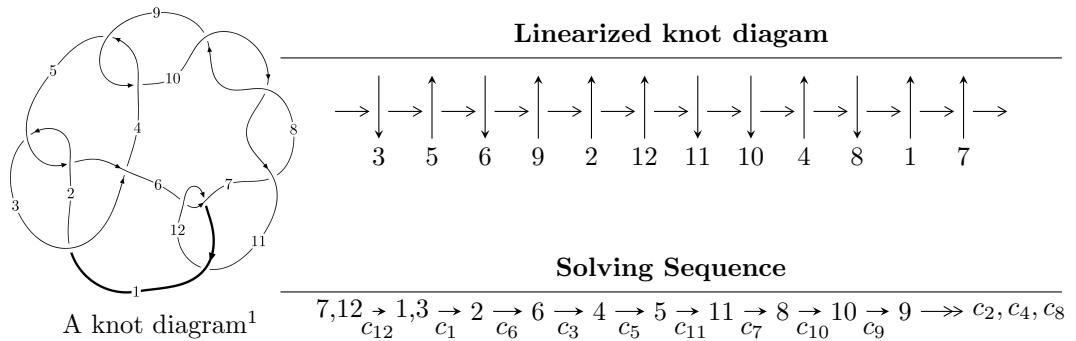


$12a_{0032}$  ( $K12a_{0032}$ )



Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$

$$I_1^u = \langle 4u^{72} + 9u^{71} + \dots + b - 5, 3u^{72} + 6u^{71} + \dots + 2a - 5, u^{73} + 3u^{72} + \dots - 4u - 1 \rangle$$

$$I_2^u = \langle b, a^2 - a + 1, u - 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 75 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I_1^u = \langle 4u^{72} + 9u^{71} + \dots + b - 5, 3u^{72} + 6u^{71} + \dots + 2a - 5, u^{73} + 3u^{72} + \dots - 4u - 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_7 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_1 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -\frac{3}{2}u^{72} - 3u^{71} + \dots + \frac{9}{2}u + \frac{5}{2} \\ -4u^{72} - 9u^{71} + \dots + 14u + 5 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -\frac{1}{2}u^{72} - u^{71} + \dots - \frac{3}{2}u + \frac{1}{2} \\ u^{29} - 9u^{27} + \dots + 2u^2 + u \end{pmatrix} \\ a_6 &= \begin{pmatrix} -u \\ u \end{pmatrix} \\ a_4 &= \begin{pmatrix} 2u^{72} + 5u^{71} + \dots - 8u - 2 \\ -\frac{15}{2}u^{72} - 17u^{71} + \dots + \frac{53}{2}u + \frac{19}{2} \end{pmatrix} \\ a_5 &= \begin{pmatrix} 5u^{72} + 11u^{71} + \dots - 18u - 6 \\ \frac{3}{2}u^{72} + 3u^{71} + \dots - \frac{7}{2}u - \frac{3}{2} \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -u^2 + 1 \\ u^4 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -u^5 + 2u^3 - u \\ u^7 - u^5 + u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -u^8 + 3u^6 - 3u^4 + 1 \\ u^{10} - 2u^8 + u^6 + 2u^4 - u^2 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -u^{11} + 4u^9 - 6u^7 + 2u^5 + 3u^3 - 2u \\ u^{13} - 3u^{11} + 3u^9 + 2u^7 - 4u^5 + u^3 + u \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-18u^{72} - 43u^{71} + \dots + 66u + 25$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{73} + 32u^{72} + \cdots + 11u - 1$
$c_2, c_5$	$u^{73} + 2u^{72} + \cdots - u - 1$
$c_3$	$u^{73} - 2u^{72} + \cdots + 165u - 17$
$c_4, c_9$	$u^{73} + u^{72} + \cdots + 4u - 4$
$c_6, c_{12}$	$u^{73} + 3u^{72} + \cdots - 4u - 1$
$c_7, c_8, c_{10}$	$u^{73} + 15u^{72} + \cdots - 216u - 16$
$c_{11}$	$u^{73} - 43u^{72} + \cdots - 2u - 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{73} + 20y^{72} + \cdots + 275y - 1$
$c_2, c_5$	$y^{73} + 32y^{72} + \cdots + 11y - 1$
$c_3$	$y^{73} + 8y^{72} + \cdots - 6877y - 289$
$c_4, c_9$	$y^{73} + 15y^{72} + \cdots - 216y - 16$
$c_6, c_{12}$	$y^{73} - 43y^{72} + \cdots - 2y - 1$
$c_7, c_8, c_{10}$	$y^{73} + 83y^{72} + \cdots + 4384y - 256$
$c_{11}$	$y^{73} - 23y^{72} + \cdots + 38y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.796832 + 0.538347I$		
$a = -2.31129 + 0.06801I$	$-4.24142 - 5.70697I$	0
$b = 1.70540 - 1.05275I$		
$u = -0.796832 - 0.538347I$		
$a = -2.31129 - 0.06801I$	$-4.24142 + 5.70697I$	0
$b = 1.70540 + 1.05275I$		
$u = 0.899085 + 0.326015I$		
$a = 0.02535 - 2.32970I$	$0.082824 + 0.160201I$	0
$b = -0.58316 + 2.15466I$		
$u = 0.899085 - 0.326015I$		
$a = 0.02535 + 2.32970I$	$0.082824 - 0.160201I$	0
$b = -0.58316 - 2.15466I$		
$u = -1.030080 + 0.324784I$		
$a = 0.645259 - 0.737289I$	$2.50971 + 0.29837I$	0
$b = 0.428910 - 0.037104I$		
$u = -1.030080 - 0.324784I$		
$a = 0.645259 + 0.737289I$	$2.50971 - 0.29837I$	0
$b = 0.428910 + 0.037104I$		
$u = -0.060471 + 0.908501I$		
$a = -1.143350 + 0.045300I$	$6.24864 + 10.27490I$	$2.89542 - 7.01845I$
$b = -0.15329 - 1.46139I$		
$u = -0.060471 - 0.908501I$		
$a = -1.143350 - 0.045300I$	$6.24864 - 10.27490I$	$2.89542 + 7.01845I$
$b = -0.15329 + 1.46139I$		
$u = -0.045023 + 0.902001I$		
$a = 1.048390 - 0.026697I$	$8.09212 + 4.88858I$	$5.55498 - 2.56495I$
$b = 0.425897 + 0.828457I$		
$u = -0.045023 - 0.902001I$		
$a = 1.048390 + 0.026697I$	$8.09212 - 4.88858I$	$5.55498 + 2.56495I$
$b = 0.425897 - 0.828457I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.027830 + 0.411352I$		
$a = -2.75340 - 1.31041I$	$1.86319 + 6.29573I$	0
$b = 2.13202 + 2.36044I$		
$u = 1.027830 - 0.411352I$		
$a = -2.75340 + 1.31041I$	$1.86319 - 6.29573I$	0
$b = 2.13202 - 2.36044I$		
$u = -0.992153 + 0.494153I$		
$a = -0.13867 + 1.47620I$	$-2.09315 - 4.25967I$	0
$b = -0.25797 - 1.67319I$		
$u = -0.992153 - 0.494153I$		
$a = -0.13867 - 1.47620I$	$-2.09315 + 4.25967I$	0
$b = -0.25797 + 1.67319I$		
$u = -0.003685 + 0.885221I$		
$a = 1.061200 + 0.001583I$	$8.26656 + 1.57314I$	$5.85573 - 2.28832I$
$b = 0.448605 - 0.796552I$		
$u = -0.003685 - 0.885221I$		
$a = 1.061200 - 0.001583I$	$8.26656 - 1.57314I$	$5.85573 + 2.28832I$
$b = 0.448605 + 0.796552I$		
$u = 1.061310 + 0.358999I$		
$a = 1.73187 + 0.46057I$	$3.61712 + 1.77427I$	0
$b = -1.55065 - 1.27425I$		
$u = 1.061310 - 0.358999I$		
$a = 1.73187 - 0.46057I$	$3.61712 - 1.77427I$	0
$b = -1.55065 + 1.27425I$		
$u = -1.055210 + 0.377398I$		
$a = 0.143235 + 0.585101I$	$3.48602 - 4.64873I$	0
$b = -0.653103 + 0.376649I$		
$u = -1.055210 - 0.377398I$		
$a = 0.143235 - 0.585101I$	$3.48602 + 4.64873I$	0
$b = -0.653103 - 0.376649I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.014910 + 0.877594I$		
$a = -1.170160 + 0.036770I$	$6.56651 - 3.81304I$	$3.48761 + 2.37237I$
$b = -0.15465 + 1.42320I$		
$u = 0.014910 - 0.877594I$		
$a = -1.170160 - 0.036770I$	$6.56651 + 3.81304I$	$3.48761 - 2.37237I$
$b = -0.15465 - 1.42320I$		
$u = -0.745666 + 0.449141I$		
$a = 1.241710 - 0.206618I$	$-1.60556 - 1.91846I$	$-0.83992 + 4.54593I$
$b = -0.615729 + 0.808004I$		
$u = -0.745666 - 0.449141I$		
$a = 1.241710 + 0.206618I$	$-1.60556 + 1.91846I$	$-0.83992 - 4.54593I$
$b = -0.615729 - 0.808004I$		
$u = -0.663356 + 0.548451I$		
$a = -1.09116 + 1.48131I$	$-4.60806 + 1.34225I$	$-6.07081 - 0.60893I$
$b = 0.05851 - 1.82675I$		
$u = -0.663356 - 0.548451I$		
$a = -1.09116 - 1.48131I$	$-4.60806 - 1.34225I$	$-6.07081 + 0.60893I$
$b = 0.05851 + 1.82675I$		
$u = -0.044946 + 0.858380I$		
$a = -0.926262 - 0.036801I$	$2.49214 + 3.07068I$	$-0.36042 - 2.48054I$
$b = 0.583114 - 0.035791I$		
$u = -0.044946 - 0.858380I$		
$a = -0.926262 + 0.036801I$	$2.49214 - 3.07068I$	$-0.36042 + 2.48054I$
$b = 0.583114 + 0.035791I$		
$u = 1.148100 + 0.066282I$		
$a = 0.481281 - 0.828556I$	$0.94991 + 1.54341I$	0
$b = -0.072635 + 0.333417I$		
$u = 1.148100 - 0.066282I$		
$a = 0.481281 + 0.828556I$	$0.94991 - 1.54341I$	0
$b = -0.072635 - 0.333417I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.831297$		
$a = 1.18611$	1.20245	8.84780
$b = -0.878157$		
$u = -1.067090 + 0.480663I$		
$a = 1.43081 - 0.55418I$	2.23047 - 6.58216I	0
$b = -1.10301 + 1.47768I$		
$u = -1.067090 - 0.480663I$		
$a = 1.43081 + 0.55418I$	2.23047 + 6.58216I	0
$b = -1.10301 - 1.47768I$		
$u = 1.143120 + 0.264741I$		
$a = 0.321926 - 0.475229I$	3.87826 + 0.47986I	0
$b = -0.765191 - 0.174011I$		
$u = 1.143120 - 0.264741I$		
$a = 0.321926 + 0.475229I$	3.87826 - 0.47986I	0
$b = -0.765191 + 0.174011I$		
$u = -1.072090 + 0.517956I$		
$a = -2.16667 + 1.15750I$	0.09169 - 11.38030I	0
$b = 1.50805 - 2.21750I$		
$u = -1.072090 - 0.517956I$		
$a = -2.16667 - 1.15750I$	0.09169 + 11.38030I	0
$b = 1.50805 + 2.21750I$		
$u = 1.189960 + 0.217721I$		
$a = 0.538138 + 0.733544I$	2.38629 - 3.99102I	0
$b = 0.386122 - 0.182674I$		
$u = 1.189960 - 0.217721I$		
$a = 0.538138 - 0.733544I$	2.38629 + 3.99102I	0
$b = 0.386122 + 0.182674I$		
$u = -0.759472 + 0.078072I$		
$a = 0.409671 + 1.121040I$	0.90189 - 2.32067I	-2.23029 + 5.61700I
$b = -0.025028 + 0.368371I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.759472 - 0.078072I$		
$a = 0.409671 - 1.121040I$	$0.90189 + 2.32067I$	$-2.23029 - 5.61700I$
$b = -0.025028 - 0.368371I$		
$u = -0.294691 + 0.697762I$		
$a = -1.52227 + 0.52821I$	$-2.13058 + 6.78357I$	$-1.78763 - 7.49032I$
$b = 0.04655 - 1.54343I$		
$u = -0.294691 - 0.697762I$		
$a = -1.52227 - 0.52821I$	$-2.13058 - 6.78357I$	$-1.78763 + 7.49032I$
$b = 0.04655 + 1.54343I$		
$u = -0.411090 + 0.594862I$		
$a = -1.33198 - 0.64422I$	$-3.71919 - 0.03530I$	$-5.73582 - 0.13433I$
$b = 1.058470 - 0.183219I$		
$u = -0.411090 - 0.594862I$		
$a = -1.33198 + 0.64422I$	$-3.71919 + 0.03530I$	$-5.73582 + 0.13433I$
$b = 1.058470 + 0.183219I$		
$u = 0.638508 + 0.276958I$		
$a = -2.85677 + 1.41704I$	$-0.67209 + 2.83977I$	$0.57232 - 5.77641I$
$b = 2.23207 - 0.27893I$		
$u = 0.638508 - 0.276958I$		
$a = -2.85677 - 1.41704I$	$-0.67209 - 2.83977I$	$0.57232 + 5.77641I$
$b = 2.23207 + 0.27893I$		
$u = 1.245740 + 0.440942I$		
$a = 0.151191 - 1.053990I$	$6.38924 + 1.49871I$	0
$b = -0.087474 + 1.281280I$		
$u = 1.245740 - 0.440942I$		
$a = 0.151191 + 1.053990I$	$6.38924 - 1.49871I$	0
$b = -0.087474 - 1.281280I$		
$u = -1.237210 + 0.485257I$		
$a = 0.092149 + 1.060120I$	$6.06816 - 7.90409I$	0
$b = -0.069199 - 1.349010I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.237210 - 0.485257I$		
$a = 0.092149 - 1.060120I$	$6.06816 + 7.90409I$	0
$b = -0.069199 + 1.349010I$		
$u = -0.247172 + 0.623477I$		
$a = 1.109370 - 0.156214I$	$-0.05164 + 2.31958I$	$1.90774 - 3.63180I$
$b = 0.146837 + 0.686540I$		
$u = -0.247172 - 0.623477I$		
$a = 1.109370 + 0.156214I$	$-0.05164 - 2.31958I$	$1.90774 + 3.63180I$
$b = 0.146837 - 0.686540I$		
$u = -1.254650 + 0.458550I$		
$a = 0.571192 - 0.618053I$	$10.41650 - 0.92595I$	0
$b = 0.654999 + 0.111159I$		
$u = -1.254650 - 0.458550I$		
$a = 0.571192 + 0.618053I$	$10.41650 + 0.92595I$	0
$b = 0.654999 - 0.111159I$		
$u = 1.250410 + 0.474243I$		
$a = -1.64704 - 1.66951I$	$10.30140 + 8.63802I$	0
$b = 0.99899 + 2.81058I$		
$u = 1.250410 - 0.474243I$		
$a = -1.64704 + 1.66951I$	$10.30140 - 8.63802I$	0
$b = 0.99899 - 2.81058I$		
$u = 1.257260 + 0.465604I$		
$a = 1.34060 + 0.93797I$	$12.09550 + 3.22867I$	0
$b = -1.14852 - 2.06285I$		
$u = 1.257260 - 0.465604I$		
$a = 1.34060 - 0.93797I$	$12.09550 - 3.22867I$	0
$b = -1.14852 + 2.06285I$		
$u = -1.256050 + 0.469575I$		
$a = 0.076133 + 0.366803I$	$12.06620 - 6.39600I$	0
$b = -0.925574 + 0.435365I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.256050 - 0.469575I$		
$a = 0.076133 - 0.366803I$	$12.06620 + 6.39600I$	0
$b = -0.925574 - 0.435365I$		
$u = 1.273530 + 0.443626I$		
$a = 0.096224 - 0.351788I$	$12.14430 - 0.14495I$	0
$b = -0.940708 - 0.404721I$		
$u = 1.273530 - 0.443626I$		
$a = 0.096224 + 0.351788I$	$12.14430 + 0.14495I$	0
$b = -0.940708 + 0.404721I$		
$u = -1.256320 + 0.493887I$		
$a = 1.29631 - 0.89917I$	$11.7702 - 9.8863I$	0
$b = -1.07374 + 2.03687I$		
$u = -1.256320 - 0.493887I$		
$a = 1.29631 + 0.89917I$	$11.7702 + 9.8863I$	0
$b = -1.07374 - 2.03687I$		
$u = 1.279930 + 0.434233I$		
$a = 0.556079 + 0.623274I$	$10.39010 - 5.55528I$	0
$b = 0.648052 - 0.146041I$		
$u = 1.279930 - 0.434233I$		
$a = 0.556079 - 0.623274I$	$10.39010 + 5.55528I$	0
$b = 0.648052 + 0.146041I$		
$u = -1.255820 + 0.502698I$		
$a = -1.60562 + 1.57330I$	$9.8802 - 15.3350I$	0
$b = 0.94296 - 2.71614I$		
$u = -1.255820 - 0.502698I$		
$a = -1.60562 - 1.57330I$	$9.8802 + 15.3350I$	0
$b = 0.94296 + 2.71614I$		
$u = -0.014084 + 0.462153I$		
$a = 1.42124 + 0.30256I$	$0.89929 + 1.38203I$	$4.27247 - 4.11780I$
$b = 0.409463 - 0.530113I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.014084 - 0.462153I$		
$a = 1.42124 - 0.30256I$	$0.89929 - 1.38203I$	$4.27247 + 4.11780I$
$b = 0.409463 + 0.530113I$		
$u = 0.217836 + 0.395971I$		
$a = -2.71775 - 0.62754I$	$-0.21204 - 2.78157I$	$2.07158 + 2.47908I$
$b = 0.30369 + 1.39444I$		
$u = 0.217836 - 0.395971I$		
$a = -2.71775 + 0.62754I$	$-0.21204 + 2.78157I$	$2.07158 - 2.47908I$
$b = 0.30369 - 1.39444I$		

$$\text{II. } I_2^u = \langle b, a^2 - a + 1, u - 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} a \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ a \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ a \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $4a + 7$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_5$	$u^2 - u + 1$
$c_2$	$u^2 + u + 1$
$c_4, c_7, c_8$ $c_9, c_{10}$	$u^2$
$c_6, c_{11}$	$(u + 1)^2$
$c_{12}$	$(u - 1)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_5$	$y^2 + y + 1$
$c_4, c_7, c_8$ $c_9, c_{10}$	$y^2$
$c_6, c_{11}, c_{12}$	$(y - 1)^2$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$		
$a = 0.500000 + 0.866025I$	$1.64493 - 2.02988I$	$9.00000 + 3.46410I$
$b = 0$		
$u = 1.00000$		
$a = 0.500000 - 0.866025I$	$1.64493 + 2.02988I$	$9.00000 - 3.46410I$
$b = 0$		

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u^2 - u + 1)(u^{73} + 32u^{72} + \dots + 11u - 1)$
$c_2$	$(u^2 + u + 1)(u^{73} + 2u^{72} + \dots - u - 1)$
$c_3$	$(u^2 - u + 1)(u^{73} - 2u^{72} + \dots + 165u - 17)$
$c_4, c_9$	$u^2(u^{73} + u^{72} + \dots + 4u - 4)$
$c_5$	$(u^2 - u + 1)(u^{73} + 2u^{72} + \dots - u - 1)$
$c_6$	$((u + 1)^2)(u^{73} + 3u^{72} + \dots - 4u - 1)$
$c_7, c_8, c_{10}$	$u^2(u^{73} + 15u^{72} + \dots - 216u - 16)$
$c_{11}$	$((u + 1)^2)(u^{73} - 43u^{72} + \dots - 2u - 1)$
$c_{12}$	$((u - 1)^2)(u^{73} + 3u^{72} + \dots - 4u - 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^2 + y + 1)(y^{73} + 20y^{72} + \dots + 275y - 1)$
$c_2, c_5$	$(y^2 + y + 1)(y^{73} + 32y^{72} + \dots + 11y - 1)$
$c_3$	$(y^2 + y + 1)(y^{73} + 8y^{72} + \dots - 6877y - 289)$
$c_4, c_9$	$y^2(y^{73} + 15y^{72} + \dots - 216y - 16)$
$c_6, c_{12}$	$((y - 1)^2)(y^{73} - 43y^{72} + \dots - 2y - 1)$
$c_7, c_8, c_{10}$	$y^2(y^{73} + 83y^{72} + \dots + 4384y - 256)$
$c_{11}$	$((y - 1)^2)(y^{73} - 23y^{72} + \dots + 38y - 1)$