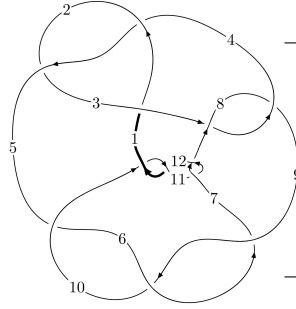
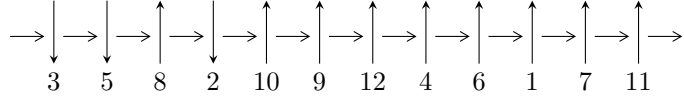


12a<sub>0089</sub> (K12a<sub>0089</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$5,10 \xrightarrow{c_5} 3,6 \xrightarrow{c_2} 2 \xrightarrow{c_1} 1 \xrightarrow{c_{10}} 11 \xrightarrow{c_4} 4 \xrightarrow{c_9} 9 \xrightarrow{c_6} 7 \xrightarrow{c_8} 8 \xrightarrow{c_{12}} 12 \Rightarrow c_3, c_7, c_{11}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -2.39749 \times 10^{215} u^{99} - 3.64797 \times 10^{215} u^{98} + \dots + 1.47790 \times 10^{217} b - 8.18496 \times 10^{217}, \\ -7.22651 \times 10^{217} u^{99} - 1.52650 \times 10^{218} u^{98} + \dots + 6.20718 \times 10^{218} a + 5.09074 \times 10^{219}, \\ u^{100} + 2u^{99} + \dots - 329u - 49 \rangle$$

$$I_2^u = \langle 1878a^5u - 2600a^4u + \dots + 23830a - 8647, \\ a^6 + 3a^5u - 4a^5 - 7a^4u - a^4 + a^3u - 3a^3 - 9a^2u + 5a^2 + 6au + 2a - u, u^2 + 1 \rangle$$

$$I_3^u = \langle b + 1, -u^3 - u^2 + a - 3u - 2, u^5 + u^4 + 4u^3 + 3u^2 + 3u + 1 \rangle$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 117 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -2.40 \times 10^{215}u^{99} - 3.65 \times 10^{215}u^{98} + \dots + 1.48 \times 10^{217}b - 8.18 \times 10^{217}, -7.23 \times 10^{217}u^{99} - 1.53 \times 10^{218}u^{98} + \dots + 6.21 \times 10^{218}a + 5.09 \times 10^{219}, u^{100} + 2u^{99} + \dots - 329u - 49 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0.116422u^{99} + 0.245925u^{98} + \dots - 89.5951u - 8.20137 \\ 0.0162222u^{99} + 0.0246835u^{98} + \dots + 12.6540u + 5.53823 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.132644u^{99} + 0.270609u^{98} + \dots - 76.9410u - 2.66314 \\ 0.0162222u^{99} + 0.0246835u^{98} + \dots + 12.6540u + 5.53823 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0.109624u^{99} + 0.205069u^{98} + \dots - 101.450u - 13.1153 \\ 0.0556512u^{99} + 0.125051u^{98} + \dots - 32.6639u - 1.40263 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.0962786u^{99} + 0.162953u^{98} + \dots - 42.0923u + 2.63606 \\ -0.0148568u^{99} - 0.0180767u^{98} + \dots + 15.1895u + 5.87732 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.0397497u^{99} + 0.138384u^{98} + \dots - 87.1158u - 19.5365 \\ 0.0202763u^{99} + 0.0752641u^{98} + \dots - 32.7675u - 4.86979 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^2 + 1 \\ -u^4 - 2u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0.0290553u^{99} + 0.0399308u^{98} + \dots + 26.9108u + 15.1478 \\ -0.0135353u^{99} - 0.0340762u^{98} + \dots + 44.4150u + 8.98928 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.109897u^{99} + 0.198612u^{98} + \dots - 42.6716u + 4.91221 \\ -0.0101391u^{99} - 0.0246196u^{98} + \dots + 21.3117u + 6.96002 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $0.216920u^{99} + 0.318284u^{98} + \dots - 68.3104u + 21.0535$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{100} + 50u^{99} + \dots + 79u + 1$
$c_2, c_4$	$u^{100} - 10u^{99} + \dots + 11u - 1$
$c_3, c_8$	$u^{100} + u^{99} + \dots + 224u + 32$
$c_5, c_6, c_9$	$u^{100} + 2u^{99} + \dots - 329u - 49$
$c_7, c_{11}$	$u^{100} + 2u^{99} + \dots - 15u - 17$
$c_{10}, c_{12}$	$u^{100} - 32u^{99} + \dots + 149u + 289$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{100} + 10y^{99} + \dots - 2487y + 1$
$c_2, c_4$	$y^{100} - 50y^{99} + \dots - 79y + 1$
$c_3, c_8$	$y^{100} - 45y^{99} + \dots - 52736y + 1024$
$c_5, c_6, c_9$	$y^{100} + 98y^{99} + \dots + 34251y + 2401$
$c_7, c_{11}$	$y^{100} - 32y^{99} + \dots + 149y + 289$
$c_{10}, c_{12}$	$y^{100} + 80y^{99} + \dots - 3531239y + 83521$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.065515 + 0.990541I$ $a = -0.41447 + 7.77506I$ $b = -1.024690 - 0.010060I$	$-3.35320 - 2.04195I$	0
$u = -0.065515 - 0.990541I$ $a = -0.41447 - 7.77506I$ $b = -1.024690 + 0.010060I$	$-3.35320 + 2.04195I$	0
$u = -0.969042 + 0.362969I$ $a = -0.44792 - 1.56289I$ $b = 1.167800 + 0.578024I$	$-1.88652 - 12.41730I$	0
$u = -0.969042 - 0.362969I$ $a = -0.44792 + 1.56289I$ $b = 1.167800 - 0.578024I$	$-1.88652 + 12.41730I$	0
$u = 0.940871 + 0.436198I$ $a = -0.35176 + 1.46851I$ $b = 1.145610 - 0.541902I$	$-2.76156 + 6.42552I$	0
$u = 0.940871 - 0.436198I$ $a = -0.35176 - 1.46851I$ $b = 1.145610 + 0.541902I$	$-2.76156 - 6.42552I$	0
$u = -0.449054 + 0.956643I$ $a = 0.757248 - 1.013000I$ $b = 0.254382 + 0.493343I$	$-1.24139 + 2.42018I$	0
$u = -0.449054 - 0.956643I$ $a = 0.757248 + 1.013000I$ $b = 0.254382 - 0.493343I$	$-1.24139 - 2.42018I$	0
$u = -0.246189 + 1.031340I$ $a = -0.113223 + 0.585328I$ $b = 0.978093 - 0.719756I$	$2.20888 + 3.42556I$	0
$u = -0.246189 - 1.031340I$ $a = -0.113223 - 0.585328I$ $b = 0.978093 + 0.719756I$	$2.20888 - 3.42556I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.843566 + 0.298352I$ $a = -0.38582 + 1.43354I$ $b = 0.289367 - 0.846254I$	$0.73862 - 7.15845I$	0
$u = -0.843566 - 0.298352I$ $a = -0.38582 - 1.43354I$ $b = 0.289367 + 0.846254I$	$0.73862 + 7.15845I$	0
$u = -0.299712 + 1.087720I$ $a = 0.278229 - 1.043020I$ $b = 0.683576 + 0.775155I$	$3.05539 - 2.19835I$	0
$u = -0.299712 - 1.087720I$ $a = 0.278229 + 1.043020I$ $b = 0.683576 - 0.775155I$	$3.05539 + 2.19835I$	0
$u = 0.764156 + 0.417633I$ $a = 0.82151 - 2.08873I$ $b = -1.072760 + 0.478965I$	$-3.62812 + 6.33519I$	0
$u = 0.764156 - 0.417633I$ $a = 0.82151 + 2.08873I$ $b = -1.072760 - 0.478965I$	$-3.62812 - 6.33519I$	0
$u = 0.588441 + 0.632133I$ $a = 0.860063 + 0.744032I$ $b = -1.160920 - 0.298625I$	$-4.41103 - 1.68246I$	0
$u = 0.588441 - 0.632133I$ $a = 0.860063 - 0.744032I$ $b = -1.160920 + 0.298625I$	$-4.41103 + 1.68246I$	0
$u = 0.187210 + 1.126150I$ $a = 1.048240 + 0.603763I$ $b = -0.668387 - 0.373530I$	$-1.86846 + 1.01624I$	0
$u = 0.187210 - 1.126150I$ $a = 1.048240 - 0.603763I$ $b = -0.668387 + 0.373530I$	$-1.86846 - 1.01624I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.680822 + 0.503951I$ $a = 0.71326 + 2.08961I$ $b = -1.097340 - 0.410444I$	$-4.15515 - 0.77241I$	0
$u = -0.680822 - 0.503951I$ $a = 0.71326 - 2.08961I$ $b = -1.097340 + 0.410444I$	$-4.15515 + 0.77241I$	0
$u = 0.775959 + 0.333569I$ $a = -0.247079 - 1.299000I$ $b = 0.253877 + 0.752651I$	$-0.16735 + 1.55705I$	0
$u = 0.775959 - 0.333569I$ $a = -0.247079 + 1.299000I$ $b = 0.253877 - 0.752651I$	$-0.16735 - 1.55705I$	0
$u = 0.796339 + 0.840767I$ $a = -0.413671 - 0.190155I$ $b = 1.063020 + 0.436471I$	$-3.95267 - 0.55388I$	0
$u = 0.796339 - 0.840767I$ $a = -0.413671 + 0.190155I$ $b = 1.063020 - 0.436471I$	$-3.95267 + 0.55388I$	0
$u = -0.670815 + 0.499865I$ $a = 0.827036 - 0.598048I$ $b = -1.224950 + 0.246355I$	$-4.17026 - 3.77857I$	0
$u = -0.670815 - 0.499865I$ $a = 0.827036 + 0.598048I$ $b = -1.224950 - 0.246355I$	$-4.17026 + 3.77857I$	0
$u = 0.471451 + 1.064550I$ $a = 0.468004 + 0.750338I$ $b = 0.586409 - 0.261443I$	$-2.12923 + 2.75082I$	0
$u = 0.471451 - 1.064550I$ $a = 0.468004 - 0.750338I$ $b = 0.586409 + 0.261443I$	$-2.12923 - 2.75082I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.748764 + 0.934617I$ $a = -0.435746 + 0.254991I$ $b = 1.101640 - 0.489464I$	$-3.58978 + 6.56550I$	0
$u = -0.748764 - 0.934617I$ $a = -0.435746 - 0.254991I$ $b = 1.101640 + 0.489464I$	$-3.58978 - 6.56550I$	0
$u = 0.545121 + 0.587251I$ $a = 0.377482 + 1.297890I$ $b = 0.940217 - 0.555672I$	$0.74183 + 4.19177I$	$0. - 6.66805I$
$u = 0.545121 - 0.587251I$ $a = 0.377482 - 1.297890I$ $b = 0.940217 + 0.555672I$	$0.74183 - 4.19177I$	$0. + 6.66805I$
$u = -0.681505 + 0.289527I$ $a = 0.03851 - 1.94789I$ $b = 1.043400 + 0.637281I$	$4.27099 - 6.89948I$	$11.43396 + 7.69737I$
$u = -0.681505 - 0.289527I$ $a = 0.03851 + 1.94789I$ $b = 1.043400 - 0.637281I$	$4.27099 + 6.89948I$	$11.43396 - 7.69737I$
$u = -0.721641 + 0.152687I$ $a = -0.844995 + 1.089000I$ $b = 0.516426 - 0.779174I$	$5.82753 - 1.57926I$	$14.4879 + 1.7882I$
$u = -0.721641 - 0.152687I$ $a = -0.844995 - 1.089000I$ $b = 0.516426 + 0.779174I$	$5.82753 + 1.57926I$	$14.4879 - 1.7882I$
$u = -0.082557 + 1.272520I$ $a = -1.88035 - 0.05417I$ $b = -1.159760 + 0.213440I$	$-3.77500 - 2.20981I$	0
$u = -0.082557 - 1.272520I$ $a = -1.88035 + 0.05417I$ $b = -1.159760 - 0.213440I$	$-3.77500 + 2.20981I$	0



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.210143 + 1.259280I$ $a = 0.208298 - 0.400854I$ $b = 0.395459 - 0.440267I$	$-0.98799 + 1.90733I$	0
$u = -0.210143 - 1.259280I$ $a = 0.208298 + 0.400854I$ $b = 0.395459 + 0.440267I$	$-0.98799 - 1.90733I$	0
$u = -0.000512 + 1.327390I$ $a = -0.130531 + 0.995414I$ $b = 0.925020 - 0.921002I$	$-0.781932 + 0.661024I$	0
$u = -0.000512 - 1.327390I$ $a = -0.130531 - 0.995414I$ $b = 0.925020 + 0.921002I$	$-0.781932 - 0.661024I$	0
$u = 0.609534 + 0.272478I$ $a = -0.584068 - 0.350171I$ $b = 0.636787 + 0.561311I$	$1.64920 - 0.29233I$	$8.03329 - 0.15871I$
$u = 0.609534 - 0.272478I$ $a = -0.584068 + 0.350171I$ $b = 0.636787 - 0.561311I$	$1.64920 + 0.29233I$	$8.03329 + 0.15871I$
$u = -0.092924 + 1.331590I$ $a = -0.065930 - 1.068640I$ $b = 0.866501 + 0.946140I$	$-0.60519 - 6.07717I$	0
$u = -0.092924 - 1.331590I$ $a = -0.065930 + 1.068640I$ $b = 0.866501 - 0.946140I$	$-0.60519 + 6.07717I$	0
$u = 0.171260 + 1.324520I$ $a = -1.05185 - 1.79678I$ $b = -1.035660 + 0.449155I$	$-3.23240 + 4.53436I$	0
$u = 0.171260 - 1.324520I$ $a = -1.05185 + 1.79678I$ $b = -1.035660 - 0.449155I$	$-3.23240 - 4.53436I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.158952 + 1.352890I$ $a = 0.057726 - 0.217470I$ $b = 0.119895 + 0.688596I$	$-3.26940 + 2.41579I$	0
$u = 0.158952 - 1.352890I$ $a = 0.057726 + 0.217470I$ $b = 0.119895 - 0.688596I$	$-3.26940 - 2.41579I$	0
$u = -0.270114 + 1.346370I$ $a = -0.440781 + 0.149707I$ $b = 0.326391 - 0.819413I$	$1.09915 - 5.14819I$	0
$u = -0.270114 - 1.346370I$ $a = -0.440781 - 0.149707I$ $b = 0.326391 + 0.819413I$	$1.09915 + 5.14819I$	0
$u = 0.359092 + 0.487765I$ $a = 1.79802 + 1.38487I$ $b = -0.343192 - 0.347888I$	$-1.57085 + 2.44408I$	$6.62536 - 3.00383I$
$u = 0.359092 - 0.487765I$ $a = 1.79802 - 1.38487I$ $b = -0.343192 + 0.347888I$	$-1.57085 - 2.44408I$	$6.62536 + 3.00383I$
$u = -0.039784 + 1.394580I$ $a = -1.10221 + 0.98947I$ $b = -1.170370 - 0.381652I$	$-6.92039 - 1.32032I$	0
$u = -0.039784 - 1.394580I$ $a = -1.10221 - 0.98947I$ $b = -1.170370 + 0.381652I$	$-6.92039 + 1.32032I$	0
$u = 0.060535 + 0.600233I$ $a = 2.03401 - 0.69858I$ $b = -0.267096 + 0.124271I$	$-1.59835 + 2.35283I$	$6.98886 - 5.08882I$
$u = 0.060535 - 0.600233I$ $a = 2.03401 + 0.69858I$ $b = -0.267096 - 0.124271I$	$-1.59835 - 2.35283I$	$6.98886 + 5.08882I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.583705 + 0.093529I$ $a = 1.08030 - 2.39263I$ $b = -0.837645 + 0.440777I$	$1.17772 + 1.85934I$	$10.62955 - 4.30757I$
$u = 0.583705 - 0.093529I$ $a = 1.08030 + 2.39263I$ $b = -0.837645 - 0.440777I$	$1.17772 - 1.85934I$	$10.62955 + 4.30757I$
$u = -0.10232 + 1.46119I$ $a = 1.233410 - 0.510771I$ $b = 1.064130 + 0.480659I$	$-2.93294 - 2.08208I$	0
$u = -0.10232 - 1.46119I$ $a = 1.233410 + 0.510771I$ $b = 1.064130 - 0.480659I$	$-2.93294 + 2.08208I$	0
$u = -0.26298 + 1.44481I$ $a = 1.06935 - 1.24629I$ $b = 1.148140 + 0.579376I$	$-1.35388 - 10.35240I$	0
$u = -0.26298 - 1.44481I$ $a = 1.06935 + 1.24629I$ $b = 1.148140 - 0.579376I$	$-1.35388 + 10.35240I$	0
$u = -0.530564$ $a = 0.408996$ $b = -1.19118$	$-0.0949506$	15.0060
$u = 0.17399 + 1.46493I$ $a = 0.589969 + 0.807489I$ $b = -0.470039 - 0.824556I$	$-7.81095 + 4.69129I$	0
$u = 0.17399 - 1.46493I$ $a = 0.589969 - 0.807489I$ $b = -0.470039 + 0.824556I$	$-7.81095 - 4.69129I$	0
$u = -0.11054 + 1.47556I$ $a = 0.500820 - 0.770357I$ $b = -0.381208 + 0.834378I$	$-8.30671 + 1.25779I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.11054 - 1.47556I$		
$a = 0.500820 + 0.770357I$	$-8.30671 - 1.25779I$	0
$b = -0.381208 - 0.834378I$		
$u = 0.29268 + 1.46125I$		
$a = -0.402718 - 0.591662I$	$-5.97166 + 5.43704I$	0
$b = 0.224404 + 0.986853I$		
$u = 0.29268 - 1.46125I$		
$a = -0.402718 + 0.591662I$	$-5.97166 - 5.43704I$	0
$b = 0.224404 - 0.986853I$		
$u = -0.33248 + 1.45296I$		
$a = -0.522607 + 0.612576I$	$-4.88626 - 11.41650I$	0
$b = 0.276570 - 1.013290I$		
$u = -0.33248 - 1.45296I$		
$a = -0.522607 - 0.612576I$	$-4.88626 + 11.41650I$	0
$b = 0.276570 + 1.013290I$		
$u = -0.23283 + 1.49322I$		
$a = -0.434106 + 0.048242I$	$-10.62360 - 7.05864I$	0
$b = -1.39371 + 0.24719I$		
$u = -0.23283 - 1.49322I$		
$a = -0.434106 - 0.048242I$	$-10.62360 + 7.05864I$	0
$b = -1.39371 - 0.24719I$		
$u = 0.27946 + 1.48522I$		
$a = -0.35493 - 1.59998I$	$-9.78659 + 10.13180I$	0
$b = -1.116750 + 0.624358I$		
$u = 0.27946 - 1.48522I$		
$a = -0.35493 + 1.59998I$	$-9.78659 - 10.13180I$	0
$b = -1.116750 - 0.624358I$		
$u = -0.23041 + 1.49769I$		
$a = -0.41694 + 1.47941I$	$-10.65950 - 4.06737I$	0
$b = -1.150690 - 0.589914I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.23041 - 1.49769I$ $a = -0.41694 - 1.47941I$ $b = -1.150690 + 0.589914I$	$-10.65950 + 4.06737I$	0
$u = 0.17781 + 1.50580I$ $a = -0.493571 + 0.136163I$ $b = -1.372600 - 0.289952I$	$-11.32570 + 0.98821I$	0
$u = 0.17781 - 1.50580I$ $a = -0.493571 - 0.136163I$ $b = -1.372600 + 0.289952I$	$-11.32570 - 0.98821I$	0
$u = 0.18673 + 1.51693I$ $a = 0.937998 + 0.821389I$ $b = 1.147980 - 0.495591I$	$-6.13141 + 6.86398I$	0
$u = 0.18673 - 1.51693I$ $a = 0.937998 - 0.821389I$ $b = 1.147980 + 0.495591I$	$-6.13141 - 6.86398I$	0
$u = -0.38259 + 1.49851I$ $a = 0.59734 - 1.46380I$ $b = 1.236450 + 0.623365I$	$-7.8475 - 17.3020I$	0
$u = -0.38259 - 1.49851I$ $a = 0.59734 + 1.46380I$ $b = 1.236450 - 0.623365I$	$-7.8475 + 17.3020I$	0
$u = -0.437376 + 0.101038I$ $a = -1.72342 - 0.02563I$ $b = 0.743247 - 0.727481I$	$3.35868 + 4.45930I$	$11.81530 - 5.58434I$
$u = -0.437376 - 0.101038I$ $a = -1.72342 + 0.02563I$ $b = 0.743247 + 0.727481I$	$3.35868 - 4.45930I$	$11.81530 + 5.58434I$
$u = 0.35136 + 1.52269I$ $a = 0.61315 + 1.32966I$ $b = 1.237220 - 0.593339I$	$-9.0801 + 11.1134I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.35136 - 1.52269I$ $a = 0.61315 - 1.32966I$ $b = 1.237220 + 0.593339I$	$-9.0801 - 11.1134I$	0
$u = 0.372232$ $a = 0.631357$ $b = 0.140150$	0.703212	14.5110
$u = -0.168382 + 0.282817I$ $a = -0.07085 + 2.51635I$ $b = -0.931838 - 0.189422I$	$-1.65732 - 0.64432I$	$-2.89537 + 1.61582I$
$u = -0.168382 - 0.282817I$ $a = -0.07085 - 2.51635I$ $b = -0.931838 + 0.189422I$	$-1.65732 + 0.64432I$	$-2.89537 - 1.61582I$
$u = -0.05157 + 1.68989I$ $a = 0.526136 + 0.107090I$ $b = 1.092650 - 0.236274I$	$-13.14570 + 3.76638I$	0
$u = -0.05157 - 1.68989I$ $a = 0.526136 - 0.107090I$ $b = 1.092650 + 0.236274I$	$-13.14570 - 3.76638I$	0
$u = 0.13501 + 1.69283I$ $a = 0.505949 + 0.016872I$ $b = 1.038160 + 0.196931I$	$-12.85800 + 2.90129I$	0
$u = 0.13501 - 1.69283I$ $a = 0.505949 - 0.016872I$ $b = 1.038160 - 0.196931I$	$-12.85800 - 2.90129I$	0
$u = -0.146371 + 0.249725I$ $a = 2.79586 - 1.02647I$ $b = 0.902300 + 0.690824I$	$2.91057 - 0.92428I$	$11.94422 + 0.25513I$
$u = -0.146371 - 0.249725I$ $a = 2.79586 + 1.02647I$ $b = 0.902300 - 0.690824I$	$2.91057 + 0.92428I$	$11.94422 - 0.25513I$

$$\text{II. } I_2^u = \langle 1878a^5u - 2600a^4u + \cdots + 23830a - 8647, 3a^5u - 7a^4u + \cdots + 5a^2 + 2a, u^2 + 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} a \\ -0.313575a^5u + 0.434129a^4u + \cdots - 3.97896a + 1.44381 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.313575a^5u + 0.434129a^4u + \cdots - 2.97896a + 1.44381 \\ -0.313575a^5u + 0.434129a^4u + \cdots - 3.97896a + 1.44381 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.230422a^5u + 0.782267a^4u + \cdots - 1.18901a + 0.965103 \\ 0.165136a^5u - 0.977292a^4u + \cdots + 0.0687928a + 1.64168 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.230422a^5u + 0.782267a^4u + \cdots - 1.18901a + 0.965103 \\ 0.227918a^5u - 0.654199a^4u + \cdots + 1.66522a + 0.175822 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.183336a^5u + 0.225413a^4u + \cdots + 3.74169a - 0.115712 \\ 0.478711a^5u - 1.41142a^4u + \cdots + 4.04775a - 0.802137 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -0.0719653a^5u + 0.813157a^4u + \cdots + 0.816330a + 0.315913 \\ -0.231758a^5u + 0.583904a^4u + \cdots - 0.201703a - 0.493071 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -0.230422a^5u + 0.782267a^4u + \cdots - 1.18901a + 0.965103 \\ 0.458340a^5u - 1.43647a^4u + \cdots + 2.85423a - 0.789280 \end{pmatrix}$$

(ii) Obstruction class = 1

$$\text{(iii) Cusp Shapes} = -\frac{5788}{5989}a^5u - \frac{14428}{5989}a^5 - \frac{9080}{5989}a^4u + \frac{73372}{5989}a^4 + \frac{59108}{5989}a^3u - \frac{39572}{5989}a^3 + \frac{20364}{5989}a^2u + \frac{72864}{5989}a^2 + \frac{29264}{5989}au - \frac{114876}{5989}a - \frac{34044}{5989}u + \frac{50976}{5989}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$(u^3 - u^2 + 2u - 1)^4$
$c_2$	$(u^3 + u^2 - 1)^4$
$c_3, c_8$	$(u^6 - 3u^4 + 2u^2 + 1)^2$
$c_4$	$(u^3 - u^2 + 1)^4$
$c_5, c_6, c_9$	$(u^2 + 1)^6$
$c_7, c_{11}$	$(u^4 - u^2 + 1)^3$
$c_{10}$	$(u^2 + u + 1)^6$
$c_{12}$	$(u^2 - u + 1)^6$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^3 + 3y^2 + 2y - 1)^4$
$c_2, c_4$	$(y^3 - y^2 + 2y - 1)^4$
$c_3, c_8$	$(y^3 - 3y^2 + 2y + 1)^4$
$c_5, c_6, c_9$	$(y + 1)^{12}$
$c_7, c_{11}$	$(y^2 - y + 1)^6$
$c_{10}, c_{12}$	$(y^2 + y + 1)^6$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.000000I$ $a = -0.450984 + 1.062990I$ $b = 0.877439 - 0.744862I$	$1.37919 + 0.79824I$	$5.50976 + 0.48465I$
$u = 1.000000I$ $a = 0.696107 - 0.426734I$ $b = 0.877439 + 0.744862I$	$1.37919 - 0.79824I$	$5.50976 - 0.48465I$
$u = 1.000000I$ $a = -0.258387 - 1.162360I$ $b = -0.754878$	$-2.75839 - 2.02988I$	$-1.01951 + 3.46410I$
$u = 1.000000I$ $a = 0.111295 - 1.400630I$ $b = 0.877439 + 0.744862I$	$1.37919 - 4.85801I$	$5.50976 + 6.44355I$
$u = 1.000000I$ $a = 0.133827 + 0.089093I$ $b = 0.877439 - 0.744862I$	$1.37919 + 4.85801I$	$5.50976 - 6.44355I$
$u = 1.000000I$ $a = 3.76814 - 1.16236I$ $b = -0.754878$	$-2.75839 + 2.02988I$	$-1.01951 - 3.46410I$
$u = -1.000000I$ $a = -0.450984 - 1.062990I$ $b = 0.877439 + 0.744862I$	$1.37919 - 0.79824I$	$5.50976 - 0.48465I$
$u = -1.000000I$ $a = 0.696107 + 0.426734I$ $b = 0.877439 - 0.744862I$	$1.37919 + 0.79824I$	$5.50976 + 0.48465I$
$u = -1.000000I$ $a = -0.258387 + 1.162360I$ $b = -0.754878$	$-2.75839 + 2.02988I$	$-1.01951 - 3.46410I$
$u = -1.000000I$ $a = 0.111295 + 1.400630I$ $b = 0.877439 - 0.744862I$	$1.37919 + 4.85801I$	$5.50976 - 6.44355I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.000000I$		
$a = 0.133827 - 0.089093I$	$1.37919 - 4.85801I$	$5.50976 + 6.44355I$
$b = 0.877439 + 0.744862I$		
$u = -1.000000I$		
$a = 3.76814 + 1.16236I$	$-2.75839 - 2.02988I$	$-1.01951 + 3.46410I$
$b = -0.754878$		

$$\text{III. } I_3^u = \langle b + 1, -u^3 - u^2 + a - 3u - 2, u^5 + u^4 + 4u^3 + 3u^2 + 3u + 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^3 + u^2 + 3u + 2 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^3 + u^2 + 3u + 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^3 + u^2 + 3u + 2 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^2 + 1 \\ -u^4 - 2u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^2 - 1 \\ -u^2 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $4u^4 + 5u^3 + 12u^2 + 16u + 8$

(iv) **u**-Polynomials at the component

Crossings	<b>u</b> -Polynomials at each crossing
$c_1, c_2$	$(u - 1)^5$
$c_3, c_8$	$u^5$
$c_4$	$(u + 1)^5$
$c_5, c_6, c_{10}$	$u^5 + u^4 + 4u^3 + 3u^2 + 3u + 1$
$c_7$	$u^5 + u^4 - u^2 + u + 1$
$c_9, c_{12}$	$u^5 - u^4 + 4u^3 - 3u^2 + 3u - 1$
$c_{11}$	$u^5 - u^4 + u^2 + u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y - 1)^5$
$c_3, c_8$	$y^5$
$c_5, c_6, c_9$ $c_{10}, c_{12}$	$y^5 + 7y^4 + 16y^3 + 13y^2 + 3y - 1$
$c_7, c_{11}$	$y^5 - y^4 + 4y^3 - 3y^2 + 3y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.233677 + 0.885557I$ $a = 1.10636 + 1.69341I$ $b = -1.00000$	$-3.46474 - 2.21397I$	$-0.36497 + 8.87119I$
$u = -0.233677 - 0.885557I$ $a = 1.10636 - 1.69341I$ $b = -1.00000$	$-3.46474 + 2.21397I$	$-0.36497 - 8.87119I$
$u = -0.416284$ $a = 0.852303$ $b = -1.00000$	$-0.762751$	$3.17840$
$u = -0.05818 + 1.69128I$ $a = -0.532511 + 0.056433I$ $b = -1.00000$	$-12.60320 - 3.33174I$	$7.77577 + 5.09400I$
$u = -0.05818 - 1.69128I$ $a = -0.532511 - 0.056433I$ $b = -1.00000$	$-12.60320 + 3.33174I$	$7.77577 - 5.09400I$

#### IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u-1)^5)(u^3-u^2+2u-1)^4(u^{100}+50u^{99}+\dots+79u+1)$
$c_2$	$((u-1)^5)(u^3+u^2-1)^4(u^{100}-10u^{99}+\dots+11u-1)$
$c_3, c_8$	$u^5(u^6-3u^4+2u^2+1)^2(u^{100}+u^{99}+\dots+224u+32)$
$c_4$	$((u+1)^5)(u^3-u^2+1)^4(u^{100}-10u^{99}+\dots+11u-1)$
$c_5, c_6$	$((u^2+1)^6)(u^5+u^4+\dots+3u+1)(u^{100}+2u^{99}+\dots-329u-49)$
$c_7$	$((u^4-u^2+1)^3)(u^5+u^4-u^2+u+1)(u^{100}+2u^{99}+\dots-15u-17)$
$c_9$	$((u^2+1)^6)(u^5-u^4+\dots+3u-1)(u^{100}+2u^{99}+\dots-329u-49)$
$c_{10}$	$(u^2+u+1)^6(u^5+u^4+4u^3+3u^2+3u+1)$ $\cdot (u^{100}-32u^{99}+\dots+149u+289)$
$c_{11}$	$((u^4-u^2+1)^3)(u^5-u^4+u^2+u-1)(u^{100}+2u^{99}+\dots-15u-17)$
$c_{12}$	$(u^2-u+1)^6(u^5-u^4+4u^3-3u^2+3u-1)$ $\cdot (u^{100}-32u^{99}+\dots+149u+289)$



### V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y-1)^5)(y^3+3y^2+2y-1)^4(y^{100}+10y^{99}+\dots-2487y+1)$
$c_2, c_4$	$((y-1)^5)(y^3-y^2+2y-1)^4(y^{100}-50y^{99}+\dots-79y+1)$
$c_3, c_8$	$y^5(y^3-3y^2+2y+1)^4(y^{100}-45y^{99}+\dots-52736y+1024)$
$c_5, c_6, c_9$	$(y+1)^{12}(y^5+7y^4+16y^3+13y^2+3y-1)$ $\cdot (y^{100}+98y^{99}+\dots+34251y+2401)$
$c_7, c_{11}$	$(y^2-y+1)^6(y^5-y^4+4y^3-3y^2+3y-1)$ $\cdot (y^{100}-32y^{99}+\dots+149y+289)$
$c_{10}, c_{12}$	$(y^2+y+1)^6(y^5+7y^4+16y^3+13y^2+3y-1)$ $\cdot (y^{100}+80y^{99}+\dots-3531239y+83521)$