1.19659 - 1.04112I$	$-1.58196 + 1.29510I$	$-1.93721 + 1.18186I$
$b = -0.210597 - 0.072758I$		
$u = -0.303786 - 0.554609I$		
$a = -1.19659 + 1.04112I$	$-1.58196 - 1.29510I$	$-1.93721 - 1.18186I$
$b = -0.210597 + 0.072758I$		
$u = -0.595593 + 0.161209I$		
$a = 1.251620 - 0.570638I$	$-0.62036 + 3.20996I$	$3.63110 - 5.43743I$
$b = -0.897475 + 0.589151I$		
$u = -0.595593 - 0.161209I$		
$a = 1.251620 + 0.570638I$	$-0.62036 - 3.20996I$	$3.63110 + 5.43743I$
$b = -0.897475 - 0.589151I$		
$u = 0.470796 + 0.374659I$		
$a = -0.742938 - 0.762785I$	$1.01700 + 1.01665I$	$4.69191 - 3.41900I$
$b = 0.262089 + 0.698748I$		
$u = 0.470796 - 0.374659I$		
$a = -0.742938 + 0.762785I$	$1.01700 - 1.01665I$	$4.69191 + 3.41900I$
$b = 0.262089 - 0.698748I$		
$u = 2.01532 + 0.15224I$		
$a = 0.624248 + 0.501185I$	$-19.7069 + 0.3487I$	$4.25811 + 0.03534I$
$b = -0.19806 - 2.25477I$		
$u = 2.01532 - 0.15224I$		
$a = 0.624248 - 0.501185I$	$-19.7069 - 0.3487I$	$4.25811 - 0.03534I$
$b = -0.19806 + 2.25477I$		
$u = -2.08674 + 0.29586I$		
$a = -0.436339 - 0.622756I$	$-19.4087 - 8.7708I$	$4.35608 + 3.79545I$
$b = 0.54405 + 2.41435I$		
$u = -2.08674 - 0.29586I$		
$a = -0.436339 + 0.622756I$	$-19.4087 + 8.7708I$	$4.35608 - 3.79545I$
$b = 0.54405 - 2.41435I$		

$$\text{II. } I_2^u = \langle -u^6 + u^5 + 3u^4 - 2u^3 - 2u^2 + b + u, u^4 - u^3 - 3u^2 + a + 2u + 2, u^7 - u^6 - 4u^5 + 3u^4 + 5u^3 - 2u^2 - 2u - 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^4 + u^3 + 3u^2 - 2u - 2 \\ u^6 - u^5 - 3u^4 + 2u^3 + 2u^2 - u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^6 + u^5 + 3u^4 - 2u^3 - 3u^2 + u + 2 \\ u^4 - u^3 - 2u^2 + 2u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^4 + 2u^3 + u^2 - 3u + 2 \\ -u^5 + 2u^4 + u^3 - 4u^2 + u + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^4 + 3u^2 - u - 2 \\ u^6 - u^5 - 3u^4 + 3u^3 + 2u^2 - 2u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^6 - u^5 - 4u^4 + 3u^3 + 5u^2 - 3u - 2 \\ u^6 - u^5 - 3u^4 + 3u^3 + 2u^2 - 2u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^5 + u^4 + 3u^3 - 3u^2 - 2u + 1 \\ u^5 - 3u^3 + 2u + 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^4 + u^3 + 3u^2 - 3u - 2 \\ u^6 - u^5 - 3u^4 + 3u^3 + 2u^2 - u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^4 + u^3 + 3u^2 - 3u - 2 \\ u^6 - u^5 - 3u^4 + 3u^3 + 2u^2 - u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $u^6 + 2u^5 - 8u^4 - 3u^3 + 12u^2$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$u^7 - u^6 + 2u^5 - 2u^4 + 2u^3 - 3u^2 + u - 1$
c_2	$u^7 + 3u^6 + 4u^5 - 6u^3 - 9u^2 - 5u - 1$
c_3, c_8	$u^7 - u^6 - 4u^5 + 3u^4 + 5u^3 - 2u^2 - 2u - 1$
c_4, c_{10}	$u^7 + u^6 - 4u^5 - 3u^4 + 5u^3 + 2u^2 - 2u + 1$
c_5	$u^7 + u^6 + 2u^5 + 2u^4 + 2u^3 + 3u^2 + u + 1$
c_6	$u^7 + 2u^6 - 2u^5 - 3u^4 - 3u^3 + 6u^2 - u + 1$
c_7, c_9	$u^7 + 2u^6 - u^5 - 3u^4 - 2u^3 + u^2 + 2u + 1$
c_{11}	$u^7 - 2u^6 + u^5 + 2u^4 - 3u^3 + u^2 + 2u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_5	$y^7 + 3y^6 + 4y^5 - 6y^3 - 9y^2 - 5y - 1$
c_2	$y^7 - y^6 + 4y^5 - 4y^4 + 2y^3 - 21y^2 + 7y - 1$
c_3, c_4, c_8 c_{10}	$y^7 - 9y^6 + 32y^5 - 57y^4 + 51y^3 - 18y^2 - 1$
c_6	$y^7 - 8y^6 + 10y^5 - 23y^4 + 45y^3 - 24y^2 - 11y - 1$
c_7, c_9	$y^7 - 6y^6 + 9y^5 - 5y^4 + 2y^3 - 3y^2 + 2y - 1$
c_{11}	$y^7 - 2y^6 + 3y^5 - 2y^4 + 5y^3 - 9y^2 + 6y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.212610 + 0.314318I$ $a = -0.186986 + 0.922572I$ $b = -0.25287 - 1.43719I$	$4.41567 + 1.74618I$	$3.81474 - 1.89982I$
$u = 1.212610 - 0.314318I$ $a = -0.186986 - 0.922572I$ $b = -0.25287 + 1.43719I$	$4.41567 - 1.74618I$	$3.81474 + 1.89982I$
$u = -1.303070 + 0.139348I$ $a = 0.819449 + 0.558129I$ $b = -0.275124 - 0.778615I$	$2.10492 - 4.17967I$	$2.47305 + 4.17814I$
$u = -1.303070 - 0.139348I$ $a = 0.819449 - 0.558129I$ $b = -0.275124 + 0.778615I$	$2.10492 + 4.17967I$	$2.47305 - 4.17814I$
$u = -0.278087 + 0.369158I$ $a = -1.48979 - 1.34313I$ $b = 0.466038 - 0.754209I$	$-1.45284 + 2.44043I$	$-0.66357 - 2.79895I$
$u = -0.278087 - 0.369158I$ $a = -1.48979 + 1.34313I$ $b = 0.466038 + 0.754209I$	$-1.45284 - 2.44043I$	$-0.66357 + 2.79895I$
$u = 1.73710$ $a = -0.285336$ $b = -0.876095$	6.31383	6.75150

III.

$$I_3^u = \langle -2u^3 + 5u^2 + b + 2u - 12, 4u^3 - 11u^2 + 7a - 2u + 23, u^4 - u^3 - 4u^2 + 4u + 7 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -\frac{4}{7}u^3 + \frac{11}{7}u^2 + \frac{2}{7}u - \frac{23}{7} \\ 2u^3 - 5u^2 - 2u + 12 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -\frac{5}{7}u^3 + \frac{12}{7}u^2 + \frac{6}{7}u - \frac{27}{7} \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} \frac{5}{7}u^3 - \frac{12}{7}u^2 - \frac{6}{7}u + \frac{34}{7} \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} \frac{10}{7}u^3 - \frac{24}{7}u^2 - \frac{12}{7}u + \frac{75}{7} \\ -2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} \frac{10}{7}u^3 - \frac{24}{7}u^2 - \frac{12}{7}u + \frac{61}{7} \\ -2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} \frac{15}{7}u^3 - \frac{36}{7}u^2 - \frac{18}{7}u + \frac{95}{7} \\ -3 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} \frac{3}{7}u^3 - \frac{3}{7}u^2 - \frac{12}{7}u + \frac{12}{7} \\ u^3 - 2u^2 + u + 5 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} \frac{3}{7}u^3 - \frac{3}{7}u^2 - \frac{12}{7}u + \frac{12}{7} \\ u^3 - 2u^2 + u + 5 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $-4u^3 + 8u^2 + 4u - 10$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_5	$(u + 1)^4$
c_2	$(u - 1)^4$
c_3, c_4, c_8 c_{10}	$u^4 - u^3 - 4u^2 + 4u + 7$
c_6	$(u + 2)^4$
c_7, c_9	$u^4 - 3u^3 + 2u^2 + 6u + 13$
c_{11}	$(u^2 - u + 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_5	$(y - 1)^4$
c_3, c_4, c_8 c_{10}	$y^4 - 9y^3 + 38y^2 - 72y + 49$
c_6	$(y - 4)^4$
c_7, c_9	$y^4 - 5y^3 + 66y^2 + 16y + 169$
c_{11}	$(y^2 + y + 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.328780 + 0.090174I$		
$a = 0.418587 - 0.623340I$	$6.57974 + 2.02988I$	$8.00000 - 3.46410I$
$b = 1.24248 + 1.97169I$		
$u = -1.328780 - 0.090174I$		
$a = 0.418587 + 0.623340I$	$6.57974 - 2.02988I$	$8.00000 + 3.46410I$
$b = 1.24248 - 1.97169I$		
$u = 1.82878 + 0.77585I$		
$a = -0.061444 + 0.499622I$	$6.57974 + 2.02988I$	$8.00000 - 3.46410I$
$b = 0.257518 - 1.105670I$		
$u = 1.82878 - 0.77585I$		
$a = -0.061444 - 0.499622I$	$6.57974 - 2.02988I$	$8.00000 + 3.46410I$
$b = 0.257518 + 1.105670I$		

IV. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$(u+1)^4(u^7 - u^6 + 2u^5 - 2u^4 + 2u^3 - 3u^2 + u - 1)$ $\cdot (u^{10} - 6u^9 + \dots - 10u + 4)$
c_2	$(u-1)^4(u^7 + 3u^6 + 4u^5 - 6u^3 - 9u^2 - 5u - 1)$ $\cdot (u^{10} + 2u^9 + \dots + 20u + 16)$
c_3, c_8	$(u^4 - u^3 - 4u^2 + 4u + 7)(u^7 - u^6 - 4u^5 + 3u^4 + 5u^3 - 2u^2 - 2u - 1)$ $\cdot (u^{10} + u^9 - 8u^8 - 8u^7 + 16u^6 + 16u^5 + 3u^4 - 2u^3 + 2u + 1)$
c_4, c_{10}	$(u^4 - u^3 - 4u^2 + 4u + 7)(u^7 + u^6 - 4u^5 - 3u^4 + 5u^3 + 2u^2 - 2u + 1)$ $\cdot (u^{10} + u^9 - 8u^8 - 8u^7 + 16u^6 + 16u^5 + 3u^4 - 2u^3 + 2u + 1)$
c_5	$(u+1)^4(u^7 + u^6 + 2u^5 + 2u^4 + 2u^3 + 3u^2 + u + 1)$ $\cdot (u^{10} - 6u^9 + \dots - 10u + 4)$
c_6	$(u+2)^4(u^7 + 2u^6 - 2u^5 - 3u^4 - 3u^3 + 6u^2 - u + 1)$ $\cdot (u^{10} + 12u^9 + \dots + 1072u + 712)$
c_7, c_9	$(u^4 - 3u^3 + 2u^2 + 6u + 13)(u^7 + 2u^6 + \dots + 2u + 1)$ $\cdot (u^{10} + 2u^9 + \dots - 12u + 1)$
c_{11}	$(u^2 - u + 1)^2(u^7 - 2u^6 + u^5 + 2u^4 - 3u^3 + u^2 + 2u - 1)$ $\cdot (u^{10} + 5u^9 + 12u^8 + 15u^7 + 10u^6 + 4u^5 + 6u^4 + 8u^3 + 5u^2 + 3u + 2)$

V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1, c_5	$(y-1)^4(y^7 + 3y^6 + 4y^5 - 6y^3 - 9y^2 - 5y - 1)$ $\cdot (y^{10} + 2y^9 + \dots + 20y + 16)$
c_2	$(y-1)^4(y^7 - y^6 + 4y^5 - 4y^4 + 2y^3 - 21y^2 + 7y - 1)$ $\cdot (y^{10} + 38y^9 + \dots + 3216y + 256)$
c_3, c_4, c_8 c_{10}	$(y^4 - 9y^3 + 38y^2 - 72y + 49)(y^7 - 9y^6 + \dots - 18y^2 - 1)$ $\cdot (y^{10} - 17y^9 + \dots - 4y + 1)$
c_6	$(y-4)^4(y^7 - 8y^6 + 10y^5 - 23y^4 + 45y^3 - 24y^2 - 11y - 1)$ $\cdot (y^{10} + 68y^9 + \dots + 2222848y + 506944)$
c_7, c_9	$(y^4 - 5y^3 + 66y^2 + 16y + 169)$ $\cdot (y^7 - 6y^6 + \dots + 2y - 1)(y^{10} + 46y^9 + \dots - 38y + 1)$
c_{11}	$(y^2 + y + 1)^2(y^7 - 2y^6 + 3y^5 - 2y^4 + 5y^3 - 9y^2 + 6y - 1)$ $\cdot (y^{10} - y^9 + 14y^8 - 13y^7 + 54y^6 - 42y^5 + 30y^4 + 12y^3 + y^2 + 11y + 4)$