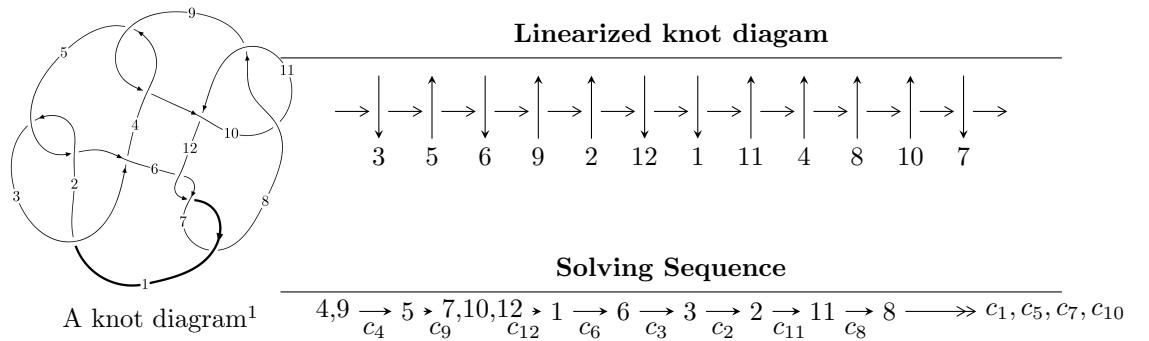


$12a_{0033}$  ( $K12a_{0033}$ )



Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

$$\begin{aligned}
I_1^u &= \langle 4.19179 \times 10^{162} u^{76} - 8.99312 \times 10^{162} u^{75} + \dots + 5.13128 \times 10^{164} d + 1.74805 \times 10^{165}, \\
&\quad 5.20225 \times 10^{162} u^{76} - 1.09357 \times 10^{163} u^{75} + \dots + 5.13128 \times 10^{164} c + 2.30253 \times 10^{165}, \\
&\quad 5.03182 \times 10^{182} u^{76} - 1.22724 \times 10^{183} u^{75} + \dots + 1.08760 \times 10^{185} b + 3.35895 \times 10^{185}, \\
&\quad - 3.61857 \times 10^{182} u^{76} + 6.18392 \times 10^{182} u^{75} + \dots + 5.43799 \times 10^{184} a - 1.83798 \times 10^{184}, \\
&\quad u^{77} - 2u^{76} + \dots - 2560u^2 - 512 \rangle, \\
I_2^u &= \langle -43u^3a^2 - 6a^2u^2 - 37u^3a - 62a^2u - 58u^2a + 38u^3 + 36a^2 - 55au + 2u^2 + 71d - 78a - 74u - 12, \\
&\quad - 47u^3a^2 + 5a^2u^2 - 52u^3a - 43a^2u - 70u^2a - 8u^3 + 41a^2 - 37au + 22u^2 + 71c - 6a - 104u + 10, \\
&\quad - 24u^3a^2 - 5a^2u^2 - 19u^3a - 28a^2u - u^2a + 8u^3 + 30a^2 - 34au - 22u^2 + 71b - 65a - 38u - 10, \\
&\quad - 2u^3a^2 - u^3a + a^3 - 2a^2u - 5u^2a - u^3 + 2a^2 - au + u^2 - u, u^4 + u^2 - u + 1 \rangle \\
I_3^u &= \langle -75u^5a^2 + 125u^5a + \dots - 31a + 44, -55u^5a^2 + 167u^5a + \dots + 143a - 28, \\
&\quad - 58u^5a^2 + 59u^5a + \dots - 30a + 28, \\
&\quad - 2u^5a^2 - 2u^4a^2 + 2u^5a - 4u^3a^2 + u^4a + u^5 - 4a^2u^2 + 3u^3a + a^3 - 4a^2u - 2u^2a - 4a^2 + 2au + 2a, \\
&\quad u^6 + u^5 + 2u^4 + 2u^3 + 2u^2 + 2u + 1 \rangle \\
I_1^v &= \langle a, d - v + 1, c + a, b + v - 1, v^2 - v + 1 \rangle \\
I_2^v &= \langle a, d, c - v, b - v - 1, v^2 + v + 1 \rangle \\
I_3^v &= \langle a, d + 1, c + a - 1, b - 1, v - 1 \rangle \\
I_4^v &= \langle a, -b^2v - bv + d + 2b - v + 1, -b^2av - bav + cb + 2ba - av + a - 1, \\
&\quad v^2c - bav + v^2b - cv - av + v^2 + c + 2a - 2v, b^2v^2 + v^2b - 2bv + v^2 - v + 1 \rangle
\end{aligned}$$

\* 6 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 112 representations.

\* 1 irreducible components of  $\dim_{\mathbb{C}} = 1$

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<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle 4.19 \times 10^{162} u^{76} - 8.99 \times 10^{162} u^{75} + \dots + 5.13 \times 10^{164} d + 1.75 \times 10^{165}, 5.20 \times 10^{162} u^{76} - 1.09 \times 10^{163} u^{75} + \dots + 5.13 \times 10^{164} c + 2.30 \times 10^{165}, 5.03 \times 10^{182} u^{76} - 1.23 \times 10^{183} u^{75} + \dots + 1.09 \times 10^{185} b + 3.36 \times 10^{185}, -3.62 \times 10^{182} u^{76} + 6.18 \times 10^{182} u^{75} + \dots + 5.44 \times 10^{184} a - 1.84 \times 10^{184}, u^{77} - 2u^{76} + \dots - 2560u^2 - 512 \rangle$$

(i) **Arc colorings**

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.00665423u^{76} - 0.0113717u^{75} + \dots - 8.65830u + 0.337989 \\ -0.00462654u^{76} + 0.0112840u^{75} + \dots + 6.23600u - 3.08841 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -0.0101383u^{76} + 0.0213118u^{75} + \dots + 12.1450u - 4.48724 \\ -0.00816908u^{76} + 0.0175261u^{75} + \dots + 11.0464u - 3.40665 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.0125394u^{76} + 0.0245545u^{75} + \dots + 16.0108u - 3.02234 \\ -0.00622485u^{76} + 0.0135037u^{75} + \dots + 7.88286u - 2.23172 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0.0108390u^{76} - 0.0188168u^{75} + \dots - 14.5481u + 0.522142 \\ -0.00170046u^{76} + 0.00573767u^{75} + \dots + 1.46268u - 2.50020 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -0.00903125u^{76} + 0.0210962u^{75} + \dots + 7.69784u - 4.39652 \\ -0.00575546u^{76} + 0.0105565u^{75} + \dots + 7.63073u + 1.82138 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.00761038u^{76} + 0.0196600u^{75} + \dots + 4.69111u - 7.77114 \\ -0.00621954u^{76} + 0.0118805u^{75} + \dots + 6.90325u + 1.10173 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.00891820u^{76} + 0.0191719u^{75} + \dots + 11.1367u - 4.56543 \\ -0.00694897u^{76} + 0.0153862u^{75} + \dots + 10.0381u - 3.48484 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0.00196923u^{76} - 0.00378574u^{75} + \dots - 1.09859u + 1.08059 \\ -0.00694897u^{76} + 0.0153862u^{75} + \dots + 10.0381u - 3.48484 \end{pmatrix}$$

(ii) **Obstruction class = -1**

(iii) **Cusp Shapes** =  $0.0221138u^{76} - 0.0478032u^{75} + \dots - 21.6023u - 0.388088$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{77} + 36u^{76} + \cdots + 216u - 16$
$c_2, c_5$	$u^{77} + 2u^{76} + \cdots + 27u^2 - 4$
$c_3$	$u^{77} - 2u^{76} + \cdots + 351912u - 66564$
$c_4, c_9$	$u^{77} - 2u^{76} + \cdots - 2560u^2 - 512$
$c_6, c_7, c_{12}$	$u^{77} - 8u^{76} + \cdots - 72u - 16$
$c_8, c_{10}$	$u^{77} + 8u^{76} + \cdots - 72u - 16$
$c_{11}$	$u^{77} - 34u^{76} + \cdots + 1568u - 256$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{77} + 12y^{76} + \cdots + 84256y - 256$
$c_2, c_5$	$y^{77} + 36y^{76} + \cdots + 216y - 16$
$c_3$	$y^{77} - 12y^{76} + \cdots + 120020616504y - 4430766096$
$c_4, c_9$	$y^{77} + 30y^{76} + \cdots - 2621440y - 262144$
$c_6, c_7, c_{12}$	$y^{77} - 74y^{76} + \cdots + 7712y - 256$
$c_8, c_{10}$	$y^{77} - 34y^{76} + \cdots + 1568y - 256$
$c_{11}$	$y^{77} + 26y^{76} + \cdots + 3416576y - 65536$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.508886 + 0.845592I$ $a = 1.118510 + 0.861761I$ $b = 0.504405 - 0.239677I$ $c = -0.82230 - 2.15378I$ $d = -1.077350 - 0.552668I$	$2.40889 + 4.27390I$	$3.74115 - 6.44221I$
$u = 0.508886 - 0.845592I$ $a = 1.118510 - 0.861761I$ $b = 0.504405 + 0.239677I$ $c = -0.82230 + 2.15378I$ $d = -1.077350 + 0.552668I$	$2.40889 - 4.27390I$	$3.74115 + 6.44221I$
$u = -0.848496 + 0.585068I$ $a = -0.008580 + 0.439129I$ $b = 0.103075 - 0.222508I$ $c = 0.749137 - 0.747672I$ $d = 1.049330 + 0.534087I$	$3.78378 + 2.11500I$	$7.65464 - 1.99007I$
$u = -0.848496 - 0.585068I$ $a = -0.008580 - 0.439129I$ $b = 0.103075 + 0.222508I$ $c = 0.749137 + 0.747672I$ $d = 1.049330 - 0.534087I$	$3.78378 - 2.11500I$	$7.65464 + 1.99007I$
$u = -0.990280 + 0.319237I$ $a = -1.79246 + 0.10308I$ $b = -0.675932 - 1.005350I$ $c = -1.016130 + 0.043329I$ $d = -1.111790 - 0.533215I$	$-2.98745 + 0.86657I$	0
$u = -0.990280 - 0.319237I$ $a = -1.79246 - 0.10308I$ $b = -0.675932 + 1.005350I$ $c = -1.016130 - 0.043329I$ $d = -1.111790 + 0.533215I$	$-2.98745 - 0.86657I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.617221 + 0.733532I$ $a = -0.619707 + 0.764557I$ $b = -0.277695 - 0.242708I$ $c = 0.75499 - 1.66880I$ $d = 1.079400 - 0.162408I$	$4.09446 + 0.35704I$	$8.04104 + 0.70386I$
$u = -0.617221 - 0.733532I$ $a = -0.619707 - 0.764557I$ $b = -0.277695 + 0.242708I$ $c = 0.75499 + 1.66880I$ $d = 1.079400 + 0.162408I$	$4.09446 - 0.35704I$	$8.04104 - 0.70386I$
$u = 0.517431 + 0.792256I$ $a = -0.602670 + 0.058164I$ $b = -1.312620 + 0.060155I$ $c = -0.799858 - 0.461927I$ $d = -2.05780 - 0.08517I$	$2.57405 - 0.08416I$	$4.54592 - 2.74373I$
$u = 0.517431 - 0.792256I$ $a = -0.602670 - 0.058164I$ $b = -1.312620 - 0.060155I$ $c = -0.799858 + 0.461927I$ $d = -2.05780 + 0.08517I$	$2.57405 + 0.08416I$	$4.54592 + 2.74373I$
$u = -0.082487 + 0.936352I$ $a = -0.948613 + 0.464331I$ $b = -0.836303 + 0.719975I$ $c = 0.066226 + 0.663106I$ $d = -0.575224 + 0.771574I$	$-1.72016 + 1.41215I$	$-1.65188 - 3.77223I$
$u = -0.082487 - 0.936352I$ $a = -0.948613 - 0.464331I$ $b = -0.836303 - 0.719975I$ $c = 0.066226 - 0.663106I$ $d = -0.575224 - 0.771574I$	$-1.72016 - 1.41215I$	$-1.65188 + 3.77223I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.582500 + 0.889546I$		
$a = 0.372525 + 0.042062I$		
$b = 0.984114 - 0.079699I$	$3.62010 - 5.07823I$	$6.10660 + 7.37918I$
$c = 0.620752 - 0.807952I$		
$d = 1.88365 - 0.53487I$		
$u = -0.582500 - 0.889546I$		
$a = 0.372525 - 0.042062I$		
$b = 0.984114 + 0.079699I$	$3.62010 + 5.07823I$	$6.10660 - 7.37918I$
$c = 0.620752 + 0.807952I$		
$d = 1.88365 + 0.53487I$		
$u = 0.228301 + 1.040040I$		
$a = -0.13810 - 1.60777I$		
$b = -1.48108 - 2.66829I$	$-3.92825 - 1.69884I$	$-4.65730 + 2.32962I$
$c = -0.126234 + 0.944655I$		
$d = 0.516753 + 0.893507I$		
$u = 0.228301 - 1.040040I$		
$a = -0.13810 + 1.60777I$		
$b = -1.48108 + 2.66829I$	$-3.92825 + 1.69884I$	$-4.65730 - 2.32962I$
$c = -0.126234 - 0.944655I$		
$d = 0.516753 - 0.893507I$		
$u = 0.782003 + 0.468875I$		
$a = -2.36435 - 2.24948I$		
$b = -1.06894 + 1.62874I$	$0.65497 - 3.51390I$	$3.54011 + 4.44478I$
$c = -0.310023 - 0.749893I$		
$d = -0.722438 + 0.469371I$		
$u = 0.782003 - 0.468875I$		
$a = -2.36435 + 2.24948I$		
$b = -1.06894 - 1.62874I$	$0.65497 + 3.51390I$	$3.54011 - 4.44478I$
$c = -0.310023 + 0.749893I$		
$d = -0.722438 - 0.469371I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.374962 + 1.039940I$ $a = 0.00241 - 1.81691I$ $b = 1.04564 - 2.79506I$ $c = -0.054535 + 1.153860I$ $d = -0.648190 + 1.006590I$	$-3.38837 - 3.78470I$	0
$u = -0.374962 - 1.039940I$ $a = 0.00241 + 1.81691I$ $b = 1.04564 + 2.79506I$ $c = -0.054535 - 1.153860I$ $d = -0.648190 - 1.006590I$	$-3.38837 + 3.78470I$	0
$u = 0.965284 + 0.548957I$ $a = -0.183189 + 0.297060I$ $b = -0.297598 - 0.221943I$ $c = -0.820096 - 0.337678I$ $d = -1.051710 + 0.877929I$	$1.81197 - 6.85619I$	0
$u = 0.965284 - 0.548957I$ $a = -0.183189 - 0.297060I$ $b = -0.297598 + 0.221943I$ $c = -0.820096 + 0.337678I$ $d = -1.051710 - 0.877929I$	$1.81197 + 6.85619I$	0
$u = 0.288832 + 1.092220I$ $a = 1.30645 + 0.68041I$ $b = 1.045540 + 0.686079I$ $c = -0.140070 + 1.099610I$ $d = 0.513316 + 0.990185I$	$-4.40655 + 2.61636I$	0
$u = 0.288832 - 1.092220I$ $a = 1.30645 - 0.68041I$ $b = 1.045540 - 0.686079I$ $c = -0.140070 - 1.099610I$ $d = 0.513316 - 0.990185I$	$-4.40655 - 2.61636I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.815552 + 0.276755I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.393181 + 0.675339I$		
$b = -0.097483 + 0.217571I$	$-0.065597 - 0.205341I$	$1.21551 + 1.86968I$
$c = 0.125990 - 0.372709I$		
$d = -0.310498 + 0.604570I$		
$u = 0.815552 - 0.276755I$		
$a = -0.393181 - 0.675339I$		
$b = -0.097483 - 0.217571I$	$-0.065597 + 0.205341I$	$1.21551 - 1.86968I$
$c = 0.125990 + 0.372709I$		
$d = -0.310498 - 0.604570I$		
$u = -0.008067 + 1.164640I$		
$a = 0.831879 + 0.802027I$		
$b = 0.838657 + 0.822115I$	$-4.97078 - 4.99360I$	0
$c = -0.537680 + 0.563389I$		
$d = 0.297322 + 0.581051I$		
$u = -0.008067 - 1.164640I$		
$a = 0.831879 - 0.802027I$		
$b = 0.838657 - 0.822115I$	$-4.97078 + 4.99360I$	0
$c = -0.537680 - 0.563389I$		
$d = 0.297322 - 0.581051I$		
$u = 1.177360 + 0.140655I$		
$a = 1.271130 - 0.073091I$		
$b = 0.52624 - 1.59073I$	$-6.72367 + 2.38646I$	0
$c = 0.914208 - 0.465491I$		
$d = 0.97456 - 1.22806I$		
$u = 1.177360 - 0.140655I$		
$a = 1.271130 + 0.073091I$		
$b = 0.52624 + 1.59073I$	$-6.72367 - 2.38646I$	0
$c = 0.914208 + 0.465491I$		
$d = 0.97456 + 1.22806I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.516220 + 1.088150I$ $a = -0.25335 + 1.54951I$ $b = -2.64287 + 2.22003I$ $c = -0.099851 - 0.875419I$ $d = 1.071770 - 0.719904I$	$-2.28765 - 3.11487I$	0
$u = -0.516220 - 1.088150I$ $a = -0.25335 - 1.54951I$ $b = -2.64287 - 2.22003I$ $c = -0.099851 + 0.875419I$ $d = 1.071770 + 0.719904I$	$-2.28765 + 3.11487I$	0
$u = 1.143240 + 0.423905I$ $a = 1.84398 - 0.15315I$ $b = 1.05407 - 1.18141I$ $c = 1.391370 - 0.013506I$ $d = 1.59551 - 0.65628I$	$-5.54743 - 5.38085I$	0
$u = 1.143240 - 0.423905I$ $a = 1.84398 + 0.15315I$ $b = 1.05407 + 1.18141I$ $c = 1.391370 + 0.013506I$ $d = 1.59551 + 0.65628I$	$-5.54743 + 5.38085I$	0
$u = 1.079500 + 0.575143I$ $a = -1.83354 - 0.15848I$ $b = -0.99311 + 2.16498I$ $c = -1.062600 - 0.002710I$ $d = -1.21557 + 1.20650I$	$-1.00971 - 5.65602I$	0
$u = 1.079500 - 0.575143I$ $a = -1.83354 + 0.15848I$ $b = -0.99311 - 2.16498I$ $c = -1.062600 + 0.002710I$ $d = -1.21557 - 1.20650I$	$-1.00971 + 5.65602I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.163010 + 0.411297I$		
$a = 0.932646 - 0.077718I$		
$b = 0.61556 + 2.18561I$	$-5.58247 + 2.79509I$	0
$c = 0.600063 + 0.450923I$		
$d = 0.71184 + 1.55150I$		
$u = -1.163010 - 0.411297I$		
$a = 0.932646 + 0.077718I$		
$b = 0.61556 - 2.18561I$	$-5.58247 - 2.79509I$	0
$c = 0.600063 - 0.450923I$		
$d = 0.71184 - 1.55150I$		
$u = 0.530613 + 1.137340I$		
$a = -0.105063 + 0.441883I$		
$b = -0.477698 + 0.273175I$	$-2.68982 + 5.10175I$	0
$c = 0.250279 - 0.980703I$		
$d = -0.925423 - 0.856938I$		
$u = 0.530613 - 1.137340I$		
$a = -0.105063 - 0.441883I$		
$b = -0.477698 - 0.273175I$	$-2.68982 - 5.10175I$	0
$c = 0.250279 + 0.980703I$		
$d = -0.925423 + 0.856938I$		
$u = 0.601554 + 1.104580I$		
$a = -0.00922 + 1.88522I$		
$b = 2.21114 + 2.74600I$	$-1.29562 + 8.75795I$	0
$c = 0.048393 - 1.187080I$		
$d = -1.17229 - 1.05265I$		
$u = 0.601554 - 1.104580I$		
$a = -0.00922 - 1.88522I$		
$b = 2.21114 - 2.74600I$	$-1.29562 - 8.75795I$	0
$c = 0.048393 + 1.187080I$		
$d = -1.17229 + 1.05265I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.666542 + 1.084300I$		
$a = -0.037947 + 0.186829I$		
$b = 0.412925 - 0.063735I$	$2.21245 - 7.79054I$	0
$c = 0.116654 - 1.386120I$		
$d = 1.37592 - 1.25181I$		
$u = -0.666542 - 1.084300I$		
$a = -0.037947 - 0.186829I$		
$b = 0.412925 + 0.063735I$	$2.21245 + 7.79054I$	0
$c = 0.116654 + 1.386120I$		
$d = 1.37592 + 1.25181I$		
$u = -0.620529 + 0.325559I$		
$a = 1.77807 - 5.56934I$		
$b = 1.16767 + 1.32481I$	$-0.115678 - 1.341920I$	$2.41782 + 1.83708I$
$c = -0.359051 - 0.919317I$		
$d = 0.376140 + 0.228285I$		
$u = -0.620529 - 0.325559I$		
$a = 1.77807 + 5.56934I$		
$b = 1.16767 - 1.32481I$	$-0.115678 + 1.341920I$	$2.41782 - 1.83708I$
$c = -0.359051 + 0.919317I$		
$d = 0.376140 - 0.228285I$		
$u = -1.161000 + 0.625559I$		
$a = 1.85681 + 0.28553I$		
$b = 1.03264 + 2.35339I$	$-3.39852 + 10.69180I$	0
$c = 1.348640 + 0.218279I$		
$d = 1.44939 + 1.44440I$		
$u = -1.161000 - 0.625559I$		
$a = 1.85681 - 0.28553I$		
$b = 1.03264 - 2.35339I$	$-3.39852 - 10.69180I$	0
$c = 1.348640 - 0.218279I$		
$d = 1.44939 - 1.44440I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.423653 + 0.527399I$ $a = -1.74593 - 0.28445I$ $b = -0.556628 + 0.090443I$ $c = -0.424220 + 0.542119I$ $d = -0.623453 + 0.419471I$	$-1.92120 + 0.81846I$	$-4.58107 + 0.87681I$
$u = -0.423653 - 0.527399I$ $a = -1.74593 + 0.28445I$ $b = -0.556628 - 0.090443I$ $c = -0.424220 - 0.542119I$ $d = -0.623453 - 0.419471I$	$-1.92120 - 0.81846I$	$-4.58107 - 0.87681I$
$u = -0.662834 + 0.003253I$ $a = 0.226784 + 0.451173I$ $b = -0.577746 + 0.442113I$ $c = -0.680090 - 0.132286I$ $d = -0.197422 + 0.184363I$	$-0.58945 + 2.77011I$	$1.22579 - 6.61866I$
$u = -0.662834 - 0.003253I$ $a = 0.226784 - 0.451173I$ $b = -0.577746 - 0.442113I$ $c = -0.680090 + 0.132286I$ $d = -0.197422 - 0.184363I$	$-0.58945 - 2.77011I$	$1.22579 + 6.61866I$
$u = 0.703559 + 1.143570I$ $a = 0.181516 + 0.233850I$ $b = -0.233401 - 0.053613I$ $c = 0.04116 - 1.61209I$ $d = -1.22614 - 1.51356I$	$-0.07596 + 12.98220I$	0
$u = 0.703559 - 1.143570I$ $a = 0.181516 - 0.233850I$ $b = -0.233401 + 0.053613I$ $c = 0.04116 + 1.61209I$ $d = -1.22614 + 1.51356I$	$-0.07596 - 12.98220I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.624723 + 1.201920I$		
$a = -0.19734 - 2.12904I$		
$b = 0.63726 - 2.75540I$	$-5.70918 - 6.67323I$	0
$c = -0.33021 + 1.80553I$		
$d = -0.96291 + 1.48151I$		
$u = -0.624723 - 1.201920I$		
$a = -0.19734 + 2.12904I$		
$b = 0.63726 + 2.75540I$	$-5.70918 + 6.67323I$	0
$c = -0.33021 - 1.80553I$		
$d = -0.96291 - 1.48151I$		
$u = 0.127875 + 0.624992I$		
$a = 0.97951 + 3.07905I$		
$b = 0.341044 + 0.403757I$	$0.93270 - 1.56780I$	$-1.99036 - 0.81001I$
$c = 0.03373 - 2.60509I$		
$d = -0.194927 - 0.524028I$		
$u = 0.127875 - 0.624992I$		
$a = 0.97951 - 3.07905I$		
$b = 0.341044 - 0.403757I$	$0.93270 + 1.56780I$	$-1.99036 + 0.81001I$
$c = 0.03373 + 2.60509I$		
$d = -0.194927 + 0.524028I$		
$u = -0.115044 + 1.357830I$		
$a = 0.565753 - 0.402137I$		
$b = -1.143390 - 0.603699I$	$-9.14335 - 2.92995I$	0
$c = -1.139500 + 0.344978I$		
$d = -0.179723 + 0.294069I$		
$u = -0.115044 - 1.357830I$		
$a = 0.565753 + 0.402137I$		
$b = -1.143390 + 0.603699I$	$-9.14335 + 2.92995I$	0
$c = -1.139500 - 0.344978I$		
$d = -0.179723 - 0.294069I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.518606 + 1.307430I$ $a = 0.40096 - 2.01546I$ $b = -0.57151 - 2.58245I$ $c = -0.09494 + 1.89349I$ $d = 0.61008 + 1.60156I$	$-10.68990 + 3.50430I$	0
$u = 0.518606 - 1.307430I$ $a = 0.40096 + 2.01546I$ $b = -0.57151 + 2.58245I$ $c = -0.09494 - 1.89349I$ $d = 0.61008 - 1.60156I$	$-10.68990 - 3.50430I$	0
$u = 0.758435 + 1.184640I$ $a = -0.64579 + 2.27951I$ $b = 1.18564 + 3.27514I$ $c = 0.10967 - 1.88745I$ $d = -1.17616 - 1.81573I$	$-2.97939 + 12.30500I$	0
$u = 0.758435 - 1.184640I$ $a = -0.64579 - 2.27951I$ $b = 1.18564 - 3.27514I$ $c = 0.10967 + 1.88745I$ $d = -1.17616 + 1.81573I$	$-2.97939 - 12.30500I$	0
$u = 0.69467 + 1.24791I$ $a = 0.21709 - 2.24890I$ $b = -0.58292 - 2.80554I$ $c = 0.45261 + 2.01847I$ $d = 1.09745 + 1.65272I$	$-8.2281 + 11.9338I$	0
$u = 0.69467 - 1.24791I$ $a = 0.21709 + 2.24890I$ $b = -0.58292 + 2.80554I$ $c = 0.45261 - 2.01847I$ $d = 1.09745 - 1.65272I$	$-8.2281 - 11.9338I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.043030 + 0.567805I$ $a = -0.248115 + 0.756603I$ $b = -0.40870 + 1.85697I$ $c = -0.182345 + 1.003610I$ $d = -0.42920 + 2.02878I$	$0.91327 + 2.30980I$	$-2.35018 - 5.72620I$
$u = 0.043030 - 0.567805I$ $a = -0.248115 - 0.756603I$ $b = -0.40870 - 1.85697I$ $c = -0.182345 - 1.003610I$ $d = -0.42920 - 2.02878I$	$0.91327 - 2.30980I$	$-2.35018 + 5.72620I$
$u = -0.68480 + 1.26233I$ $a = 0.77022 + 1.88079I$ $b = -1.05613 + 2.67355I$ $c = -0.52883 - 1.71234I$ $d = 0.71570 - 1.66643I$	$-8.38263 - 9.37788I$	0
$u = -0.68480 - 1.26233I$ $a = 0.77022 - 1.88079I$ $b = -1.05613 - 2.67355I$ $c = -0.52883 + 1.71234I$ $d = 0.71570 + 1.66643I$	$-8.38263 + 9.37788I$	0
$u = -0.80648 + 1.20827I$ $a = 0.81681 + 2.38600I$ $b = -0.91530 + 3.40016I$ $c = -0.12117 - 2.11842I$ $d = 1.18116 - 2.06331I$	$-5.3240 - 17.7550I$	0
$u = -0.80648 - 1.20827I$ $a = 0.81681 - 2.38600I$ $b = -0.91530 - 3.40016I$ $c = -0.12117 + 2.11842I$ $d = 1.18116 + 2.06331I$	$-5.3240 + 17.7550I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.00564 + 1.45291I$		
$a = -0.851063 - 0.822170I$		
$b = 0.636678 - 1.070480I$	$-13.06970 - 1.34685I$	0
$c = 1.36039 + 0.81823I$		
$d = 0.427830 + 0.688849I$		
$u = -0.00564 - 1.45291I$		
$a = -0.851063 + 0.822170I$		
$b = 0.636678 + 1.070480I$	$-13.06970 + 1.34685I$	0
$c = 1.36039 - 0.81823I$		
$d = 0.427830 - 0.688849I$		
$u = 0.22004 + 1.44810I$		
$a = -0.929164 - 0.066704I$		
$b = 0.729786 - 0.060469I$	$-12.6554 + 7.5654I$	0
$c = 1.50177 + 0.01187I$		
$d = 0.470629 - 0.058111I$		
$u = 0.22004 - 1.44810I$		
$a = -0.929164 + 0.066704I$		
$b = 0.729786 + 0.060469I$	$-12.6554 - 7.5654I$	0
$c = 1.50177 - 0.01187I$		
$d = 0.470629 + 0.058111I$		
$u = 0.499413$		
$a = -1.13138$		
$b = 0.269950$	1.20722	9.11790
$c = 1.32737$		
$d = -0.0790890$		

$$\text{II. } I_2^u = \langle -43a^2u^3 - 37au^3 + \dots - 78a - 12, -47a^2u^3 - 52au^3 + \dots - 6a + 10, -24a^2u^3 - 19au^3 + \dots - 65a - 10, -2u^3a^2 - u^3a + \dots + a^3 + 2a^2, u^4 + u^2 - u + 1 \rangle$$

(i) **Arc colorings**

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} a \\ 0.338028a^2u^3 + 0.267606au^3 + \dots + 0.915493a + 0.140845 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.661972a^2u^3 + 0.732394au^3 + \dots + 0.0845070a - 0.140845 \\ 0.605634a^2u^3 + 0.521127au^3 + \dots + 1.09859a + 0.169014 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^3 \\ u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^3 + u^2 + 1 \\ -u^3 + u^2 - u + 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^3 + u^2 - u + 1 \\ u^2 - u + 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.338028a^2u^3 + 0.267606au^3 + \dots - 0.0845070a + 0.140845 \\ 0.281690a^2u^3 + 0.0563380au^3 + \dots + 0.929577a + 0.450704 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -0.0563380a^2u^3 - 0.211268au^3 + \dots + 1.01408a + 0.309859 \\ 0.281690a^2u^3 + 0.0563380au^3 + \dots + 0.929577a + 0.450704 \end{pmatrix}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $-4u^3 - 4u^2 + 2$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$(u^4 + 2u^3 + 3u^2 + u + 1)^3$
$c_2, c_4, c_5$ $c_9$	$(u^4 + u^2 - u + 1)^3$
$c_3$	$(u^4 - 3u^3 + 4u^2 - 3u + 2)^3$
$c_6, c_7, c_8$ $c_{10}, c_{12}$	$u^{12} - 4u^{10} - 2u^9 + 6u^8 + 6u^7 - u^6 - 6u^5 - 5u^4 + u^3 + 3u^2 + u + 1$
$c_{11}$	$u^{12} - 8u^{11} + \dots + 5u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^4 + 2y^3 + 7y^2 + 5y + 1)^3$
$c_2, c_4, c_5$ $c_9$	$(y^4 + 2y^3 + 3y^2 + y + 1)^3$
$c_3$	$(y^4 - y^3 + 2y^2 + 7y + 4)^3$
$c_6, c_7, c_8$ $c_{10}, c_{12}$	$y^{12} - 8y^{11} + \cdots + 5y + 1$
$c_{11}$	$y^{12} - 8y^{11} + \cdots - 31y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.547424 + 0.585652I$ $a = -1.89198 - 0.26082I$ $b = -3.05256 + 0.49971I$ $c = -1.42862 - 0.19451I$ $d = -2.88321 + 0.32177I$	$0.98010 + 1.39709I$	$3.77019 - 3.86736I$
$u = 0.547424 + 0.585652I$ $a = -0.0684280 + 0.0496997I$ $b = 0.375309 + 0.506052I$ $c = 0.571089 + 0.621740I$ $d = 0.814495 + 0.406682I$	$0.98010 + 1.39709I$	$3.77019 - 3.86736I$
$u = 0.547424 + 0.585652I$ $a = 0.25679 + 2.03371I$ $b = 0.973637 + 0.816821I$ $c = -0.23731 - 1.59853I$ $d = -0.729744 - 0.077176I$	$0.98010 + 1.39709I$	$3.77019 - 3.86736I$
$u = 0.547424 - 0.585652I$ $a = -1.89198 + 0.26082I$ $b = -3.05256 - 0.49971I$ $c = -1.42862 + 0.19451I$ $d = -2.88321 - 0.32177I$	$0.98010 - 1.39709I$	$3.77019 + 3.86736I$
$u = 0.547424 - 0.585652I$ $a = -0.0684280 - 0.0496997I$ $b = 0.375309 - 0.506052I$ $c = 0.571089 - 0.621740I$ $d = 0.814495 - 0.406682I$	$0.98010 - 1.39709I$	$3.77019 + 3.86736I$
$u = 0.547424 - 0.585652I$ $a = 0.25679 - 2.03371I$ $b = 0.973637 - 0.816821I$ $c = -0.23731 + 1.59853I$ $d = -0.729744 + 0.077176I$	$0.98010 - 1.39709I$	$3.77019 + 3.86736I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.547424 + 1.120870I$		
$a = 0.522652 - 0.149285I$		
$b = 0.017395 + 0.374071I$	$-2.62503 - 7.64338I$	$-1.77019 + 6.51087I$
$c = -0.25807 + 1.52032I$		
$d = -0.86105 + 1.25168I$		
$u = -0.547424 + 1.120870I$		
$a = 1.11333 - 1.38898I$		
$b = 1.91343 - 0.82551I$	$-2.62503 - 7.64338I$	$-1.77019 + 6.51087I$
$c = -0.173830 - 1.019770I$		
$d = 1.013450 - 0.887820I$		
$u = -0.547424 + 1.120870I$		
$a = -0.93237 + 2.97895I$		
$b = -1.22720 + 1.89212I$	$-2.62503 - 7.64338I$	$-1.77019 + 6.51087I$
$c = 1.52675 - 2.74230I$		
$d = 1.64606 - 1.16492I$		
$u = -0.547424 - 1.120870I$		
$a = 0.522652 + 0.149285I$		
$b = 0.017395 - 0.374071I$	$-2.62503 + 7.64338I$	$-1.77019 - 6.51087I$
$c = -0.25807 - 1.52032I$		
$d = -0.86105 - 1.25168I$		
$u = -0.547424 - 1.120870I$		
$a = 1.11333 + 1.38898I$		
$b = 1.91343 + 0.82551I$	$-2.62503 + 7.64338I$	$-1.77019 - 6.51087I$
$c = -0.173830 + 1.019770I$		
$d = 1.013450 + 0.887820I$		
$u = -0.547424 - 1.120870I$		
$a = -0.93237 - 2.97895I$		
$b = -1.22720 - 1.89212I$	$-2.62503 + 7.64338I$	$-1.77019 - 6.51087I$
$c = 1.52675 + 2.74230I$		
$d = 1.64606 + 1.16492I$		

$$\text{III. } I_3^u = \langle -75a^2u^5 + 125au^5 + \cdots - 31a + 44, -55a^2u^5 + 167au^5 + \cdots + 143a - 28, -58a^2u^5 + 59au^5 + \cdots - 30a + 28, -2u^5a^2 + 2u^5a + \cdots - 4a^2 + 2a, u^6 + u^5 + \cdots + 2u + 1 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_4 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_5 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_7 &= \begin{pmatrix} a \\ 0.513274a^2u^5 - 0.522124au^5 + \cdots + 0.265487a - 0.247788 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} u \\ u \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 0.486726a^2u^5 - 1.47788au^5 + \cdots - 1.26549a + 0.247788 \\ 0.663717a^2u^5 - 1.10619au^5 + \cdots + 0.274336a - 0.389381 \end{pmatrix} \\ a_1 &= \begin{pmatrix} u \\ u \end{pmatrix} \\ a_6 &= \begin{pmatrix} u^3 \\ u^3 + u \end{pmatrix} \\ a_3 &= \begin{pmatrix} u^5 + u^4 + 2u^3 + 2u^2 + 2u + 2 \\ u^5 + 2u^3 + u^2 + 2u + 1 \end{pmatrix} \\ a_2 &= \begin{pmatrix} u^4 + u^2 + u + 1 \\ 2u^5 + u^4 + 3u^3 + 2u^2 + 3u + 2 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0.513274a^2u^5 - 0.522124au^5 + \cdots - 0.734513a - 0.247788 \\ 0.690265a^2u^5 - 0.150442au^5 + \cdots + 0.805310a - 0.884956 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 0.176991a^2u^5 + 0.371681au^5 + \cdots + 1.53982a - 0.637168 \\ 0.690265a^2u^5 - 0.150442au^5 + \cdots + 0.805310a - 0.884956 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $-4u^3 - 4u - 2$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$(u^6 + 3u^5 + 4u^4 + 2u^3 + 1)^3$
$c_2, c_4, c_5$ $c_9$	$(u^6 + u^5 + 2u^4 + 2u^3 + 2u^2 + 2u + 1)^3$
$c_3$	$(u^3 + u^2 - 1)^6$
$c_6, c_7, c_8$ $c_{10}, c_{12}$	$u^{18} - 6u^{16} + \cdots + 2u^3 + 1$
$c_{11}$	$u^{18} - 12u^{17} + \cdots + 8u^2 + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^6 - y^5 + 4y^4 - 2y^3 + 8y^2 + 1)^3$
$c_2, c_4, c_5$ $c_9$	$(y^6 + 3y^5 + 4y^4 + 2y^3 + 1)^3$
$c_3$	$(y^3 - y^2 + 2y - 1)^6$
$c_6, c_7, c_8$ $c_{10}, c_{12}$	$y^{18} - 12y^{17} + \cdots + 8y^2 + 1$
$c_{11}$	$y^{18} - 12y^{17} + \cdots + 16y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.498832 + 1.001300I$ $a = -1.17148 - 1.07480I$ $b = -1.99587 - 0.45347I$ $c = -0.157661 - 0.713279I$ $d = -1.32986 - 0.49621I$	$-0.26574 + 2.82812I$	$1.50976 - 2.97945I$
$u = 0.498832 + 1.001300I$ $a = -0.358089 - 0.128198I$ $b = 0.131651 + 0.402262I$ $c = 0.299325 + 1.234880I$ $d = 0.840299 + 1.017300I$	$-0.26574 + 2.82812I$	$1.50976 - 2.97945I$
$u = 0.498832 + 1.001300I$ $a = 0.73236 + 2.80324I$ $b = 1.06700 + 1.65145I$ $c = -1.13933 - 2.52421I$ $d = -1.30532 - 0.92346I$	$-0.26574 + 2.82812I$	$1.50976 - 2.97945I$
$u = 0.498832 - 1.001300I$ $a = -1.17148 + 1.07480I$ $b = -1.99587 + 0.45347I$ $c = -0.157661 + 0.713279I$ $d = -1.32986 + 0.49621I$	$-0.26574 - 2.82812I$	$1.50976 + 2.97945I$
$u = 0.498832 - 1.001300I$ $a = -0.358089 + 0.128198I$ $b = 0.131651 - 0.402262I$ $c = 0.299325 - 1.234880I$ $d = 0.840299 - 1.017300I$	$-0.26574 - 2.82812I$	$1.50976 + 2.97945I$
$u = 0.498832 - 1.001300I$ $a = 0.73236 - 2.80324I$ $b = 1.06700 - 1.65145I$ $c = -1.13933 + 2.52421I$ $d = -1.30532 + 0.92346I$	$-0.26574 - 2.82812I$	$1.50976 + 2.97945I$

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.284920 + 1.115140I$		
$a = 0.589677 - 1.038010I$		
$b = 1.292560 - 0.412855I$	-4.40332	$-5.01951 + 0.I$
$c = -0.384455 - 0.173537I$		
$d = 0.624963 - 0.038245I$		
$u = -0.284920 + 1.115140I$		
$a = 0.295266 - 0.439795I$		
$b = -0.225579 + 0.124250I$	-4.40332	$-5.01951 + 0.I$
$c = 0.183101 + 1.122730I$		
$d = -0.485466 + 1.007580I$		
$u = -0.284920 + 1.115140I$		
$a = -0.45478 + 3.16140I$		
$b = -0.63682 + 1.97219I$	-4.40332	$-5.01951 + 0.I$
$c = 0.77119 - 3.17947I$		
$d = 0.86050 - 1.51603I$		
$u = -0.284920 - 1.115140I$		
$a = 0.589677 + 1.038010I$		
$b = 1.292560 + 0.412855I$	-4.40332	$-5.01951 + 0.I$
$c = -0.384455 + 0.173537I$		
$d = 0.624963 + 0.038245I$		
$u = -0.284920 - 1.115140I$		
$a = 0.295266 + 0.439795I$		
$b = -0.225579 - 0.124250I$	-4.40332	$-5.01951 + 0.I$
$c = 0.183101 - 1.122730I$		
$d = -0.485466 - 1.007580I$		
$u = -0.284920 - 1.115140I$		
$a = -0.45478 - 3.16140I$		
$b = -0.63682 - 1.97219I$	-4.40332	$-5.01951 + 0.I$
$c = 0.77119 + 3.17947I$		
$d = 0.86050 + 1.51603I$		

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.713912 + 0.305839I$ $a = -0.161975 + 1.103030I$ $b = -1.085250 + 0.272261I$ $c = -0.223253 - 0.651146I$ $d = 0.361764 + 0.394419I$	$-0.26574 + 2.82812I$	$1.50976 - 2.97945I$
$u = -0.713912 + 0.305839I$ $a = -0.0828484 + 0.0502791I$ $b = -0.632432 + 0.441144I$ $c = -0.713791 + 0.255078I$ $d = -0.738624 - 0.097289I$	$-0.26574 + 2.82812I$	$1.50976 - 2.97945I$
$u = -0.713912 + 0.305839I$ $a = 2.61188 - 0.13927I$ $b = 4.08474 + 0.30064I$ $c = 2.36487 - 0.21561I$ $d = 4.17174 + 0.10523I$	$-0.26574 + 2.82812I$	$1.50976 - 2.97945I$
$u = -0.713912 - 0.305839I$ $a = -0.161975 - 1.103030I$ $b = -1.085250 - 0.272261I$ $c = -0.223253 + 0.651146I$ $d = 0.361764 - 0.394419I$	$-0.26574 - 2.82812I$	$1.50976 + 2.97945I$
$u = -0.713912 - 0.305839I$ $a = -0.0828484 - 0.0502791I$ $b = -0.632432 - 0.441144I$ $c = -0.713791 - 0.255078I$ $d = -0.738624 + 0.097289I$	$-0.26574 - 2.82812I$	$1.50976 + 2.97945I$
$u = -0.713912 - 0.305839I$ $a = 2.61188 + 0.13927I$ $b = 4.08474 - 0.30064I$ $c = 2.36487 + 0.21561I$ $d = 4.17174 - 0.10523I$	$-0.26574 - 2.82812I$	$1.50976 + 2.97945I$

$$\text{IV. } I_1^v = \langle a, d - v + 1, c + a, b + v - 1, v^2 - v + 1 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ -v + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ v - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ v - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ -v + 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ v \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -v + 1 \\ v \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} v \\ v - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ -v + 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-4v + 11$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_5$	$u^2 - u + 1$
$c_2$	$u^2 + u + 1$
$c_4, c_6, c_7$ $c_9, c_{12}$	$u^2$
$c_8$	$(u + 1)^2$
$c_{10}, c_{11}$	$(u - 1)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_5$	$y^2 + y + 1$
$c_4, c_6, c_7$ $c_9, c_{12}$	$y^2$
$c_8, c_{10}, c_{11}$	$(y - 1)^2$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_1^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = 0.500000 + 0.866025I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0$		
$b = 0.500000 - 0.866025I$	$1.64493 + 2.02988I$	$9.00000 - 3.46410I$
$c = 0$		
$d = -0.500000 + 0.866025I$		
$v = 0.500000 - 0.866025I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0$		
$b = 0.500000 + 0.866025I$	$1.64493 - 2.02988I$	$9.00000 + 3.46410I$
$c = 0$		
$d = -0.500000 - 0.866025I$		

$$\mathbf{V. } I_2^v = \langle a, d, c - v, b - v - 1, v^2 + v + 1 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_4 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_9 &= \begin{pmatrix} v \\ 0 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 0 \\ v + 1 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} v \\ 0 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} v \\ 0 \end{pmatrix} \\ a_1 &= \begin{pmatrix} v \\ -v - 1 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -v \\ v + 1 \end{pmatrix} \\ a_3 &= \begin{pmatrix} 0 \\ -v \end{pmatrix} \\ a_2 &= \begin{pmatrix} v \\ -v \end{pmatrix} \\ a_{11} &= \begin{pmatrix} v \\ 0 \end{pmatrix} \\ a_8 &= \begin{pmatrix} v \\ 0 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes =  $4v - 1$**

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_5$	$u^2 - u + 1$
$c_2$	$u^2 + u + 1$
$c_4, c_8, c_9$ $c_{10}, c_{11}$	$u^2$
$c_6, c_7$	$(u - 1)^2$
$c_{12}$	$(u + 1)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_5$	$y^2 + y + 1$
$c_4, c_8, c_9$ $c_{10}, c_{11}$	$y^2$
$c_6, c_7, c_{12}$	$(y - 1)^2$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_2^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = -0.500000 + 0.866025I$		
$a = 0$		
$b = 0.500000 + 0.866025I$	$-1.64493 - 2.02988I$	$-3.00000 + 3.46410I$
$c = -0.500000 + 0.866025I$		
$d = 0$		
$v = -0.500000 - 0.866025I$		
$a = 0$		
$b = 0.500000 - 0.866025I$	$-1.64493 + 2.02988I$	$-3.00000 - 3.46410I$
$c = -0.500000 - 0.866025I$		
$d = 0$		

$$\mathbf{VI.} \quad I_3^v = \langle a, d+1, c+a-1, b-1, v-1 \rangle$$

(i) **Arc colorings**

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 2 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes = 0**

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_3$ $c_4, c_5, c_9$	$u$
$c_6, c_7, c_8$	$u + 1$
$c_{10}, c_{11}, c_{12}$	$u - 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_4, c_5, c_9$	$y$
$c_6, c_7, c_8$ $c_{10}, c_{11}, c_{12}$	$y - 1$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_3^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = 1.00000$		
$a = 0$		
$b = 1.00000$	0	0
$c = 1.00000$		
$d = -1.00000$		

$$\text{VII. } I_4^v = \langle a, -b^2v - bv + \dots + 2b + 1, -b^2av - bav + \dots + a - 1, v^2c + v^2b + \dots + c + 2a, b^2v^2 + v^2b + \dots - v + 1 \rangle$$

(i) **Arc colorings**

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ b \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} c \\ b^2v + bv - 2b + v - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} c \\ b^2v + bv - b + v - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} c \\ b^2v + bv - b + v - 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -cv - bv + c - v + 2 \\ b^2v + bv - b + v \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -b^2v - cv - 2bv + c + b - 2v + 2 \\ b^2v + bv - b + v \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} c + v \\ b^2v + bv - 2b + v - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -c \\ -b^2v - bv + 2b - v + 1 \end{pmatrix}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $2b^3v - b^2v - 3b^2 - bv - v^2 + b - 3v + 4$

(iv) **u-Polynomials at the component** : It cannot be defined for a positive dimension component.

(v) **Riley Polynomials at the component** : It cannot be defined for a positive dimension component.

**(iv) Complex Volumes and Cusp Shapes**

Solution to $I_4^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = \dots$		
$a = \dots$		
$b = \dots$	$-2.02988I$	$1.64184 - 3.78338I$
$c = \dots$		
$d = \dots$		

### VIII. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$u(u^2 - u + 1)^2(u^4 + 2u^3 + 3u^2 + u + 1)^3(u^6 + 3u^5 + 4u^4 + 2u^3 + 1)^3 \cdot (u^{77} + 36u^{76} + \dots + 216u - 16)$
$c_2$	$u(u^2 + u + 1)^2(u^4 + u^2 - u + 1)^3 \cdot ((u^6 + u^5 + 2u^4 + 2u^3 + 2u^2 + 2u + 1)^3)(u^{77} + 2u^{76} + \dots + 27u^2 - 4)$
$c_3$	$u(u^2 - u + 1)^2(u^3 + u^2 - 1)^6(u^4 - 3u^3 + 4u^2 - 3u + 2)^3 \cdot (u^{77} - 2u^{76} + \dots + 351912u - 66564)$
$c_4, c_9$	$u^5(u^4 + u^2 - u + 1)^3(u^6 + u^5 + 2u^4 + 2u^3 + 2u^2 + 2u + 1)^3 \cdot (u^{77} - 2u^{76} + \dots - 2560u^2 - 512)$
$c_5$	$u(u^2 - u + 1)^2(u^4 + u^2 - u + 1)^3 \cdot ((u^6 + u^5 + 2u^4 + 2u^3 + 2u^2 + 2u + 1)^3)(u^{77} + 2u^{76} + \dots + 27u^2 - 4)$
$c_6, c_7$	$u^2(u - 1)^2(u + 1) \cdot (u^{12} - 4u^{10} - 2u^9 + 6u^8 + 6u^7 - u^6 - 6u^5 - 5u^4 + u^3 + 3u^2 + u + 1) \cdot (u^{18} - 6u^{16} + \dots + 2u^3 + 1)(u^{77} - 8u^{76} + \dots - 72u - 16)$
$c_8$	$u^2(u + 1)^3 \cdot (u^{12} - 4u^{10} - 2u^9 + 6u^8 + 6u^7 - u^6 - 6u^5 - 5u^4 + u^3 + 3u^2 + u + 1) \cdot (u^{18} - 6u^{16} + \dots + 2u^3 + 1)(u^{77} + 8u^{76} + \dots - 72u - 16)$
$c_{10}$	$u^2(u - 1)^3 \cdot (u^{12} - 4u^{10} - 2u^9 + 6u^8 + 6u^7 - u^6 - 6u^5 - 5u^4 + u^3 + 3u^2 + u + 1) \cdot (u^{18} - 6u^{16} + \dots + 2u^3 + 1)(u^{77} + 8u^{76} + \dots - 72u - 16)$
$c_{11}$	$u^2(u - 1)^3(u^{12} - 8u^{11} + \dots + 5u + 1)(u^{18} - 12u^{17} + \dots + 8u^2 + 1) \cdot (u^{77} - 34u^{76} + \dots + 1568u - 256)$
$c_{12}$	$u^2(u - 1)(u + 1)^2 \cdot (u^{12} - 4u^{10} - 2u^9 + 6u^8 + 6u^7 - u^6 - 6u^5 - 5u^4 + u^3 + 3u^2 + u + 1) \cdot (u^{18} - 6u^{16} + \dots + 2u^3 + 1)(u^{77} - 8u^{76} + \dots - 72u - 16)$

## IX. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$y(y^2 + y + 1)^2(y^4 + 2y^3 + 7y^2 + 5y + 1)^3$ $\cdot ((y^6 - y^5 + 4y^4 - 2y^3 + 8y^2 + 1)^3)(y^{77} + 12y^{76} + \dots + 84256y - 256)$
$c_2, c_5$	$y(y^2 + y + 1)^2(y^4 + 2y^3 + 3y^2 + y + 1)^3(y^6 + 3y^5 + 4y^4 + 2y^3 + 1)^3$ $\cdot (y^{77} + 36y^{76} + \dots + 216y - 16)$
$c_3$	$y(y^2 + y + 1)^2(y^3 - y^2 + 2y - 1)^6(y^4 - y^3 + 2y^2 + 7y + 4)^3$ $\cdot (y^{77} - 12y^{76} + \dots + 120020616504y - 4430766096)$
$c_4, c_9$	$y^5(y^4 + 2y^3 + 3y^2 + y + 1)^3(y^6 + 3y^5 + 4y^4 + 2y^3 + 1)^3$ $\cdot (y^{77} + 30y^{76} + \dots - 2621440y - 262144)$
$c_6, c_7, c_{12}$	$y^2(y - 1)^3(y^{12} - 8y^{11} + \dots + 5y + 1)(y^{18} - 12y^{17} + \dots + 8y^2 + 1)$ $\cdot (y^{77} - 74y^{76} + \dots + 7712y - 256)$
$c_8, c_{10}$	$y^2(y - 1)^3(y^{12} - 8y^{11} + \dots + 5y + 1)(y^{18} - 12y^{17} + \dots + 8y^2 + 1)$ $\cdot (y^{77} - 34y^{76} + \dots + 1568y - 256)$
$c_{11}$	$y^2(y - 1)^3(y^{12} - 8y^{11} + \dots - 31y + 1)(y^{18} - 12y^{17} + \dots + 16y + 1)$ $\cdot (y^{77} + 26y^{76} + \dots + 3416576y - 65536)$