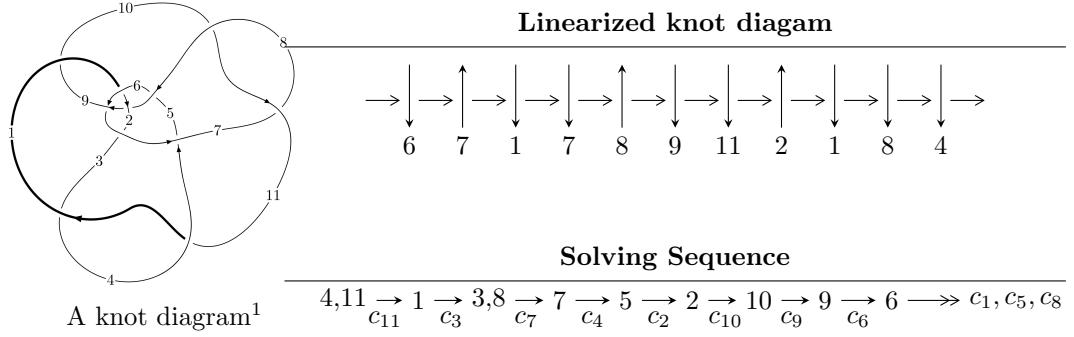


## $11n_{163}$ ( $K11n_{163}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$\begin{aligned}
 I_1^u &= \langle b - u, -45168u^{15} + 5735u^{14} + \dots + 12553a - 4016, \\
 &\quad u^{16} + 4u^{14} + 13u^{12} + 25u^{10} + 37u^8 + u^7 + 39u^6 + 5u^5 + 24u^4 + 7u^3 + 8u^2 + 2u + 1 \rangle \\
 I_2^u &= \langle 9.55720 \times 10^{54}u^{41} + 1.20936 \times 10^{55}u^{40} + \dots + 1.06854 \times 10^{57}b + 1.17356 \times 10^{57}, \\
 &\quad 1.73442 \times 10^{56}u^{41} + 5.21769 \times 10^{56}u^{40} + \dots + 1.06854 \times 10^{57}a + 1.20542 \times 10^{58}, u^{42} + 3u^{41} + \dots + 36u - \\
 I_3^u &= \langle b + u, 2u^6 - 4u^5 + 7u^4 - 6u^3 + 4u^2 + a - u - 1, u^7 - 2u^6 + 4u^5 - 4u^4 + 4u^3 - 2u^2 + u - 1 \rangle \\
 I_4^u &= \langle -u^5 + 2u^4 - 4u^3 + 5u^2 + b - 4u + 2, -u^4 + 2u^3 - 4u^2 + a + 5u - 3, u^6 - 2u^5 + 4u^4 - 5u^3 + 4u^2 - 2u + 1 \rangle
 \end{aligned}$$

\* 4 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 71 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle b-u, -45168u^{15} + 5735u^{14} + \cdots + 12553a - 4016, u^{16} + 4u^{14} + \cdots + 2u + 1 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 3.59818u^{15} - 0.456863u^{14} + \cdots + 6.71059u + 0.319924 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 3.59818u^{15} - 0.456863u^{14} + \cdots + 7.71059u + 0.319924 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -2.45439u^{15} - 4.20816u^{14} + \cdots - 29.2987u - 12.3139 \\ 1.39951u^{15} - 0.238270u^{14} + \cdots + 3.68446u - 0.456863 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -2.66016u^{15} - 2.57118u^{14} + \cdots - 20.1125u - 7.64885 \\ 0.808412u^{15} - 0.199793u^{14} + \cdots + 2.76149u - 0.218593 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.456863u^{15} + 1.39951u^{14} + \cdots + 6.87644u + 4.59818 \\ -u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.695133u^{15} + 1.99060u^{14} + \cdots + 10.1323u + 5.99769 \\ -0.0384769u^{15} - 0.336175u^{14} + \cdots - 1.42046u - 0.591094 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1.01418u^{15} - 1.83677u^{14} + \cdots - 6.42476u - 4.88361 \\ 0.591094u^{15} - 0.0384769u^{14} + \cdots + 1.92297u - 0.238270 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1.01418u^{15} - 1.83677u^{14} + \cdots - 6.42476u - 4.88361 \\ 0.591094u^{15} - 0.0384769u^{14} + \cdots + 1.92297u - 0.238270 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-\frac{31115}{12553}u^{15} + \frac{20322}{12553}u^{14} + \cdots - \frac{177549}{12553}u - \frac{9899}{12553}$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_6$	$u^{16} - u^{15} + \cdots - u + 1$
$c_2, c_5$	$u^{16} - u^{15} + \cdots + 15u^2 + 1$
$c_3, c_7, c_{10}$ $c_{11}$	$u^{16} + 4u^{14} + \cdots + 2u + 1$
$c_4$	$u^{16} - 13u^{15} + \cdots - 352u + 64$
$c_8$	$u^{16} - 13u^{15} + \cdots - 36u + 8$
$c_9$	$u^{16} - 16u^{15} + \cdots - 544u + 64$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_6$	$y^{16} - 3y^{15} + \cdots - 5y + 1$
$c_2, c_5$	$y^{16} + 9y^{15} + \cdots + 30y + 1$
$c_3, c_7, c_{10}$ $c_{11}$	$y^{16} + 8y^{15} + \cdots + 12y + 1$
$c_4$	$y^{16} + 5y^{15} + \cdots + 40448y + 4096$
$c_8$	$y^{16} - y^{15} + \cdots + 496y + 64$
$c_9$	$y^{16} - 4y^{15} + \cdots + 23552y + 4096$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.362872 + 0.921754I$		
$a = 0.762991 - 0.560929I$	$3.94475 + 1.12356I$	$1.32088 + 0.73756I$
$b = 0.362872 + 0.921754I$		
$u = 0.362872 - 0.921754I$		
$a = 0.762991 + 0.560929I$	$3.94475 - 1.12356I$	$1.32088 - 0.73756I$
$b = 0.362872 - 0.921754I$		
$u = -0.067924 + 1.048980I$		
$a = 0.59848 - 1.57127I$	$3.11555 + 2.14731I$	$-0.93627 - 3.92704I$
$b = -0.067924 + 1.048980I$		
$u = -0.067924 - 1.048980I$		
$a = 0.59848 + 1.57127I$	$3.11555 - 2.14731I$	$-0.93627 + 3.92704I$
$b = -0.067924 - 1.048980I$		
$u = 0.867369 + 0.851352I$		
$a = 0.39653 - 1.47637I$	$-4.45687 + 2.76976I$	$-6.60351 - 1.02062I$
$b = 0.867369 + 0.851352I$		
$u = 0.867369 - 0.851352I$		
$a = 0.39653 + 1.47637I$	$-4.45687 - 2.76976I$	$-6.60351 + 1.02062I$
$b = 0.867369 - 0.851352I$		
$u = -0.924080 + 0.993395I$		
$a = -0.062325 - 1.181310I$	$-2.56347 + 5.89381I$	$-14.0887 - 6.8568I$
$b = -0.924080 + 0.993395I$		
$u = -0.924080 - 0.993395I$		
$a = -0.062325 + 1.181310I$	$-2.56347 - 5.89381I$	$-14.0887 + 6.8568I$
$b = -0.924080 - 0.993395I$		
$u = -0.037947 + 0.609427I$		
$a = -4.09907 - 0.73703I$	$0.98282 - 4.26271I$	$-0.536037 - 0.693456I$
$b = -0.037947 + 0.609427I$		
$u = -0.037947 - 0.609427I$		
$a = -4.09907 + 0.73703I$	$0.98282 + 4.26271I$	$-0.536037 + 0.693456I$
$b = -0.037947 - 0.609427I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.74781 + 1.20294I$		
$a = -0.21869 - 1.80308I$	$-0.89621 + 7.24124I$	$-3.27217 - 13.36826I$
$b = -0.74781 + 1.20294I$		
$u = -0.74781 - 1.20294I$		
$a = -0.21869 + 1.80308I$	$-0.89621 - 7.24124I$	$-3.27217 + 13.36826I$
$b = -0.74781 - 1.20294I$		
$u = 0.82584 + 1.20295I$		
$a = 0.47696 - 1.60926I$	$-2.2047 - 16.1487I$	$-3.69661 + 9.09082I$
$b = 0.82584 + 1.20295I$		
$u = 0.82584 - 1.20295I$		
$a = 0.47696 + 1.60926I$	$-2.2047 + 16.1487I$	$-3.69661 - 9.09082I$
$b = 0.82584 - 1.20295I$		
$u = -0.278326 + 0.368111I$		
$a = 1.14513 - 0.86473I$	$-0.389238 + 1.281380I$	$-3.68762 - 5.53338I$
$b = -0.278326 + 0.368111I$		
$u = -0.278326 - 0.368111I$		
$a = 1.14513 + 0.86473I$	$-0.389238 - 1.281380I$	$-3.68762 + 5.53338I$
$b = -0.278326 - 0.368111I$		

$$\text{II. } I_2^u = \langle 9.56 \times 10^{54} u^{41} + 1.21 \times 10^{55} u^{40} + \dots + 1.07 \times 10^{57} b + 1.17 \times 10^{57}, 1.73 \times 10^{56} u^{41} + 5.22 \times 10^{56} u^{40} + \dots + 1.07 \times 10^{57} a + 1.21 \times 10^{58}, u^{42} + 3u^{41} + \dots + 36u - 1 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -0.162317u^{41} - 0.488303u^{40} + \dots + 6.42121u - 11.2810 \\ -0.00894419u^{41} - 0.0113179u^{40} + \dots - 3.72593u - 1.09829 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.171261u^{41} - 0.499621u^{40} + \dots + 2.69528u - 12.3793 \\ -0.00894419u^{41} - 0.0113179u^{40} + \dots - 3.72593u - 1.09829 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0.0765764u^{41} + 0.218473u^{40} + \dots - 9.92664u - 3.95597 \\ 0.0117602u^{41} + 0.0207404u^{40} + \dots - 5.71991u - 0.217988 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.0458921u^{41} + 0.116885u^{40} + \dots - 1.72493u - 3.74924 \\ -0.00981888u^{41} - 0.0511014u^{40} + \dots - 3.81460u - 0.236598 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -0.222058u^{41} - 0.640758u^{40} + \dots - 2.30612u - 12.3439 \\ 0.00407009u^{41} - 0.00144471u^{40} + \dots - 7.80288u - 1.22358 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -0.234716u^{41} - 0.693689u^{40} + \dots - 8.97199u - 13.5929 \\ -0.0134003u^{41} - 0.0709336u^{40} + \dots - 7.27710u - 1.23853 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0.245729u^{41} + 0.839363u^{40} + \dots + 9.37284u + 4.46731 \\ 0.0686483u^{41} + 0.146810u^{40} + \dots - 6.32759u + 0.755792 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0.245729u^{41} + 0.839363u^{40} + \dots + 9.37284u + 4.46731 \\ 0.0686483u^{41} + 0.146810u^{40} + \dots - 6.32759u + 0.755792 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $0.445546u^{41} + 1.05637u^{40} + \dots - 7.66940u + 9.51539$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_6$	$u^{42} - u^{41} + \cdots - 7u - 1$
$c_2, c_5$	$u^{42} + 7u^{40} + \cdots + 1895u + 457$
$c_3, c_7, c_{10}$ $c_{11}$	$u^{42} + 3u^{41} + \cdots + 36u - 1$
$c_4$	$(u^{21} + 8u^{20} + \cdots + 43u + 7)^2$
$c_8$	$(u^{21} + 6u^{20} + \cdots + 5u + 1)^2$
$c_9$	$(u^{21} + 6u^{20} + \cdots + 9u + 1)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_6$	$y^{42} - y^{41} + \cdots - 45y + 1$
$c_2, c_5$	$y^{42} + 14y^{41} + \cdots + 2544657y + 208849$
$c_3, c_7, c_{10}$ $c_{11}$	$y^{42} + 11y^{41} + \cdots - 1288y + 1$
$c_4$	$(y^{21} - 10y^{20} + \cdots + 1149y - 49)^2$
$c_8$	$(y^{21} + 2y^{20} + \cdots - 11y - 1)^2$
$c_9$	$(y^{21} - 8y^{20} + \cdots + 33y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.885119 + 0.440669I$		
$a = 0.437217 + 0.545665I$	$-3.16717 - 1.07030I$	$-12.89268 + 5.67416I$
$b = -0.998691 - 0.783756I$		
$u = -0.885119 - 0.440669I$		
$a = 0.437217 - 0.545665I$	$-3.16717 + 1.07030I$	$-12.89268 - 5.67416I$
$b = -0.998691 + 0.783756I$		
$u = -0.221318 + 0.954664I$		
$a = 1.023340 + 0.577719I$	$2.51518 + 5.37801I$	$0.71786 - 8.23406I$
$b = 0.715301 - 0.650320I$		
$u = -0.221318 - 0.954664I$		
$a = 1.023340 - 0.577719I$	$2.51518 - 5.37801I$	$0.71786 + 8.23406I$
$b = 0.715301 + 0.650320I$		
$u = 0.715301 + 0.650320I$		
$a = -1.186310 - 0.108494I$	$2.51518 - 5.37801I$	$0.71786 + 8.23406I$
$b = -0.221318 - 0.954664I$		
$u = 0.715301 - 0.650320I$		
$a = -1.186310 + 0.108494I$	$2.51518 + 5.37801I$	$0.71786 - 8.23406I$
$b = -0.221318 + 0.954664I$		
$u = 0.660616 + 0.665590I$		
$a = 0.142774 + 0.166906I$	$-3.87464 - 0.10689I$	$-16.3307 + 2.6685I$
$b = -1.181090 + 0.555383I$		
$u = 0.660616 - 0.665590I$		
$a = 0.142774 - 0.166906I$	$-3.87464 + 0.10689I$	$-16.3307 - 2.6685I$
$b = -1.181090 - 0.555383I$		
$u = 0.746526 + 0.760439I$		
$a = 0.567031 - 0.156980I$	$-2.33356 + 1.75773I$	$-7.03716 - 6.33959I$
$b = -0.884140 + 0.948082I$		
$u = 0.746526 - 0.760439I$		
$a = 0.567031 + 0.156980I$	$-2.33356 - 1.75773I$	$-7.03716 + 6.33959I$
$b = -0.884140 - 0.948082I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.549689 + 0.965680I$		
$a = 1.164290 + 0.499543I$	$0.21083 + 2.02252I$	$-3.27794 - 3.16369I$
$b = -0.011102 - 0.408161I$		
$u = -0.549689 - 0.965680I$		
$a = 1.164290 - 0.499543I$	$0.21083 - 2.02252I$	$-3.27794 + 3.16369I$
$b = -0.011102 + 0.408161I$		
$u = 0.587817 + 1.024500I$		
$a = -0.44869 + 1.75524I$	$-2.75188 - 4.82047I$	$-10.54242 + 4.40996I$
$b = -0.903022 - 0.809434I$		
$u = 0.587817 - 1.024500I$		
$a = -0.44869 - 1.75524I$	$-2.75188 + 4.82047I$	$-10.54242 - 4.40996I$
$b = -0.903022 + 0.809434I$		
$u = 0.112117 + 0.790036I$		
$a = 0.80867 - 3.05059I$	$5.06212 + 3.17952I$	$3.66314 + 2.07098I$
$b = -0.175620 + 1.395210I$		
$u = 0.112117 - 0.790036I$		
$a = 0.80867 + 3.05059I$	$5.06212 - 3.17952I$	$3.66314 - 2.07098I$
$b = -0.175620 - 1.395210I$		
$u = 0.716213 + 0.968774I$		
$a = -0.72128 + 1.60893I$	$-1.69311 - 7.34221I$	$-7.2251 + 12.7560I$
$b = -0.84147 - 1.24514I$		
$u = 0.716213 - 0.968774I$		
$a = -0.72128 - 1.60893I$	$-1.69311 + 7.34221I$	$-7.2251 - 12.7560I$
$b = -0.84147 + 1.24514I$		
$u = -1.20681$		
$a = 0.255916$	$-2.39902$	$9.38220$
$b = 0.0276533$		
$u = -0.903022 + 0.809434I$		
$a = 0.95127 + 1.48619I$	$-2.75188 + 4.82047I$	$-10.54242 - 4.40996I$
$b = 0.587817 - 1.024500I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.903022 - 0.809434I$		
$a = 0.95127 - 1.48619I$	$-2.75188 - 4.82047I$	$-10.54242 + 4.40996I$
$b = 0.587817 + 1.024500I$		
$u = 0.280918 + 0.724094I$		
$a = -0.42253 + 2.14926I$	$4.77684 - 4.89958I$	$-1.86079 + 9.83067I$
$b = -0.06930 - 1.59935I$		
$u = 0.280918 - 0.724094I$		
$a = -0.42253 - 2.14926I$	$4.77684 + 4.89958I$	$-1.86079 - 9.83067I$
$b = -0.06930 + 1.59935I$		
$u = 0.819992 + 0.955539I$		
$a = -0.487721 + 0.138368I$	$-4.12482 - 9.03603I$	$-5.90532 + 6.27658I$
$b = 1.170640 - 0.603687I$		
$u = 0.819992 - 0.955539I$		
$a = -0.487721 - 0.138368I$	$-4.12482 + 9.03603I$	$-5.90532 - 6.27658I$
$b = 1.170640 + 0.603687I$		
$u = -0.998691 + 0.783756I$		
$a = 0.529988 + 0.125234I$	$-3.16717 + 1.07030I$	$-12.89268 - 5.67416I$
$b = -0.885119 - 0.440669I$		
$u = -0.998691 - 0.783756I$		
$a = 0.529988 - 0.125234I$	$-3.16717 - 1.07030I$	$-12.89268 + 5.67416I$
$b = -0.885119 + 0.440669I$		
$u = -0.884140 + 0.948082I$		
$a = -0.108358 - 0.471345I$	$-2.33356 + 1.75773I$	$-7.03716 - 6.33959I$
$b = 0.746526 + 0.760439I$		
$u = -0.884140 - 0.948082I$		
$a = -0.108358 + 0.471345I$	$-2.33356 - 1.75773I$	$-7.03716 + 6.33959I$
$b = 0.746526 - 0.760439I$		
$u = -1.181090 + 0.555383I$		
$a = 0.078562 - 0.136872I$	$-3.87464 - 0.10689I$	$-16.3307 + 2.6685I$
$b = 0.660616 + 0.665590I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.181090 - 0.555383I$		
$a = 0.078562 + 0.136872I$	$-3.87464 + 0.10689I$	$-16.3307 - 2.6685I$
$b = 0.660616 - 0.665590I$		
$u = 1.170640 + 0.603687I$		
$a = -0.236393 + 0.423087I$	$-4.12482 + 9.03603I$	$-5.90532 - 6.27658I$
$b = 0.819992 - 0.955539I$		
$u = 1.170640 - 0.603687I$		
$a = -0.236393 - 0.423087I$	$-4.12482 - 9.03603I$	$-5.90532 + 6.27658I$
$b = 0.819992 + 0.955539I$		
$u = -0.175620 + 1.395210I$		
$a = -0.01264 - 1.79079I$	$5.06212 + 3.17952I$	$3.66314 + 2.07098I$
$b = 0.112117 + 0.790036I$		
$u = -0.175620 - 1.395210I$		
$a = -0.01264 + 1.79079I$	$5.06212 - 3.17952I$	$3.66314 - 2.07098I$
$b = 0.112117 - 0.790036I$		
$u = -0.84147 + 1.24514I$		
$a = 0.523153 + 1.313150I$	$-1.69311 + 7.34221I$	$0. - 12.75605I$
$b = 0.716213 - 0.968774I$		
$u = -0.84147 - 1.24514I$		
$a = 0.523153 - 1.313150I$	$-1.69311 - 7.34221I$	$0. + 12.75605I$
$b = 0.716213 + 0.968774I$		
$u = -0.011102 + 0.408161I$		
$a = -2.00560 + 2.80444I$	$0.21083 - 2.02252I$	$-3.27794 + 3.16369I$
$b = -0.549689 - 0.965680I$		
$u = -0.011102 - 0.408161I$		
$a = -2.00560 - 2.80444I$	$0.21083 + 2.02252I$	$-3.27794 - 3.16369I$
$b = -0.549689 + 0.965680I$		
$u = -0.06930 + 1.59935I$		
$a = -0.140568 + 1.053370I$	$4.77684 + 4.89958I$	$0$
$b = 0.280918 - 0.724094I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.06930 - 1.59935I$		
$a = -0.140568 - 1.053370I$	$4.77684 - 4.89958I$	0
$b = 0.280918 + 0.724094I$		
$u = 0.0276533$		
$a = -11.1684$	-2.39902	9.38220
$b = -1.20681$		

$$\text{III. } I_3^u = \langle b + u, 2u^6 - 4u^5 + 7u^4 - 6u^3 + 4u^2 + a - u - 1, u^7 - 2u^6 + 4u^5 - 4u^4 + 4u^3 - 2u^2 + u - 1 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_4 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_1 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_3 &= \begin{pmatrix} u \\ u^3 + u \end{pmatrix} \\ a_8 &= \begin{pmatrix} -2u^6 + 4u^5 - 7u^4 + 6u^3 - 4u^2 + u + 1 \\ -u \end{pmatrix} \\ a_7 &= \begin{pmatrix} -2u^6 + 4u^5 - 7u^4 + 6u^3 - 4u^2 + 1 \\ -u \end{pmatrix} \\ a_5 &= \begin{pmatrix} -2u^5 + 6u^4 - 11u^3 + 13u^2 - 11u + 4 \\ u^6 - 2u^5 + 4u^4 - 4u^3 + 3u^2 - u \end{pmatrix} \\ a_2 &= \begin{pmatrix} u^6 - 3u^5 + 7u^4 - 10u^3 + 10u^2 - 6u + 2 \\ u^6 - 2u^5 + 3u^4 - 2u^3 + 2u^2 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} u^5 - 2u^4 + 4u^3 - 3u^2 + 3u - 1 \\ -u^2 \end{pmatrix} \\ a_9 &= \begin{pmatrix} u^5 - 3u^4 + 5u^3 - 5u^2 + 4u - 2 \\ -u^6 + u^5 - 2u^4 + u^3 - 2u^2 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -u^5 + 2u^4 - 4u^3 + 5u^2 - 5u + 2 \\ u^4 - u^3 + u^2 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -u^5 + 2u^4 - 4u^3 + 5u^2 - 5u + 2 \\ u^4 - u^3 + u^2 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes** =  $-4u^6 - u^5 + 2u^4 - 16u^3 + 11u^2 - 14u - 1$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_6$	$u^7 - u^6 + u^5 - u^4 + 3u^3 - u^2 - 1$
$c_2, c_5$	$u^7 - u^6 + 3u^5 - 5u^4 + 4u^3 - 5u^2 + 5u - 1$
$c_3, c_{10}$	$u^7 + 2u^6 + 4u^5 + 4u^4 + 4u^3 + 2u^2 + u + 1$
$c_4$	$u^7 - 6u^6 + 22u^5 - 53u^4 + 84u^3 - 80u^2 + 42u - 9$
$c_7, c_{11}$	$u^7 - 2u^6 + 4u^5 - 4u^4 + 4u^3 - 2u^2 + u - 1$
$c_8$	$u^7 - 2u^6 + u^5 + 2u^4 - 2u^3 + u^2 + u - 1$
$c_9$	$u^7 - u^6 - u^5 + 2u^4 - 2u^3 - u^2 + 2u - 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_6$	$y^7 + y^6 + 5y^5 + 3y^4 + 5y^3 - 3y^2 - 2y - 1$
$c_2, c_5$	$y^7 + 5y^6 + 7y^5 - y^4 - 6y^3 + 5y^2 + 15y - 1$
$c_3, c_7, c_{10}$ $c_{11}$	$y^7 + 4y^6 + 8y^5 + 10y^4 + 4y^3 - 4y^2 - 3y - 1$
$c_4$	$y^7 + 8y^6 + 16y^5 + 11y^4 + 316y^3 - 298y^2 + 324y - 81$
$c_8$	$y^7 - 2y^6 + 5y^5 - 2y^4 - 2y^3 - y^2 + 3y - 1$
$c_9$	$y^7 - 3y^6 + y^5 + 2y^4 + 2y^3 - 5y^2 + 2y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.820970$		
$a = 0.144523$	-2.80107	-14.6220
$b = -0.820970$		
$u = 0.090842 + 1.238600I$		
$a = -0.38149 + 1.84270I$	6.98186 - 4.35553I	4.40252 + 4.67318I
$b = -0.090842 - 1.238600I$		
$u = 0.090842 - 1.238600I$		
$a = -0.38149 - 1.84270I$	6.98186 + 4.35553I	4.40252 - 4.67318I
$b = -0.090842 + 1.238600I$		
$u = 0.780534 + 1.059930I$		
$a = -0.46249 + 1.46757I$	-1.42367 - 6.15520I	-4.27125 + 4.83482I
$b = -0.780534 - 1.059930I$		
$u = 0.780534 - 1.059930I$		
$a = -0.46249 - 1.46757I$	-1.42367 + 6.15520I	-4.27125 - 4.83482I
$b = -0.780534 + 1.059930I$		
$u = -0.281861 + 0.613464I$		
$a = 3.27172 - 0.15712I$	0.77714 + 4.87266I	-5.32028 - 10.34979I
$b = 0.281861 - 0.613464I$		
$u = -0.281861 - 0.613464I$		
$a = 3.27172 + 0.15712I$	0.77714 - 4.87266I	-5.32028 + 10.34979I
$b = 0.281861 + 0.613464I$		

$$\text{IV. } I_4^u = \langle -u^5 + 2u^4 - 4u^3 + 5u^2 + b - 4u + 2, -u^4 + 2u^3 - 4u^2 + a + 5u - 3, u^6 - 2u^5 + 4u^4 - 5u^3 + 4u^2 - 2u + 1 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_4 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_1 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_3 &= \begin{pmatrix} u \\ u^3 + u \end{pmatrix} \\ a_8 &= \begin{pmatrix} u^4 - 2u^3 + 4u^2 - 5u + 3 \\ u^5 - 2u^4 + 4u^3 - 5u^2 + 4u - 2 \end{pmatrix} \\ a_7 &= \begin{pmatrix} u^5 - u^4 + 2u^3 - u^2 - u + 1 \\ u^5 - 2u^4 + 4u^3 - 5u^2 + 4u - 2 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -u^5 + 2u^4 - 3u^3 + 3u^2 - u - 1 \\ u^5 - u^4 + 2u^3 - u^2 + 1 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -u^5 + u^4 - 2u^3 + u^2 + 2u - 2 \\ u^4 - u^3 + 3u^2 - 3u + 2 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -3u^5 + 6u^4 - 11u^3 + 13u^2 - 8u + 2 \\ 2u^5 - 3u^4 + 6u^3 - 6u^2 + 3u \end{pmatrix} \\ a_9 &= \begin{pmatrix} -2u^5 + 5u^4 - 9u^3 + 11u^2 - 8u + 2 \\ 2u^5 - 4u^4 + 7u^3 - 8u^2 + 4u - 1 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -3u^5 + 6u^4 - 10u^3 + 12u^2 - 7u \\ 2u^5 - 3u^4 + 5u^3 - 5u^2 + 2u + 1 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -3u^5 + 6u^4 - 10u^3 + 12u^2 - 7u \\ 2u^5 - 3u^4 + 5u^3 - 5u^2 + 2u + 1 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes** =  $3u^5 + u^4 - 2u^3 + 6u^2 - 12u + 2$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_6$	$u^6 - 2u^3 + 4u^2 - 3u + 1$
$c_2, c_5$	$u^6 + 3u^5 + 4u^4 + 4u^3 + 3u^2 + u + 1$
$c_3, c_{10}$	$u^6 + 2u^5 + 4u^4 + 5u^3 + 4u^2 + 2u + 1$
$c_4, c_8$	$(u^3 + u^2 - 1)^2$
$c_7, c_{11}$	$u^6 - 2u^5 + 4u^4 - 5u^3 + 4u^2 - 2u + 1$
$c_9$	$(u^3 - u - 1)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_6$	$y^6 + 8y^4 - 2y^3 + 4y^2 - y + 1$
$c_2, c_5$	$y^6 - y^5 - 2y^4 + 4y^3 + 9y^2 + 5y + 1$
$c_3, c_7, c_{10}$ $c_{11}$	$y^6 + 4y^5 + 4y^4 + y^3 + 4y^2 + 4y + 1$
$c_4, c_8$	$(y^3 - y^2 + 2y - 1)^2$
$c_9$	$(y^3 - 2y^2 + y - 1)^2$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.877439 + 0.479689I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.215080 - 0.117582I$	-2.90188	$-8.25352 + 0.I$
$b = -0.877439 + 0.479689I$		
$u = 0.877439 - 0.479689I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.215080 + 0.117582I$	-2.90188	$-8.25352 + 0.I$
$b = -0.877439 - 0.479689I$		
$u = 0.039862 + 0.693124I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 1.22636 - 2.63813I$	4.74081 + 3.77083I	$-0.87324 - 6.91540I$
$b = -0.08270 + 1.43799I$		
$u = 0.039862 - 0.693124I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 1.22636 + 2.63813I$	4.74081 - 3.77083I	$-0.87324 + 6.91540I$
$b = -0.08270 - 1.43799I$		
$u = 0.08270 + 1.43799I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.441444 - 1.330990I$	4.74081 - 3.77083I	$-0.87324 + 6.91540I$
$b = -0.039862 + 0.693124I$		
$u = 0.08270 - 1.43799I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.441444 + 1.330990I$	4.74081 + 3.77083I	$-0.87324 - 6.91540I$
$b = -0.039862 - 0.693124I$		

## V. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_6$	$(u^6 - 2u^3 + 4u^2 - 3u + 1)(u^7 - u^6 + u^5 - u^4 + 3u^3 - u^2 - 1)$ $\cdot (u^{16} - u^{15} + \dots - u + 1)(u^{42} - u^{41} + \dots - 7u - 1)$
$c_2, c_5$	$(u^6 + 3u^5 + 4u^4 + 4u^3 + 3u^2 + u + 1)$ $\cdot (u^7 - u^6 + \dots + 5u - 1)(u^{16} - u^{15} + \dots + 15u^2 + 1)$ $\cdot (u^{42} + 7u^{40} + \dots + 1895u + 457)$
$c_3, c_{10}$	$(u^6 + 2u^5 + 4u^4 + 5u^3 + 4u^2 + 2u + 1)$ $\cdot (u^7 + 2u^6 + \dots + u + 1)(u^{16} + 4u^{14} + \dots + 2u + 1)$ $\cdot (u^{42} + 3u^{41} + \dots + 36u - 1)$
$c_4$	$(u^3 + u^2 - 1)^2(u^7 - 6u^6 + 22u^5 - 53u^4 + 84u^3 - 80u^2 + 42u - 9)$ $\cdot (u^{16} - 13u^{15} + \dots - 352u + 64)(u^{21} + 8u^{20} + \dots + 43u + 7)^2$
$c_7, c_{11}$	$(u^6 - 2u^5 + 4u^4 - 5u^3 + 4u^2 - 2u + 1)$ $\cdot (u^7 - 2u^6 + \dots + u - 1)(u^{16} + 4u^{14} + \dots + 2u + 1)$ $\cdot (u^{42} + 3u^{41} + \dots + 36u - 1)$
$c_8$	$(u^3 + u^2 - 1)^2(u^7 - 2u^6 + u^5 + 2u^4 - 2u^3 + u^2 + u - 1)$ $\cdot (u^{16} - 13u^{15} + \dots - 36u + 8)(u^{21} + 6u^{20} + \dots + 5u + 1)^2$
$c_9$	$(u^3 - u - 1)^2(u^7 - u^6 - u^5 + 2u^4 - 2u^3 - u^2 + 2u - 1)$ $\cdot (u^{16} - 16u^{15} + \dots - 544u + 64)(u^{21} + 6u^{20} + \dots + 9u + 1)^2$

## VI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_6$	$(y^6 + 8y^4 - 2y^3 + 4y^2 - y + 1)(y^7 + y^6 + \dots - 2y - 1)$ $\cdot (y^{16} - 3y^{15} + \dots - 5y + 1)(y^{42} - y^{41} + \dots - 45y + 1)$
$c_2, c_5$	$(y^6 - y^5 - 2y^4 + 4y^3 + 9y^2 + 5y + 1)$ $\cdot (y^7 + 5y^6 + \dots + 15y - 1)(y^{16} + 9y^{15} + \dots + 30y + 1)$ $\cdot (y^{42} + 14y^{41} + \dots + 2544657y + 208849)$
$c_3, c_7, c_{10}$ $c_{11}$	$(y^6 + 4y^5 + 4y^4 + y^3 + 4y^2 + 4y + 1)$ $\cdot (y^7 + 4y^6 + 8y^5 + 10y^4 + 4y^3 - 4y^2 - 3y - 1)$ $\cdot (y^{16} + 8y^{15} + \dots + 12y + 1)(y^{42} + 11y^{41} + \dots - 1288y + 1)$
$c_4$	$(y^3 - y^2 + 2y - 1)^2$ $\cdot (y^7 + 8y^6 + 16y^5 + 11y^4 + 316y^3 - 298y^2 + 324y - 81)$ $\cdot (y^{16} + 5y^{15} + \dots + 40448y + 4096)$ $\cdot (y^{21} - 10y^{20} + \dots + 1149y - 49)^2$
$c_8$	$(y^3 - y^2 + 2y - 1)^2(y^7 - 2y^6 + 5y^5 - 2y^4 - 2y^3 - y^2 + 3y - 1)$ $\cdot (y^{16} - y^{15} + \dots + 496y + 64)(y^{21} + 2y^{20} + \dots - 11y - 1)^2$
$c_9$	$(y^3 - 2y^2 + y - 1)^2(y^7 - 3y^6 + y^5 + 2y^4 + 2y^3 - 5y^2 + 2y - 1)$ $\cdot (y^{16} - 4y^{15} + \dots + 23552y + 4096)(y^{21} - 8y^{20} + \dots + 33y - 1)^2$