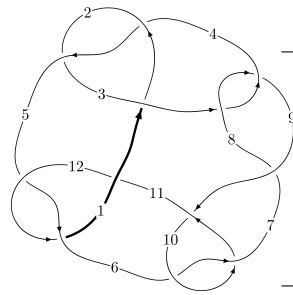
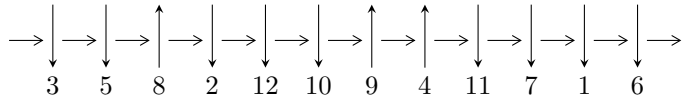


12a<sub>0119</sub> (K12a<sub>0119</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$3,8 \xrightarrow{c_3} 4 \xrightarrow{c_8} 5,9 \xrightarrow{c_2} 2 \xrightarrow{c_1} 1,11 \xrightarrow{c_{11}} 12 \xrightarrow{c_7} 7 \xrightarrow{c_{10}} 10 \xrightarrow{c_6} 6 \longrightarrow c_4, c_5, c_9, c_{12}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

$$\begin{aligned}
I_1^u &= \langle 2u^{13} - u^{11} + 2u^{10} + 5u^9 + 2u^8 + 2u^7 - 4u^6 + 3u^5 + 2u^4 - 2u^3 - 12u^2 + 4d - 8u - 8, \\
&\quad - u^{13} + u^{11} - u^{10} - 4u^9 + u^8 + u^7 - 4u^5 - u^4 + 2u^3 + 8u^2 + 4c + 4, \\
&\quad - u^{13} + u^{11} - u^{10} - 3u^9 + u^7 + u^6 - 2u^5 - u^4 + 2u^3 + 6u^2 + 2b + 2u + 2, \\
&\quad 3u^{13} - 2u^{11} + 3u^{10} + 9u^9 + u^8 - u^7 - 4u^6 + 7u^5 + 3u^4 - 6u^3 - 18u^2 + 4a - 8u - 12, \\
&\quad u^{14} - u^{13} - u^{12} + 2u^{11} + 2u^{10} - 3u^9 - u^8 - u^7 + 4u^6 - u^5 - 4u^4 - 4u^3 + 4u^2 + 4 \rangle \\
I_2^u &= \langle -3u^{21} + 9u^{19} + \dots + 4d + 4, -2u^{22} + 6u^{20} + \dots + 4c - 2, \\
&\quad - u^{16} + 2u^{14} - 5u^{12} + 6u^{10} - u^9 - 6u^8 + u^7 + 4u^6 - 4u^5 - u^4 + 3u^3 - 4u^2 + 2b - 2u, \\
&\quad - 2u^{21} + 4u^{20} + \dots + 4a + 6, u^{23} - 2u^{22} + \dots + 2u - 2 \rangle \\
I_3^u &= \langle -3u^{21} + 9u^{19} + \dots + 4d + 4, -2u^{22} + 6u^{20} + \dots + 4c - 2, 2u^{22} - 2u^{21} + \dots + 4b + 2, \\
&\quad - 2u^{22} + u^{21} + \dots + 4a - 6, u^{23} - 2u^{22} + \dots + 2u - 2 \rangle \\
I_4^u &= \langle -2u^{22} + 3u^{21} + \dots + 4d + 10u, u^{19} - 2u^{17} + \dots + 4c + 4, 2u^{22} - 2u^{21} + \dots + 4b + 2, \\
&\quad - 2u^{22} + u^{21} + \dots + 4a - 6, u^{23} - 2u^{22} + \dots + 2u - 2 \rangle \\
I_5^u &= \langle -a^2u^2c - u^2ca + 2a^2u^2 - a^2c + 2cau + 2u^2a + 4ca - 3cu + au - u^2 + d - 4c - 5a + u + 3, \\
&\quad a^2u^2c - a^2cu + 3u^2ca - 2a^2u^2 - a^2c + 4cau - 2u^2c - u^2a + c^2 - ca - 2cu + 2a^2 - 5au + 2a + 3u - 1, \\
&\quad - a^2u^2 + b + 2a - 2, a^3 - 2a^2u - 2a^2 + 3au + 3a - u - 1, u^3 + u^2 - 1 \rangle
\end{aligned}$$

$$\begin{aligned}
I_1^v &= \langle a, d, c + 1, b - 1, v + 1 \rangle \\
I_2^v &= \langle c, d + 1, b, a - 1, v + 1 \rangle \\
I_3^v &= \langle a, d + 1, c + a, b - 1, v + 1 \rangle \\
I_4^v &= \langle a, da - c + 1, dv - 1, cv - a - v, b - 1 \rangle
\end{aligned}$$

\* 8 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 104 representations.

\* 1 irreducible components of  $\dim_{\mathbb{C}} = 1$

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<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle 2u^{13} - u^{11} + \dots + 4d - 8, -u^{13} + u^{11} + \dots + 4c + 4, -u^{13} + u^{11} + \dots + 2b + 2, 3u^{13} - 2u^{11} + \dots + 4a - 12, u^{14} - u^{13} + \dots + 4u^2 + 4 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -\frac{3}{4}u^{13} + \frac{1}{2}u^{11} + \dots + 2u + 3 \\ \frac{1}{2}u^{13} - \frac{1}{2}u^{11} + \dots - u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -\frac{3}{4}u^{13} + \frac{1}{2}u^{11} + \dots + 2u + 3 \\ \frac{1}{2}u^{13} - \frac{1}{4}u^{11} + \dots - 2u - 2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -\frac{1}{4}u^{13} + \frac{1}{4}u^{11} + \dots + \frac{3}{2}u^2 + 1 \\ \frac{1}{2}u^{13} - \frac{1}{4}u^{11} + \dots - 2u - 2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} \frac{1}{4}u^{13} - \frac{1}{4}u^{11} + \dots - 2u^2 - 1 \\ -\frac{1}{2}u^{13} + \frac{1}{4}u^{11} + \dots + 2u + 2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} \frac{1}{2}u^{13} - \frac{1}{2}u^{11} + \dots - u - 2 \\ -\frac{1}{2}u^{13} - \frac{1}{2}u^{10} + \dots + 2u + 2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^3 \\ u^5 - u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -\frac{1}{4}u^{13} + \frac{1}{4}u^{11} + \dots + 2u + 1 \\ \frac{1}{4}u^{11} - \frac{1}{4}u^9 + \dots - \frac{3}{2}u^3 + u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -\frac{3}{4}u^{13} + \frac{1}{2}u^{11} + \dots + 2u + 3 \\ \frac{1}{2}u^{13} - \frac{1}{2}u^{11} + \dots - u - 1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= -3u^{13} - u^{12} + u^{11} - 2u^{10} - 8u^9 - 5u^8 - 3u^7 + 7u^6 - 2u^5 - 7u^4 + 4u^3 + 22u^2 + 16u + 10$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_9, c_{11}$	$u^{14} + 7u^{13} + \dots + 3u + 1$
$c_2, c_4, c_5$ $c_6, c_{10}, c_{12}$	$u^{14} - u^{13} + \dots + u + 1$
$c_3, c_8$	$u^{14} + u^{13} + \dots + 4u^2 + 4$
$c_7$	$u^{14} - 3u^{13} + \dots + 32u + 16$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_9, c_{11}$	$y^{14} + 5y^{13} + \dots + 9y + 1$
$c_2, c_4, c_5$ $c_6, c_{10}, c_{12}$	$y^{14} - 7y^{13} + \dots - 3y + 1$
$c_3, c_8$	$y^{14} - 3y^{13} + \dots + 32y + 16$
$c_7$	$y^{14} + 9y^{13} + \dots - 1536y + 256$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.351654 + 0.974470I$ $a = 0.484407 + 0.125788I$ $b = 0.933970 - 0.502203I$ $c = 0.065921 - 0.250683I$ $d = -0.762746 - 0.668204I$	$-2.00841 + 5.97343I$	$-8.41754 - 8.60965I$
$u = -0.351654 - 0.974470I$ $a = 0.484407 - 0.125788I$ $b = 0.933970 + 0.502203I$ $c = 0.065921 + 0.250683I$ $d = -0.762746 + 0.668204I$	$-2.00841 - 5.97343I$	$-8.41754 + 8.60965I$
$u = -0.915559 + 0.598258I$ $a = 0.664888 - 0.608266I$ $b = -0.181237 + 0.749038I$ $c = -1.159390 + 0.550105I$ $d = -0.936616 - 0.512222I$	$0.94494 - 2.29172I$	$-1.04510 + 1.71019I$
$u = -0.915559 - 0.598258I$ $a = 0.664888 + 0.608266I$ $b = -0.181237 - 0.749038I$ $c = -1.159390 - 0.550105I$ $d = -0.936616 + 0.512222I$	$0.94494 + 2.29172I$	$-1.04510 - 1.71019I$
$u = 1.120580 + 0.015323I$ $a = 0.577432 - 1.267280I$ $b = -0.702265 + 0.653431I$ $c = 0.530358 + 0.435838I$ $d = -0.072651 - 0.949218I$	$4.01770 + 3.65190I$	$-0.27967 - 6.51151I$
$u = 1.120580 - 0.015323I$ $a = 0.577432 + 1.267280I$ $b = -0.702265 - 0.653431I$ $c = 0.530358 - 0.435838I$ $d = -0.072651 + 0.949218I$	$4.01770 - 3.65190I$	$-0.27967 + 6.51151I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.145230 + 0.485598I$ $a = -0.08828 + 1.64061I$ $b = -1.032700 - 0.607770I$ $c = 0.834303 + 0.325183I$ $d = -0.546866 - 0.244514I$	$0.82935 - 11.25490I$	$-6.02298 + 10.89166I$
$u = -1.145230 - 0.485598I$ $a = -0.08828 - 1.64061I$ $b = -1.032700 + 0.607770I$ $c = 0.834303 - 0.325183I$ $d = -0.546866 + 0.244514I$	$0.82935 + 11.25490I$	$-6.02298 - 10.89166I$
$u = -0.065300 + 0.726861I$ $a = 0.634835 - 0.129477I$ $b = 0.512305 + 0.308441I$ $c = -0.117499 + 0.636011I$ $d = 0.171343 + 0.691065I$	$-0.66587 - 1.25835I$	$-4.79341 + 6.11957I$
$u = -0.065300 - 0.726861I$ $a = 0.634835 + 0.129477I$ $b = 0.512305 - 0.308441I$ $c = -0.117499 - 0.636011I$ $d = 0.171343 - 0.691065I$	$-0.66587 + 1.25835I$	$-4.79341 - 6.11957I$
$u = 0.800659 + 0.997483I$ $a = 0.429409 - 0.097928I$ $b = 1.213650 + 0.504832I$ $c = -0.65473 - 1.70324I$ $d = -2.26378 - 1.40323I$	$-9.38350 - 10.57210I$	$-12.21836 + 7.10513I$
$u = 0.800659 - 0.997483I$ $a = 0.429409 + 0.097928I$ $b = 1.213650 - 0.504832I$ $c = -0.65473 + 1.70324I$ $d = -2.26378 + 1.40323I$	$-9.38350 + 10.57210I$	$-12.21836 - 7.10513I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.056500 + 0.850786I$ $a = -0.70270 - 1.54576I$ $b = -1.243720 + 0.536134I$ $c = -1.99896 - 0.54543I$ $d = -2.08869 + 1.91409I$	$-8.5386 + 17.3286I$	$-11.2229 - 10.7940I$
$u = 1.056500 - 0.850786I$ $a = -0.70270 + 1.54576I$ $b = -1.243720 - 0.536134I$ $c = -1.99896 + 0.54543I$ $d = -2.08869 - 1.91409I$	$-8.5386 - 17.3286I$	$-11.2229 + 10.7940I$



$$\text{II. } I_2^u = \langle -3u^{21} + 9u^{19} + \dots + 4d + 4, -2u^{22} + 6u^{20} + \dots + 4c - 2, -u^{16} + 2u^{14} + \dots + 2b - 2u, -2u^{21} + 4u^{20} + \dots + 4a + 6, u^{23} - 2u^{22} + \dots + 2u - 2 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_3 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_5 &= \begin{pmatrix} \frac{1}{2}u^{21} - u^{20} + \dots + 5u - \frac{3}{2} \\ \frac{1}{2}u^{16} - u^{14} + \dots + 2u^2 + u \end{pmatrix} \\ a_9 &= \begin{pmatrix} u \\ -u^3 + u \end{pmatrix} \\ a_2 &= \begin{pmatrix} \frac{1}{2}u^{21} - u^{20} + \dots + 5u - \frac{3}{2} \\ -\frac{1}{4}u^{18} + \frac{1}{2}u^{16} + \dots - u^3 - 1 \end{pmatrix} \\ a_1 &= \begin{pmatrix} \frac{1}{2}u^{21} - u^{20} + \dots + 5u - \frac{5}{2} \\ -\frac{1}{4}u^{18} + \frac{1}{2}u^{16} + \dots - u^3 - 1 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} \frac{1}{2}u^{22} - \frac{3}{2}u^{20} + \dots - \frac{1}{2}u + \frac{1}{2} \\ \frac{3}{4}u^{21} - \frac{9}{4}u^{19} + \dots + \frac{1}{2}u - 1 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -\frac{1}{2}u^{21} + u^{20} + \dots - \frac{9}{2}u + 2 \\ 1 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -u^3 \\ u^5 - u^3 + u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} \frac{1}{4}u^{18} - \frac{3}{4}u^{16} + \dots + \frac{1}{2}u + \frac{1}{2} \\ \frac{1}{4}u^{18} - \frac{1}{2}u^{16} + \dots - u^3 + u \end{pmatrix} \\ a_6 &= \begin{pmatrix} -\frac{1}{2}u^{22} + \frac{3}{4}u^{21} + \dots + u - \frac{3}{2} \\ -\frac{1}{2}u^{22} + \frac{1}{4}u^{21} + \dots + u - \frac{1}{2} \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= 2u^{22} - 6u^{20} + 4u^{19} + 14u^{18} - 8u^{17} - 20u^{16} + 22u^{15} + 20u^{14} - 28u^{13} - 6u^{12} + 34u^{11} - 6u^{10} - 28u^9 + 36u^8 + 10u^7 - 30u^6 + 26u^5 + 10u^4 - 10u^3 + 10u^2 + 4u - 8$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{23} + 14u^{22} + \dots + 24u + 16$
$c_2, c_4$	$u^{23} - 7u^{21} + \dots - 3u^2 + 4$
$c_3, c_8$	$u^{23} + 2u^{22} + \dots + 2u + 2$
$c_5, c_6, c_{10}$ $c_{12}$	$u^{23} - 2u^{22} + \dots + 3u - 1$
$c_7$	$u^{23} - 6u^{22} + \dots + 8u - 4$
$c_9, c_{11}$	$u^{23} + 12u^{22} + \dots + 7u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{23} - 14y^{22} + \dots - 736y - 256$
$c_2, c_4$	$y^{23} - 14y^{22} + \dots + 24y - 16$
$c_3, c_8$	$y^{23} - 6y^{22} + \dots + 8y - 4$
$c_5, c_6, c_{10}$ $c_{12}$	$y^{23} - 12y^{22} + \dots + 7y - 1$
$c_7$	$y^{23} + 18y^{22} + \dots - 8y - 16$
$c_9, c_{11}$	$y^{23} + 32y^{21} + \dots + 31y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.694668 + 0.784847I$		
$a = 0.450244 - 0.080442I$		
$b = 1.152320 + 0.384542I$	$-2.86000 - 1.29238I$	$-6.06322 + 0.45977I$
$c = 0.782630 + 0.951667I$		
$d = 1.54383 + 0.54732I$		
$u = 0.694668 - 0.784847I$		
$a = 0.450244 + 0.080442I$		
$b = 1.152320 - 0.384542I$	$-2.86000 + 1.29238I$	$-6.06322 - 0.45977I$
$c = 0.782630 - 0.951667I$		
$d = 1.54383 - 0.54732I$		
$u = -0.892323 + 0.293165I$		
$a = 0.438777 + 0.026420I$		
$b = 1.270830 - 0.136735I$	$-3.02064 - 3.59706I$	$-7.24355 + 7.79597I$
$c = 0.009889 - 0.214450I$		
$d = -0.224788 - 1.053390I$		
$u = -0.892323 - 0.293165I$		
$a = 0.438777 - 0.026420I$		
$b = 1.270830 + 0.136735I$	$-3.02064 + 3.59706I$	$-7.24355 - 7.79597I$
$c = 0.009889 + 0.214450I$		
$d = -0.224788 + 1.053390I$		
$u = -1.095410 + 0.175785I$		
$a = 0.45789 + 1.51421I$		
$b = -0.817025 - 0.605081I$	$3.68412 - 1.20490I$	$-0.197865 + 0.587959I$
$c = -0.908669 - 0.269252I$		
$d = 0.299223 + 0.396395I$		
$u = -1.095410 - 0.175785I$		
$a = 0.45789 - 1.51421I$		
$b = -0.817025 + 0.605081I$	$3.68412 + 1.20490I$	$-0.197865 - 0.587959I$
$c = -0.908669 + 0.269252I$		
$d = 0.299223 - 0.396395I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.159876 + 0.866608I$ $a = 0.607182 + 0.204119I$ $b = 0.479725 - 0.497445I$ $c = -0.128604 + 0.305274I$ $d = 0.691140 + 0.217382I$	$-0.79201 - 1.83570I$	$-5.62427 + 3.60335I$
$u = 0.159876 - 0.866608I$ $a = 0.607182 - 0.204119I$ $b = 0.479725 + 0.497445I$ $c = -0.128604 - 0.305274I$ $d = 0.691140 - 0.217382I$	$-0.79201 + 1.83570I$	$-5.62427 - 3.60335I$
$u = 1.115790 + 0.351606I$ $a = 0.621931 + 0.844762I$ $b = -0.434825 - 0.767671I$ $c = -0.374060 + 0.344406I$ $d = 0.457120 - 0.806395I$	$2.56195 + 6.12354I$	$-2.77038 - 6.59776I$
$u = 1.115790 - 0.351606I$ $a = 0.621931 - 0.844762I$ $b = -0.434825 + 0.767671I$ $c = -0.374060 - 0.344406I$ $d = 0.457120 + 0.806395I$	$2.56195 - 6.12354I$	$-2.77038 + 6.59776I$
$u = 0.810032 + 0.844947I$ $a = -1.09305 - 1.85522I$ $b = -1.235740 + 0.400126I$ $c = -1.17221 - 1.42613I$ $d = -1.79180 - 0.10501I$	$-10.13410 - 1.43226I$	$-13.58922 + 0.72835I$
$u = 0.810032 - 0.844947I$ $a = -1.09305 + 1.85522I$ $b = -1.235740 - 0.400126I$ $c = -1.17221 + 1.42613I$ $d = -1.79180 + 0.10501I$	$-10.13410 + 1.43226I$	$-13.58922 - 0.72835I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.746640 + 0.934392I$ $a = 0.575739 - 0.436897I$ $b = 0.102199 + 0.836400I$ $c = 0.76290 - 1.40128I$ $d = 1.61980 - 0.96664I$	$-6.07831 + 5.69706I$	$-9.37968 - 4.06061I$
$u = -0.746640 - 0.934392I$ $a = 0.575739 + 0.436897I$ $b = 0.102199 - 0.836400I$ $c = 0.76290 + 1.40128I$ $d = 1.61980 + 0.96664I$	$-6.07831 - 5.69706I$	$-9.37968 + 4.06061I$
$u = 1.001420 + 0.725291I$ $a = -0.59194 - 1.76529I$ $b = -1.170750 + 0.509221I$ $c = 1.41858 + 0.76507I$ $d = 1.50027 - 1.14883I$	$-1.95175 + 7.00485I$	$-4.95661 - 5.13787I$
$u = 1.001420 - 0.725291I$ $a = -0.59194 + 1.76529I$ $b = -1.170750 - 0.509221I$ $c = 1.41858 - 0.76507I$ $d = 1.50027 + 1.14883I$	$-1.95175 - 7.00485I$	$-4.95661 + 5.13787I$
$u = 0.966403 + 0.788262I$ $a = 0.422604 - 0.071283I$ $b = 1.300820 + 0.388090I$ $c = -1.60031 - 0.73645I$ $d = -2.06235 + 0.58473I$	$-9.64490 + 7.52364I$	$-12.34364 - 6.02284I$
$u = 0.966403 - 0.788262I$ $a = 0.422604 + 0.071283I$ $b = 1.300820 - 0.388090I$ $c = -1.60031 + 0.73645I$ $d = -2.06235 - 0.58473I$	$-9.64490 - 7.52364I$	$-12.34364 + 6.02284I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.040150 + 0.798969I$ $a = 0.541562 - 0.570958I$ $b = -0.125501 + 0.921967I$ $c = 1.77993 - 0.50191I$ $d = 1.69909 + 1.34789I$	$-5.14546 - 12.07470I$	$-8.17479 + 8.06520I$
$u = -1.040150 - 0.798969I$ $a = 0.541562 + 0.570958I$ $b = -0.125501 - 0.921967I$ $c = 1.77993 + 0.50191I$ $d = 1.69909 - 1.34789I$	$-5.14546 + 12.07470I$	$-8.17479 - 8.06520I$
$u = 0.598117$ $a = 0.466081$ $b = 1.14555$ $c = 0.628003$ $d = 0.737621$	$-2.27356$	$-1.62820$
$u = -0.272723 + 0.504579I$ $a = -4.66398 + 5.23784I$ $b = -1.094820 - 0.106487I$ $c = 1.115910 + 0.788549I$ $d = -0.100347 + 0.172505I$	$-4.96054 + 0.60932I$	$-15.8427 - 0.8440I$
$u = -0.272723 - 0.504579I$ $a = -4.66398 - 5.23784I$ $b = -1.094820 + 0.106487I$ $c = 1.115910 - 0.788549I$ $d = -0.100347 - 0.172505I$	$-4.96054 - 0.60932I$	$-15.8427 + 0.8440I$

III.  $I_3^u = \langle -3u^{21} + 9u^{19} + \dots + 4d + 4, -2u^{22} + 6u^{20} + \dots + 4c - 2, 2u^{22} - 2u^{21} + \dots + 4b + 2, -2u^{22} + u^{21} + \dots + 4a - 6, u^{23} - 2u^{22} + \dots + 2u - 2 \rangle$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} \frac{1}{2}u^{22} - \frac{1}{4}u^{21} + \dots + \frac{1}{4}u^2 + \frac{3}{2} \\ -\frac{1}{2}u^{22} + \frac{1}{2}u^{21} + \dots - \frac{1}{4}u^2 - \frac{1}{2} \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} \frac{1}{2}u^{22} - \frac{1}{4}u^{21} + \dots + \frac{1}{4}u^2 + \frac{3}{2} \\ \frac{1}{4}u^{21} - \frac{3}{4}u^{19} + \dots + \frac{1}{2}u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} \frac{1}{2}u^{22} - \frac{3}{2}u^{20} + \dots + \frac{1}{2}u + \frac{1}{2} \\ \frac{1}{4}u^{21} - \frac{3}{4}u^{19} + \dots + \frac{1}{2}u - 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} \frac{1}{2}u^{22} - \frac{3}{2}u^{20} + \dots - \frac{1}{2}u + \frac{1}{2} \\ \frac{3}{4}u^{21} - \frac{9}{4}u^{19} + \dots + \frac{1}{2}u - 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -\frac{1}{2}u^{22} + \frac{3}{2}u^{20} + \dots - \frac{5}{2}u^2 - \frac{1}{2}u \\ 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^3 \\ u^5 - u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} \frac{1}{4}u^{18} - \frac{3}{4}u^{16} + \dots + \frac{1}{2}u + \frac{1}{2} \\ \frac{1}{4}u^{18} - \frac{1}{2}u^{16} + \dots - u^3 + u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -\frac{1}{2}u^{22} + \frac{3}{4}u^{21} + \dots + u - \frac{3}{2} \\ -\frac{1}{2}u^{22} + \frac{1}{2}u^{21} + \dots + u - \frac{1}{2} \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= 2u^{22} - 6u^{20} + 4u^{19} + 14u^{18} - 8u^{17} - 20u^{16} + 22u^{15} + 20u^{14} - 28u^{13} - 6u^{12} + 34u^{11} - 6u^{10} - 28u^9 + 36u^8 + 10u^7 - 30u^6 + 26u^5 + 10u^4 - 10u^3 + 10u^2 + 4u - 8$$



(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_9$	$u^{23} + 12u^{22} + \dots + 7u + 1$
$c_2, c_4, c_6$ $c_{10}$	$u^{23} - 2u^{22} + \dots + 3u - 1$
$c_3, c_8$	$u^{23} + 2u^{22} + \dots + 2u + 2$
$c_5, c_{12}$	$u^{23} - 7u^{21} + \dots - 3u^2 + 4$
$c_7$	$u^{23} - 6u^{22} + \dots + 8u - 4$
$c_{11}$	$u^{23} + 14u^{22} + \dots + 24u + 16$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_9$	$y^{23} + 32y^{21} + \dots + 31y - 1$
$c_2, c_4, c_6$ $c_{10}$	$y^{23} - 12y^{22} + \dots + 7y - 1$
$c_3, c_8$	$y^{23} - 6y^{22} + \dots + 8y - 4$
$c_5, c_{12}$	$y^{23} - 14y^{22} + \dots + 24y - 16$
$c_7$	$y^{23} + 18y^{22} + \dots - 8y - 16$
$c_{11}$	$y^{23} - 14y^{22} + \dots - 736y - 256$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.694668 + 0.784847I$	$-2.86000 - 1.29238I$	$-6.06322 + 0.45977I$
$a = 0.646621 + 0.443219I$		
$b = 0.052166 - 0.721195I$		
$c = 0.782630 + 0.951667I$		
$d = 1.54383 + 0.54732I$		
$u = 0.694668 - 0.784847I$	$-2.86000 + 1.29238I$	$-6.06322 - 0.45977I$
$a = 0.646621 - 0.443219I$		
$b = 0.052166 + 0.721195I$		
$c = 0.782630 - 0.951667I$		
$d = 1.54383 - 0.54732I$		
$u = -0.892323 + 0.293165I$	$-3.02064 - 3.59706I$	$-7.24355 + 7.79597I$
$a = 0.52674 + 2.12395I$		
$b = -0.890003 - 0.443541I$		
$c = 0.009889 - 0.214450I$		
$d = -0.224788 - 1.053390I$		
$u = -0.892323 - 0.293165I$	$-3.02064 + 3.59706I$	$-7.24355 - 7.79597I$
$a = 0.52674 - 2.12395I$		
$b = -0.890003 + 0.443541I$		
$c = 0.009889 + 0.214450I$		
$d = -0.224788 + 1.053390I$		
$u = -1.095410 + 0.175785I$	$3.68412 - 1.20490I$	$-0.197865 + 0.587959I$
$a = 0.663876 - 1.020630I$		
$b = -0.552165 + 0.688491I$		
$c = -0.908669 - 0.269252I$		
$d = 0.299223 + 0.396395I$		
$u = -1.095410 - 0.175785I$	$3.68412 + 1.20490I$	$-0.197865 - 0.587959I$
$a = 0.663876 + 1.020630I$		
$b = -0.552165 - 0.688491I$		
$c = -0.908669 + 0.269252I$		
$d = 0.299223 - 0.396395I$		

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.159876 + 0.866608I$ $a = 0.531180 - 0.126379I$ $b = 0.781744 + 0.423915I$ $c = -0.128604 + 0.305274I$ $d = 0.691140 + 0.217382I$	$-0.79201 - 1.83570I$	$-5.62427 + 3.60335I$
$u = 0.159876 - 0.866608I$ $a = 0.531180 + 0.126379I$ $b = 0.781744 - 0.423915I$ $c = -0.128604 - 0.305274I$ $d = 0.691140 - 0.217382I$	$-0.79201 + 1.83570I$	$-5.62427 - 3.60335I$
$u = 1.115790 + 0.351606I$ $a = 0.15695 - 1.65297I$ $b = -0.943072 + 0.599566I$ $c = -0.374060 + 0.344406I$ $d = 0.457120 - 0.806395I$	$2.56195 + 6.12354I$	$-2.77038 - 6.59776I$
$u = 1.115790 - 0.351606I$ $a = 0.15695 + 1.65297I$ $b = -0.943072 - 0.599566I$ $c = -0.374060 - 0.344406I$ $d = 0.457120 + 0.806395I$	$2.56195 - 6.12354I$	$-2.77038 + 6.59776I$
$u = 0.810032 + 0.844947I$ $a = 0.435558 - 0.082401I$ $b = 1.216570 + 0.419344I$ $c = -1.17221 - 1.42613I$ $d = -1.79180 - 0.10501I$	$-10.13410 - 1.43226I$	$-13.58922 + 0.72835I$
$u = 0.810032 - 0.844947I$ $a = 0.435558 + 0.082401I$ $b = 1.216570 - 0.419344I$ $c = -1.17221 + 1.42613I$ $d = -1.79180 + 0.10501I$	$-10.13410 + 1.43226I$	$-13.58922 - 0.72835I$

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.746640 + 0.934392I$ $a = 0.438031 + 0.094410I$ $b = 1.181600 - 0.470208I$ $c = 0.76290 - 1.40128I$ $d = 1.61980 - 0.96664I$	$-6.07831 + 5.69706I$	$-9.37968 - 4.06061I$
$u = -0.746640 - 0.934392I$ $a = 0.438031 - 0.094410I$ $b = 1.181600 + 0.470208I$ $c = 0.76290 + 1.40128I$ $d = 1.61980 + 0.96664I$	$-6.07831 - 5.69706I$	$-9.37968 + 4.06061I$
$u = 1.001420 + 0.725291I$ $a = 0.578527 + 0.586894I$ $b = -0.148145 - 0.864175I$ $c = 1.41858 + 0.76507I$ $d = 1.50027 - 1.14883I$	$-1.95175 + 7.00485I$	$-4.95661 - 5.13787I$
$u = 1.001420 - 0.725291I$ $a = 0.578527 - 0.586894I$ $b = -0.148145 + 0.864175I$ $c = 1.41858 - 0.76507I$ $d = 1.50027 + 1.14883I$	$-1.95175 - 7.00485I$	$-4.95661 + 5.13787I$
$u = 0.966403 + 0.788262I$ $a = -0.73482 - 1.74058I$ $b = -1.205860 + 0.487616I$ $c = -1.60031 - 0.73645I$ $d = -2.06235 + 0.58473I$	$-9.64490 + 7.52364I$	$-12.34364 - 6.02284I$
$u = 0.966403 - 0.788262I$ $a = -0.73482 + 1.74058I$ $b = -1.205860 - 0.487616I$ $c = -1.60031 + 0.73645I$ $d = -2.06235 - 0.58473I$	$-9.64490 - 7.52364I$	$-12.34364 + 6.02284I$

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.040150 + 0.798969I$ $a = -0.65748 + 1.62443I$ $b = -1.214090 - 0.528949I$ $c = 1.77993 - 0.50191I$ $d = 1.69909 + 1.34789I$	$-5.14546 - 12.07470I$	$-8.17479 + 8.06520I$
$u = -1.040150 - 0.798969I$ $a = -0.65748 - 1.62443I$ $b = -1.214090 + 0.528949I$ $c = 1.77993 + 0.50191I$ $d = 1.69909 - 1.34789I$	$-5.14546 + 12.07470I$	$-8.17479 - 8.06520I$
$u = 0.598117$ $a = 1.80880$ $b = -0.447146$ $c = 0.628003$ $d = 0.737621$	$-2.27356$	$-1.62820$
$u = -0.272723 + 0.504579I$ $a = 0.510432 + 0.043771I$ $b = 0.944825 - 0.166773I$ $c = 1.115910 + 0.788549I$ $d = -0.100347 + 0.172505I$	$-4.96054 + 0.60932I$	$-15.8427 - 0.8440I$
$u = -0.272723 - 0.504579I$ $a = 0.510432 - 0.043771I$ $b = 0.944825 + 0.166773I$ $c = 1.115910 - 0.788549I$ $d = -0.100347 - 0.172505I$	$-4.96054 - 0.60932I$	$-15.8427 + 0.8440I$

IV.  $I_4^u = \langle -2u^{22} + 3u^{21} + \dots + 4d + 10u, u^{19} - 2u^{17} + \dots + 4c + 4, 2u^{22} - 2u^{21} + \dots + 4b + 2, -2u^{22} + u^{21} + \dots + 4a - 6, u^{23} - 2u^{22} + \dots + 2u - 2 \rangle$

(i) Arc colorings

$$\begin{aligned}
a_3 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\
a_8 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\
a_4 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\
a_5 &= \begin{pmatrix} \frac{1}{2}u^{22} - \frac{1}{4}u^{21} + \dots + \frac{1}{4}u^2 + \frac{3}{2} \\ -\frac{1}{2}u^{22} + \frac{1}{2}u^{21} + \dots - \frac{1}{4}u^2 - \frac{1}{2} \end{pmatrix} \\
a_9 &= \begin{pmatrix} u \\ -u^3 + u \end{pmatrix} \\
a_2 &= \begin{pmatrix} \frac{1}{2}u^{22} - \frac{1}{4}u^{21} + \dots + \frac{1}{4}u^2 + \frac{3}{2} \\ \frac{1}{4}u^{21} - \frac{3}{4}u^{19} + \dots + \frac{1}{2}u - 1 \end{pmatrix} \\
a_1 &= \begin{pmatrix} \frac{1}{2}u^{22} - \frac{3}{2}u^{20} + \dots + \frac{1}{2}u + \frac{1}{2} \\ \frac{1}{4}u^{21} - \frac{3}{4}u^{19} + \dots + \frac{1}{2}u - 1 \end{pmatrix} \\
a_{11} &= \begin{pmatrix} -\frac{1}{4}u^{19} + \frac{1}{2}u^{17} + \dots - 3u - 1 \\ \frac{1}{2}u^{22} - \frac{3}{4}u^{21} + \dots + 6u^2 - \frac{5}{2}u \end{pmatrix} \\
a_{12} &= \begin{pmatrix} -\frac{1}{2}u^{19} + u^{17} + \dots - \frac{7}{2}u - 1 \\ \frac{1}{2}u^{22} - \frac{1}{2}u^{21} + \dots + \frac{13}{2}u^2 - 3u \end{pmatrix} \\
a_7 &= \begin{pmatrix} -u^3 \\ u^5 - u^3 + u \end{pmatrix} \\
a_{10} &= \begin{pmatrix} -\frac{3}{4}u^{19} + \frac{3}{2}u^{17} + \dots - 3u - 1 \\ \frac{1}{2}u^{22} - \frac{1}{4}u^{21} + \dots + 7u^2 - \frac{5}{2}u \end{pmatrix} \\
a_6 &= \begin{pmatrix} \frac{1}{2}u^{22} - \frac{3}{4}u^{21} + \dots + \frac{1}{2}u + 1 \\ -\frac{1}{2}u^{21} + u^{20} + \dots - 3u - \frac{1}{2} \end{pmatrix}
\end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$\begin{aligned}
&= 2u^{22} - 6u^{20} + 4u^{19} + 14u^{18} - 8u^{17} - 20u^{16} + 22u^{15} + 20u^{14} - 28u^{13} - 6u^{12} + 34u^{11} - \\
&6u^{10} - 28u^9 + 36u^8 + 10u^7 - 30u^6 + 26u^5 + 10u^4 - 10u^3 + 10u^2 + 4u - 8
\end{aligned}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_{11}$	$u^{23} + 12u^{22} + \dots + 7u + 1$
$c_2, c_4, c_5$ $c_{12}$	$u^{23} - 2u^{22} + \dots + 3u - 1$
$c_3, c_8$	$u^{23} + 2u^{22} + \dots + 2u + 2$
$c_6, c_{10}$	$u^{23} - 7u^{21} + \dots - 3u^2 + 4$
$c_7$	$u^{23} - 6u^{22} + \dots + 8u - 4$
$c_9$	$u^{23} + 14u^{22} + \dots + 24u + 16$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_{11}$	$y^{23} + 32y^{21} + \dots + 31y - 1$
$c_2, c_4, c_5$ $c_{12}$	$y^{23} - 12y^{22} + \dots + 7y - 1$
$c_3, c_8$	$y^{23} - 6y^{22} + \dots + 8y - 4$
$c_6, c_{10}$	$y^{23} - 14y^{22} + \dots + 24y - 16$
$c_7$	$y^{23} + 18y^{22} + \dots - 8y - 16$
$c_9$	$y^{23} - 14y^{22} + \dots - 736y - 256$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.694668 + 0.784847I$ $a = 0.646621 + 0.443219I$ $b = 0.052166 - 0.721195I$ $c = -1.12753 - 0.96163I$ $d = -0.947232 - 0.143060I$	$-2.86000 - 1.29238I$	$-6.06322 + 0.45977I$
$u = 0.694668 - 0.784847I$ $a = 0.646621 - 0.443219I$ $b = 0.052166 + 0.721195I$ $c = -1.12753 + 0.96163I$ $d = -0.947232 + 0.143060I$	$-2.86000 + 1.29238I$	$-6.06322 - 0.45977I$
$u = -0.892323 + 0.293165I$ $a = 0.52674 + 2.12395I$ $b = -0.890003 - 0.443541I$ $c = 2.65342 - 0.49408I$ $d = -0.702937 + 1.066160I$	$-3.02064 - 3.59706I$	$-7.24355 + 7.79597I$
$u = -0.892323 - 0.293165I$ $a = 0.52674 - 2.12395I$ $b = -0.890003 + 0.443541I$ $c = 2.65342 + 0.49408I$ $d = -0.702937 - 1.066160I$	$-3.02064 + 3.59706I$	$-7.24355 - 7.79597I$
$u = -1.095410 + 0.175785I$ $a = 0.663876 - 1.020630I$ $b = -0.552165 + 0.688491I$ $c = -0.136748 + 0.374893I$ $d = -0.248300 - 1.039030I$	$3.68412 - 1.20490I$	$-0.197865 + 0.587959I$
$u = -1.095410 - 0.175785I$ $a = 0.663876 + 1.020630I$ $b = -0.552165 - 0.688491I$ $c = -0.136748 - 0.374893I$ $d = -0.248300 + 1.039030I$	$3.68412 + 1.20490I$	$-0.197865 - 0.587959I$

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.159876 + 0.866608I$ $a = 0.531180 - 0.126379I$ $b = 0.781744 + 0.423915I$ $c = 0.045517 + 0.729067I$ $d = -0.255613 + 1.166420I$	$-0.79201 - 1.83570I$	$-5.62427 + 3.60335I$
$u = 0.159876 - 0.866608I$ $a = 0.531180 + 0.126379I$ $b = 0.781744 - 0.423915I$ $c = 0.045517 - 0.729067I$ $d = -0.255613 - 1.166420I$	$-0.79201 + 1.83570I$	$-5.62427 - 3.60335I$
$u = 1.115790 + 0.351606I$ $a = 0.15695 - 1.65297I$ $b = -0.943072 + 0.599566I$ $c = 1.233050 - 0.090029I$ $d = -0.375083 - 0.309465I$	$2.56195 + 6.12354I$	$-2.77038 - 6.59776I$
$u = 1.115790 - 0.351606I$ $a = 0.15695 + 1.65297I$ $b = -0.943072 - 0.599566I$ $c = 1.233050 + 0.090029I$ $d = -0.375083 + 0.309465I$	$2.56195 - 6.12354I$	$-2.77038 + 6.59776I$
$u = 0.810032 + 0.844947I$ $a = 0.435558 - 0.082401I$ $b = 1.216570 + 0.419344I$ $c = -1.45901 - 1.35263I$ $d = -3.19657 - 0.86128I$	$-10.13410 - 1.43226I$	$-13.58922 + 0.72835I$
$u = 0.810032 - 0.844947I$ $a = 0.435558 + 0.082401I$ $b = 1.216570 - 0.419344I$ $c = -1.45901 + 1.35263I$ $d = -3.19657 + 0.86128I$	$-10.13410 + 1.43226I$	$-13.58922 - 0.72835I$

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.746640 + 0.934392I$ $a = 0.438031 + 0.094410I$ $b = 1.181600 - 0.470208I$ $c = -0.84775 + 1.27484I$ $d = -2.42278 + 0.85521I$	$-6.07831 + 5.69706I$	$-9.37968 - 4.06061I$
$u = -0.746640 - 0.934392I$ $a = 0.438031 - 0.094410I$ $b = 1.181600 + 0.470208I$ $c = -0.84775 - 1.27484I$ $d = -2.42278 - 0.85521I$	$-6.07831 - 5.69706I$	$-9.37968 + 4.06061I$
$u = 1.001420 + 0.725291I$ $a = 0.578527 + 0.586894I$ $b = -0.148145 - 0.864175I$ $c = -1.45246 - 0.50095I$ $d = -1.32533 + 0.53961I$	$-1.95175 + 7.00485I$	$-4.95661 - 5.13787I$
$u = 1.001420 - 0.725291I$ $a = 0.578527 - 0.586894I$ $b = -0.148145 + 0.864175I$ $c = -1.45246 + 0.50095I$ $d = -1.32533 - 0.53961I$	$-1.95175 - 7.00485I$	$-4.95661 + 5.13787I$
$u = 0.966403 + 0.788262I$ $a = -0.73482 - 1.74058I$ $b = -1.205860 + 0.487616I$ $c = -1.69882 - 1.77273I$ $d = -2.39909 + 1.21573I$	$-9.64490 + 7.52364I$	$-12.34364 - 6.02284I$
$u = 0.966403 - 0.788262I$ $a = -0.73482 + 1.74058I$ $b = -1.205860 - 0.487616I$ $c = -1.69882 + 1.77273I$ $d = -2.39909 - 1.21573I$	$-9.64490 - 7.52364I$	$-12.34364 + 6.02284I$

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.040150 + 0.798969I$ $a = -0.65748 + 1.62443I$ $b = -1.214090 - 0.528949I$ $c = -1.55675 + 0.92503I$ $d = -2.00676 - 1.54535I$	$-5.14546 - 12.07470I$	$-8.17479 + 8.06520I$
$u = -1.040150 - 0.798969I$ $a = -0.65748 - 1.62443I$ $b = -1.214090 + 0.528949I$ $c = -1.55675 - 0.92503I$ $d = -2.00676 + 1.54535I$	$-5.14546 + 12.07470I$	$-8.17479 - 8.06520I$
$u = 0.598117$ $a = 1.80880$ $b = -0.447146$ $c = -2.70017$ $d = 0.459836$	$-2.27356$	$-1.62820$
$u = -0.272723 + 0.504579I$ $a = 0.510432 + 0.043771I$ $b = 0.944825 - 0.166773I$ $c = -0.30283 - 2.30298I$ $d = -0.35022 - 4.81571I$	$-4.96054 + 0.60932I$	$-15.8427 - 0.8440I$
$u = -0.272723 - 0.504579I$ $a = 0.510432 - 0.043771I$ $b = 0.944825 + 0.166773I$ $c = -0.30283 + 2.30298I$ $d = -0.35022 + 4.81571I$	$-4.96054 - 0.60932I$	$-15.8427 + 0.8440I$

$$\mathbf{V. } I_5^u = \langle -a^2u^2c - u^2ca + \cdots - 5a + 3, a^2u^2c + 3u^2ca + \cdots + 2a - 1, -a^2u^2 + b + 2a - 2, -2a^2u + 3au + \cdots + 3a - 1, u^3 + u^2 - 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} a \\ a^2u^2 - 2a + 2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u \\ u^2 + u - 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a \\ -a^2u^2 - u^2a + 2a - 2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -a^2u^2 - u^2a + 3a - 2 \\ -a^2u^2 - u^2a + 2a - 2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} c \\ a^2u^2c + u^2ca + \cdots + 5a - 3 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -2a^2u^2c - 2u^2ca + \cdots - 7a + 5 \\ 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^2 - 1 \\ u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -3a^2u^2c - 2u^2ca + \cdots - 3a + 3 \\ -a^2u^2c - 3u^2ca + \cdots - 2a + 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} a^2u^2c + u^2ca + \cdots + 5a - 3 \\ -a^2u^2c + 2u^2ca + \cdots + 4a - 1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $4u - 6$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_9, c_{11}$	$(u^9 + 6u^8 + 15u^7 + 17u^6 + 3u^5 - 12u^4 - 9u^3 + u^2 + 2u + 1)^2$
$c_2, c_4, c_5$ $c_6, c_{10}, c_{12}$	$(u^9 - 3u^7 + u^6 + 3u^5 - 2u^4 + u^3 + u^2 - 2u + 1)^2$
$c_3, c_8$	$(u^3 - u^2 + 1)^6$
$c_7$	$(u^3 - u^2 + 2u - 1)^6$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_9, c_{11}$	$(y^9 - 6y^8 + 27y^7 - 73y^6 + 139y^5 - 184y^4 + 83y^3 - 13y^2 + 2y - 1)^2$
$c_2, c_4, c_5$ $c_6, c_{10}, c_{12}$	$(y^9 - 6y^8 + 15y^7 - 17y^6 + 3y^5 + 12y^4 - 9y^3 - y^2 + 2y - 1)^2$
$c_3, c_8$	$(y^3 - y^2 + 2y - 1)^6$
$c_7$	$(y^3 + 3y^2 + 2y - 1)^6$



(vi) Complex Volumes and Cusp Shapes

Solutions to $I_5^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.877439 + 0.744862I$ $a = 0.616488 - 0.534141I$ $b = -0.073457 + 0.802780I$ $c = 1.28781 - 0.94152I$ $d = 2.02696 - 0.41525I$	$-6.31400 - 2.82812I$	$-9.50976 + 2.97945I$
$u = -0.877439 + 0.744862I$ $a = 0.616488 - 0.534141I$ $b = -0.073457 + 0.802780I$ $c = 1.61569 - 1.41115I$ $d = 1.64564 + 0.80187I$	$-6.31400 - 2.82812I$	$-9.50976 + 2.97945I$
$u = -0.877439 + 0.744862I$ $a = 0.432401 + 0.070043I$ $b = 1.253530 - 0.365043I$ $c = -1.14863 + 0.86295I$ $d = -1.67261 - 0.38662I$	$-6.31400 - 2.82812I$	$-9.50976 + 2.97945I$
$u = -0.877439 + 0.744862I$ $a = 0.432401 + 0.070043I$ $b = 1.253530 - 0.365043I$ $c = 1.28781 - 0.94152I$ $d = 2.02696 - 0.41525I$	$-6.31400 - 2.82812I$	$-9.50976 + 2.97945I$
$u = -0.877439 + 0.744862I$ $a = -0.80377 + 1.95382I$ $b = -1.180080 - 0.437737I$ $c = -1.14863 + 0.86295I$ $d = -1.67261 - 0.38662I$	$-6.31400 - 2.82812I$	$-9.50976 + 2.97945I$
$u = -0.877439 + 0.744862I$ $a = -0.80377 + 1.95382I$ $b = -1.180080 - 0.437737I$ $c = 1.61569 - 1.41115I$ $d = 1.64564 + 0.80187I$	$-6.31400 - 2.82812I$	$-9.50976 + 2.97945I$

Solutions to $I_5^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.877439 - 0.744862I$ $a = 0.616488 + 0.534141I$ $b = -0.073457 - 0.802780I$ $c = 1.28781 + 0.94152I$ $d = 2.02696 + 0.41525I$	$-6.31400 + 2.82812I$	$-9.50976 - 2.97945I$
$u = -0.877439 - 0.744862I$ $a = 0.616488 + 0.534141I$ $b = -0.073457 - 0.802780I$ $c = 1.61569 + 1.41115I$ $d = 1.64564 - 0.80187I$	$-6.31400 + 2.82812I$	$-9.50976 - 2.97945I$
$u = -0.877439 - 0.744862I$ $a = 0.432401 - 0.070043I$ $b = 1.253530 + 0.365043I$ $c = -1.14863 - 0.86295I$ $d = -1.67261 + 0.38662I$	$-6.31400 + 2.82812I$	$-9.50976 - 2.97945I$
$u = -0.877439 - 0.744862I$ $a = 0.432401 - 0.070043I$ $b = 1.253530 + 0.365043I$ $c = 1.28781 + 0.94152I$ $d = 2.02696 + 0.41525I$	$-6.31400 + 2.82812I$	$-9.50976 - 2.97945I$
$u = -0.877439 - 0.744862I$ $a = -0.80377 - 1.95382I$ $b = -1.180080 + 0.437737I$ $c = -1.14863 - 0.86295I$ $d = -1.67261 + 0.38662I$	$-6.31400 + 2.82812I$	$-9.50976 - 2.97945I$
$u = -0.877439 - 0.744862I$ $a = -0.80377 - 1.95382I$ $b = -1.180080 + 0.437737I$ $c = 1.61569 + 1.41115I$ $d = 1.64564 - 0.80187I$	$-6.31400 + 2.82812I$	$-9.50976 - 2.97945I$

Solutions to $I_5^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.754878$ $a = 0.451991$ $b = 1.21243$ $c = 0.603023 + 0.131096I$ $d = 0.610449 + 0.570600I$	-2.17641	-2.98050
$u = 0.754878$ $a = 0.451991$ $b = 1.21243$ $c = 0.603023 - 0.131096I$ $d = 0.610449 - 0.570600I$	-2.17641	-2.98050
$u = 0.754878$ $a = 1.52888 + 1.24301I$ $b = -0.606217 - 0.320153I$ $c = 0.603023 - 0.131096I$ $d = 0.610449 - 0.570600I$	-2.17641	-2.98050
$u = 0.754878$ $a = 1.52888 + 1.24301I$ $b = -0.606217 - 0.320153I$ $c = -2.71580$ $d = 0.779103$	-2.17641	-2.98050
$u = 0.754878$ $a = 1.52888 - 1.24301I$ $b = -0.606217 + 0.320153I$ $c = 0.603023 + 0.131096I$ $d = 0.610449 + 0.570600I$	-2.17641	-2.98050
$u = 0.754878$ $a = 1.52888 - 1.24301I$ $b = -0.606217 + 0.320153I$ $c = -2.71580$ $d = 0.779103$	-2.17641	-2.98050

$$\text{VI. } I_1^v = \langle a, d, c + 1, b - 1, v + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = -12

(iv) **u**-Polynomials at the component

Crossings	<b>u</b> -Polynomials at each crossing
$c_1, c_2, c_5$ $c_{11}$	$u - 1$
$c_3, c_6, c_7$ $c_8, c_9, c_{10}$	$u$
$c_4, c_{12}$	$u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$ $c_5, c_{11}, c_{12}$	$y - 1$
$c_3, c_6, c_7$ $c_8, c_9, c_{10}$	$y$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = -1.00000$		
$a = 0$		
$b = 1.00000$	-3.28987	-12.0000
$c = -1.00000$		
$d = 0$		

$$\text{VII. } I_2^v = \langle c, d + 1, b, a - 1, v + 1 \rangle$$

**(i) Arc colorings**

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes = -12**



(iv) **u**-Polynomials at the component

Crossings	<b>u</b> -Polynomials at each crossing
$c_1, c_2, c_3$ $c_4, c_7, c_8$	$u$
$c_5, c_{10}$	$u + 1$
$c_6, c_9, c_{11}$ $c_{12}$	$u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_4, c_7, c_8$	$y$
$c_5, c_6, c_9$ $c_{10}, c_{11}, c_{12}$	$y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = -1.00000$		
$a = 1.00000$		
$b = 0$	-3.28987	-12.0000
$c = 0$		
$d = -1.00000$		

$$\text{VIII. } I_3^v = \langle a, d + 1, c + a, b - 1, v + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = -12

(iv) **u**-Polynomials at the component

Crossings	<b>u</b> -Polynomials at each crossing
$c_1, c_2, c_6$ $c_9$	$u - 1$
$c_3, c_5, c_7$ $c_8, c_{11}, c_{12}$	$u$
$c_4, c_{10}$	$u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$ $c_6, c_9, c_{10}$	$y - 1$
$c_3, c_5, c_7$ $c_8, c_{11}, c_{12}$	$y$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = -1.00000$		
$a = 0$		
$b = 1.00000$	-3.28987	-12.0000
$c = 0$		
$d = -1.00000$		

$$\text{IX. } I_4^v = \langle a, da - c + 1, dv - 1, cv - a - v, b - 1 \rangle$$

**(i) Arc colorings**

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ d \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ d + 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} v + 1 \\ d \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1 \\ -d \end{pmatrix}$$

**(ii) Obstruction class = -1**

**(iii) Cusp Shapes =  $-d^2 - v^2 - 16$**

**(iv) u-Polynomials at the component :** It cannot be defined for a positive dimension component.

**(v) Riley Polynomials at the component :** It cannot be defined for a positive dimension component.



(iv) Complex Volumes and Cusp Shapes

Solution to $I_4^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = \dots$		
$a = \dots$		
$b = \dots$	-4.93480	-15.5916 - 0.1902I
$c = \dots$		
$d = \dots$		

## X. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_9, c_{11}$	$  \begin{aligned}  & u(u-1)^2 \\  & \cdot (u^9 + 6u^8 + 15u^7 + 17u^6 + 3u^5 - 12u^4 - 9u^3 + u^2 + 2u + 1)^2 \\  & \cdot (u^{14} + 7u^{13} + \dots + 3u + 1)(u^{23} + 12u^{22} + \dots + 7u + 1)^2 \\  & \cdot (u^{23} + 14u^{22} + \dots + 24u + 16)  \end{aligned}  $
$c_2, c_6$	$  \begin{aligned}  & u(u-1)^2(u^9 - 3u^7 + u^6 + 3u^5 - 2u^4 + u^3 + u^2 - 2u + 1)^2 \\  & \cdot (u^{14} - u^{13} + \dots + u + 1)(u^{23} - 7u^{21} + \dots - 3u^2 + 4) \\  & \cdot (u^{23} - 2u^{22} + \dots + 3u - 1)^2  \end{aligned}  $
$c_3, c_8$	$  u^3(u^3 - u^2 + 1)^6(u^{14} + u^{13} + \dots + 4u^2 + 4)(u^{23} + 2u^{22} + \dots + 2u + 2)^3  $
$c_4, c_{10}$	$  \begin{aligned}  & u(u+1)^2(u^9 - 3u^7 + u^6 + 3u^5 - 2u^4 + u^3 + u^2 - 2u + 1)^2 \\  & \cdot (u^{14} - u^{13} + \dots + u + 1)(u^{23} - 7u^{21} + \dots - 3u^2 + 4) \\  & \cdot (u^{23} - 2u^{22} + \dots + 3u - 1)^2  \end{aligned}  $
$c_5, c_{12}$	$  \begin{aligned}  & u(u-1)(u+1)(u^9 - 3u^7 + u^6 + 3u^5 - 2u^4 + u^3 + u^2 - 2u + 1)^2 \\  & \cdot (u^{14} - u^{13} + \dots + u + 1)(u^{23} - 7u^{21} + \dots - 3u^2 + 4) \\  & \cdot (u^{23} - 2u^{22} + \dots + 3u - 1)^2  \end{aligned}  $
$c_7$	$  \begin{aligned}  & u^3(u^3 - u^2 + 2u - 1)^6(u^{14} - 3u^{13} + \dots + 32u + 16) \\  & \cdot (u^{23} - 6u^{22} + \dots + 8u - 4)^3  \end{aligned}  $

## XI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_9, c_{11}$	$y(y-1)^2$ $\cdot (y^9 - 6y^8 + 27y^7 - 73y^6 + 139y^5 - 184y^4 + 83y^3 - 13y^2 + 2y - 1)^2$ $\cdot (y^{14} + 5y^{13} + \dots + 9y + 1)(y^{23} + 32y^{21} + \dots + 31y - 1)^2$ $\cdot (y^{23} - 14y^{22} + \dots - 736y - 256)$
$c_2, c_4, c_5$ $c_6, c_{10}, c_{12}$	$y(y-1)^2$ $\cdot (y^9 - 6y^8 + 15y^7 - 17y^6 + 3y^5 + 12y^4 - 9y^3 - y^2 + 2y - 1)^2$ $\cdot (y^{14} - 7y^{13} + \dots - 3y + 1)(y^{23} - 14y^{22} + \dots + 24y - 16)$ $\cdot (y^{23} - 12y^{22} + \dots + 7y - 1)^2$
$c_3, c_8$	$y^3(y^3 - y^2 + 2y - 1)^6(y^{14} - 3y^{13} + \dots + 32y + 16)$ $\cdot (y^{23} - 6y^{22} + \dots + 8y - 4)^3$
$c_7$	$y^3(y^3 + 3y^2 + 2y - 1)^6(y^{14} + 9y^{13} + \dots - 1536y + 256)$ $\cdot (y^{23} + 18y^{22} + \dots - 8y - 16)^3$