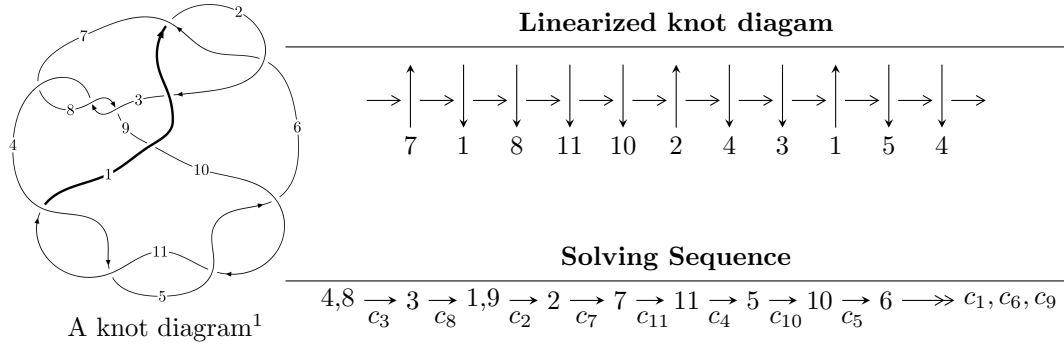


11n₁₃₉ (K11n₁₃₉)



Ideals for irreducible components² of X_{par}

$$I_1^u = \langle -7u^7 - 28u^6 - 53u^5 - 79u^4 - 15u^3 + 84u^2 + 188b - 97u + 43, \\ 21u^7 - 104u^6 + 159u^5 - 703u^4 + 797u^3 - 1380u^2 + 940a + 1043u - 1069, \\ u^8 + u^7 + 9u^6 + 2u^5 + 22u^4 - 5u^3 + 23u^2 + 6u + 5 \rangle$$

$$I_2^u = \langle b - a + 1, a^2 - au - 2a + u + 2, u^2 + 1 \rangle$$

* 2 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 12 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle -7u^7 - 28u^6 + \cdots + 188b + 43, 21u^7 - 104u^6 + \cdots + 940a - 1069, u^8 + u^7 + \cdots + 6u + 5 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.0223404u^7 + 0.110638u^6 + \cdots - 1.10957u + 1.13723 \\ 0.0372340u^7 + 0.148936u^6 + \cdots + 0.515957u - 0.228723 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.0861702u^7 - 0.144681u^6 + \cdots - 1.27979u + 1.24362 \\ -0.0265957u^7 - 0.106383u^6 + \cdots + 0.345745u - 0.122340 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.0148936u^7 + 0.259574u^6 + \cdots - 0.593617u + 0.908511 \\ 0.0372340u^7 + 0.148936u^6 + \cdots + 0.515957u - 0.228723 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0.107447u^7 + 0.229787u^6 + \cdots + 1.00319u + 1.05426 \\ 0.0425532u^7 + 0.170213u^6 + \cdots - 0.0531915u + 0.0957447 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.0989362u^7 - 0.204255u^6 + \cdots - 0.586170u + 0.0351064 \\ 0.0744681u^7 - 0.202128u^6 + \cdots + 0.531915u - 0.457447 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0.237234u^7 - 0.151064u^6 + \cdots + 1.11596u + 0.471277 \\ 0.0585106u^7 - 0.265957u^6 + \cdots - 0.760638u - 0.430851 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0.237234u^7 - 0.151064u^6 + \cdots + 1.11596u + 0.471277 \\ 0.0585106u^7 - 0.265957u^6 + \cdots - 0.760638u - 0.430851 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = -\frac{46}{47}u^7 - \frac{43}{47}u^6 - \frac{402}{47}u^5 - \frac{76}{47}u^4 - \frac{911}{47}u^3 + \frac{223}{47}u^2 - \frac{765}{47}u - \frac{362}{47}$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|--------------------------------|---|
| c_1, c_6 | $u^8 + u^7 - u^6 - 8u^5 + 2u^4 + 7u^3 + 5u^2 + 4u + 5$ |
| c_2 | $u^8 - 3u^7 + 21u^6 - 72u^5 + 108u^4 + 25u^3 - 11u^2 + 34u + 25$ |
| c_3, c_7, c_8 | $u^8 + u^7 + 9u^6 + 2u^5 + 22u^4 - 5u^3 + 23u^2 + 6u + 5$ |
| c_4, c_5, c_{10} c_{11} | $u^8 - u^7 + 8u^6 - 4u^5 + 18u^4 + 11u^2 + 5u + 2$ |
| c_9 | $u^8 + 11u^7 + 44u^6 + 62u^5 + 426u^4 - 1920u^3 + 1693u^2 - 389u + 136$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--------------------------------|---|
| c_1, c_6 | $y^8 - 3y^7 + 21y^6 - 72y^5 + 108y^4 + 25y^3 - 11y^2 + 34y + 25$ |
| c_2 | $y^8 + 33y^7 + \dots - 1706y + 625$ |
| c_3, c_7, c_8 | $y^8 + 17y^7 + 121y^6 + 448y^5 + 916y^4 + 1053y^3 + 809y^2 + 194y + 25$ |
| c_4, c_5, c_{10} c_{11} | $y^8 + 15y^7 + 92y^6 + 294y^5 + 514y^4 + 468y^3 + 193y^2 + 19y + 4$ |
| c_9 | $y^8 - 33y^7 + \dots + 309175y + 18496$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 0.611238 + 0.940914I$ | | |
| $a = 0.190317 - 0.232859I$ | $3.66920 - 1.06491I$ | $1.31198 + 1.63429I$ |
| $b = 0.234808 - 1.029490I$ | | |
| $u = 0.611238 - 0.940914I$ | | |
| $a = 0.190317 + 0.232859I$ | $3.66920 + 1.06491I$ | $1.31198 - 1.63429I$ |
| $b = 0.234808 + 1.029490I$ | | |
| $u = -0.187062 + 0.424849I$ | | |
| $a = 1.051840 - 0.641967I$ | $-0.482455 + 0.984921I$ | $-7.02443 - 7.03211I$ |
| $b = -0.258486 + 0.303432I$ | | |
| $u = -0.187062 - 0.424849I$ | | |
| $a = 1.051840 + 0.641967I$ | $-0.482455 - 0.984921I$ | $-7.02443 + 7.03211I$ |
| $b = -0.258486 - 0.303432I$ | | |
| $u = -0.45395 + 1.85746I$ | | |
| $a = -0.045979 + 0.950045I$ | $12.93020 - 1.89326I$ | $1.23462 + 1.04722I$ |
| $b = 0.36613 + 1.66771I$ | | |
| $u = -0.45395 - 1.85746I$ | | |
| $a = -0.045979 - 0.950045I$ | $12.93020 + 1.89326I$ | $1.23462 - 1.04722I$ |
| $b = 0.36613 - 1.66771I$ | | |
| $u = -0.47023 + 2.19541I$ | | |
| $a = -0.396174 - 1.205290I$ | $-12.82710 + 5.56972I$ | $0.47783 - 1.89693I$ |
| $b = 0.15755 - 1.96154I$ | | |
| $u = -0.47023 - 2.19541I$ | | |
| $a = -0.396174 + 1.205290I$ | $-12.82710 - 5.56972I$ | $0.47783 + 1.89693I$ |
| $b = 0.15755 + 1.96154I$ | | |

$$\text{II. } I_2^u = \langle b - a + 1, a^2 - au - 2a + u + 2, u^2 + 1 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} a \\ a - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a + 1 \\ a \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 2a - 1 \\ a - 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 2au + a - 2u - 2 \\ au - u - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} au - a - 3u + 1 \\ -a - u + 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -au \\ -au + u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -au \\ -au + u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 0

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|--------------------------------|--------------------------------|
| c_1, c_3, c_6 c_7, c_8 | $(u^2 + 1)^2$ |
| c_2 | $(u + 1)^4$ |
| c_4, c_5, c_{10} c_{11} | $u^4 + 3u^2 + 1$ |
| c_9 | $(u^2 - u - 1)^2$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--------------------------------|------------------------------------|
| c_1, c_3, c_6 c_7, c_8 | $(y + 1)^4$ |
| c_2 | $(y - 1)^4$ |
| c_4, c_5, c_{10} c_{11} | $(y^2 + 3y + 1)^2$ |
| c_9 | $(y^2 - 3y + 1)^2$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_2^u | | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|----------------------|------------------------|---------------------------------------|------------|
| $u =$ | $1.000000I$ | | |
| $a =$ | $1.000000 - 0.618034I$ | 0.986960 | 0 |
| $b =$ | $-0.618034I$ | | |
| $u =$ | $1.000000I$ | | |
| $a =$ | $1.000000 + 1.61803I$ | 8.88264 | 0 |
| $b =$ | $1.61803I$ | | |
| $u =$ | $-1.000000I$ | | |
| $a =$ | $1.000000 + 0.618034I$ | 0.986960 | 0 |
| $b =$ | $0.618034I$ | | |
| $u =$ | $-1.000000I$ | | |
| $a =$ | $1.000000 - 1.61803I$ | 8.88264 | 0 |
| $b =$ | $-1.61803I$ | | |

III. u-Polynomials

| Crossings | u-Polynomials at each crossing |
|--------------------------------|--|
| c_1, c_6 | $(u^2 + 1)^2(u^8 + u^7 - u^6 - 8u^5 + 2u^4 + 7u^3 + 5u^2 + 4u + 5)$ |
| c_2 | $((u + 1)^4)(u^8 - 3u^7 + \dots + 34u + 25)$ |
| c_3, c_7, c_8 | $(u^2 + 1)^2(u^8 + u^7 + 9u^6 + 2u^5 + 22u^4 - 5u^3 + 23u^2 + 6u + 5)$ |
| c_4, c_5, c_{10} c_{11} | $(u^4 + 3u^2 + 1)(u^8 - u^7 + 8u^6 - 4u^5 + 18u^4 + 11u^2 + 5u + 2)$ |
| c_9 | $(u^2 - u - 1)^2$ $\cdot (u^8 + 11u^7 + 44u^6 + 62u^5 + 426u^4 - 1920u^3 + 1693u^2 - 389u + 136)$ |

IV. Riley Polynomials

| Crossings | Riley Polynomials at each crossing |
|--------------------------------|---|
| c_1, c_6 | $((y + 1)^4)(y^8 - 3y^7 + \dots + 34y + 25)$ |
| c_2 | $((y - 1)^4)(y^8 + 33y^7 + \dots - 1706y + 625)$ |
| c_3, c_7, c_8 | $(y + 1)^4$ $\cdot (y^8 + 17y^7 + 121y^6 + 448y^5 + 916y^4 + 1053y^3 + 809y^2 + 194y + 25)$ |
| c_4, c_5, c_{10} c_{11} | $(y^2 + 3y + 1)^2$ $\cdot (y^8 + 15y^7 + 92y^6 + 294y^5 + 514y^4 + 468y^3 + 193y^2 + 19y + 4)$ |
| c_9 | $((y^2 - 3y + 1)^2)(y^8 - 33y^7 + \dots + 309175y + 18496)$ |