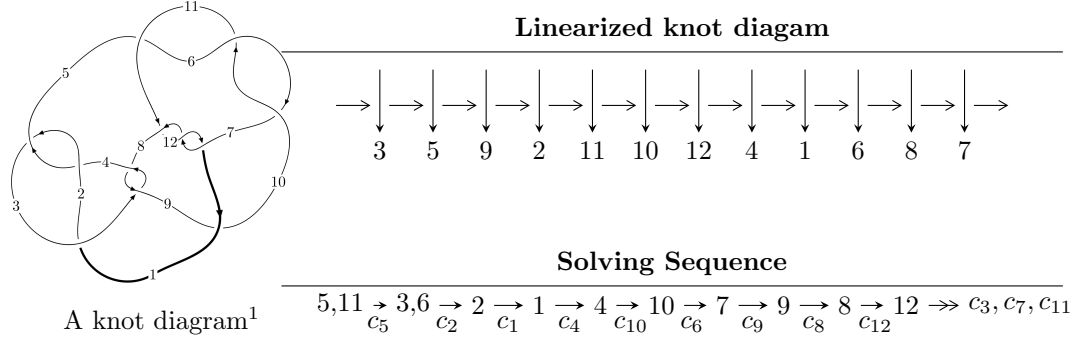


12a<sub>0156</sub> (K12a<sub>0156</sub>)



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 3u^{38} - 51u^{37} + \dots + 256b - 85, -121u^{38} + 133u^{37} + \dots + 512a - 61, u^{39} + 25u^{37} + \dots + u + 1 \rangle$$

$$I_2^u = \langle 2.94986 \times 10^{44}u^{49} + 3.65735 \times 10^{44}u^{48} + \dots + 2.95826 \times 10^{45}b - 1.68829 \times 10^{45}, \\ 2.14090 \times 10^{45}u^{49} + 1.60923 \times 10^{45}u^{48} + \dots + 8.87477 \times 10^{45}a - 4.58714 \times 10^{45}, u^{50} + 2u^{49} + \dots - 18u + 1 \rangle$$

$$I_3^u = \langle -54276a^5u + 156246a^4u + \dots + 839054a - 188617, \\ a^6 + 2a^5u - 4a^4u - a^4 + 4a^3u + 6a^3 + a^2u + 4a^2 + 10au + a + 4u - 1, u^2 + 1 \rangle$$

$$I_4^u = \langle b + 1, u^2 + 2a + u + 3, u^3 + 2u - 1 \rangle$$

$$I_5^u = \langle b + 1, u^3 + u^2 + a + u + 2, u^4 + u^3 + 2u^2 + 2u + 1 \rangle$$

\* 5 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 108 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle 3u^{38} - 51u^{37} + \dots + 256b - 85, -121u^{38} + 133u^{37} + \dots + 512a - 61, u^{39} + 25u^{37} + \dots + u + 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0.236328u^{38} - 0.259766u^{37} + \dots - 0.976563u + 0.119141 \\ -0.0117188u^{38} + 0.199219u^{37} + \dots + 1.71875u + 0.332031 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.224609u^{38} - 0.0605469u^{37} + \dots + 0.742188u + 0.451172 \\ -0.0117188u^{38} + 0.199219u^{37} + \dots + 1.71875u + 0.332031 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^3 - 2u \\ \frac{1}{64}u^{38} + \frac{3}{8}u^{36} + \dots + \frac{1}{64}u^2 + \frac{65}{64}u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.0878906u^{38} - 0.0644531u^{37} + \dots + 1.07031u + 1.04883 \\ -0.199219u^{38} - 0.207031u^{37} + \dots - 1.50000u - 0.761719 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^2 + 1 \\ u^4 + 2u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -0.0156250u^{38} - 0.375000u^{36} + \dots - 0.0156250u^2 + 0.984375u \\ 0.0312500u^{38} + 0.0312500u^{37} + \dots + 1.09375u + 0.0312500 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -1 \\ \frac{1}{64}u^{37} + \frac{3}{8}u^{35} + \dots + \frac{1}{64}u + \frac{1}{64} \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u \\ \frac{1}{64}u^{38} + \frac{3}{8}u^{36} + \dots + \frac{1}{64}u^2 + \frac{65}{64}u \end{pmatrix}$$

(ii) Obstruction class = -1

$$\mathbf{(iii) } \text{Cusp Shapes} = -\frac{2567}{1024}u^{38} + \frac{507}{1024}u^{37} + \dots + \frac{2683}{256}u - \frac{8131}{1024}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{39} + 18u^{38} + \dots + 817u + 16$
$c_2, c_4$	$u^{39} - 4u^{38} + \dots + 13u + 4$
$c_3, c_8$	$u^{39} - 3u^{38} + \dots - 8u + 32$
$c_5, c_6, c_7$ $c_{10}, c_{11}, c_{12}$	$u^{39} + 25u^{37} + \dots + u + 1$
$c_9$	$u^{39} + 24u^{38} + \dots + 132148u + 10276$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{39} + 10y^{38} + \dots + 507201y - 256$
$c_2, c_4$	$y^{39} - 18y^{38} + \dots + 817y - 16$
$c_3, c_8$	$y^{39} + 21y^{38} + \dots - 3776y - 1024$
$c_5, c_6, c_7$ $c_{10}, c_{11}, c_{12}$	$y^{39} + 50y^{38} + \dots - 3y - 1$
$c_9$	$y^{39} + 18y^{38} + \dots - 277125320y - 105596176$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.606138 + 0.433746I$		
$a = 1.10839 - 1.72999I$	$1.24768 - 8.38959I$	$-11.7192 + 9.4891I$
$b = 1.096070 + 0.636892I$		
$u = 0.606138 - 0.433746I$		
$a = 1.10839 + 1.72999I$	$1.24768 + 8.38959I$	$-11.7192 - 9.4891I$
$b = 1.096070 - 0.636892I$		
$u = -0.686742 + 0.093387I$		
$a = 1.124820 + 0.357401I$	$-1.46543 - 1.90675I$	$-13.8759 + 2.9903I$
$b = 0.888553 + 0.474189I$		
$u = -0.686742 - 0.093387I$		
$a = 1.124820 - 0.357401I$	$-1.46543 + 1.90675I$	$-13.8759 - 2.9903I$
$b = 0.888553 - 0.474189I$		
$u = 0.512624 + 0.450918I$		
$a = -0.817372 + 0.180228I$	$3.12365 - 2.96834I$	$-8.53439 + 5.45411I$
$b = 0.464938 - 0.809663I$		
$u = 0.512624 - 0.450918I$		
$a = -0.817372 - 0.180228I$	$3.12365 + 2.96834I$	$-8.53439 - 5.45411I$
$b = 0.464938 + 0.809663I$		
$u = 0.097297 + 1.396560I$		
$a = 0.600483 - 0.695228I$	$5.93701 - 6.97505I$	0
$b = 1.132180 + 0.452280I$		
$u = 0.097297 - 1.396560I$		
$a = 0.600483 + 0.695228I$	$5.93701 + 6.97505I$	0
$b = 1.132180 - 0.452280I$		
$u = -0.485730 + 0.337100I$		
$a = -0.58443 - 2.43918I$	$-1.46092 + 2.88558I$	$-14.3616 - 7.5955I$
$b = -0.928433 + 0.452438I$		
$u = -0.485730 - 0.337100I$		
$a = -0.58443 + 2.43918I$	$-1.46092 - 2.88558I$	$-14.3616 + 7.5955I$
$b = -0.928433 - 0.452438I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.160047 + 0.560104I$ $a = -0.472825 + 0.884195I$ $b = 1.058660 - 0.598292I$	$1.75331 + 5.17154I$	$-10.85539 - 2.38918I$
$u = 0.160047 - 0.560104I$ $a = -0.472825 - 0.884195I$ $b = 1.058660 + 0.598292I$	$1.75331 - 5.17154I$	$-10.85539 + 2.38918I$
$u = 0.255669 + 0.512819I$ $a = 0.095335 - 1.276560I$ $b = 0.500188 + 0.744588I$	$3.42355 + 0.06447I$	$-7.35584 + 3.68014I$
$u = 0.255669 - 0.512819I$ $a = 0.095335 + 1.276560I$ $b = 0.500188 - 0.744588I$	$3.42355 - 0.06447I$	$-7.35584 - 3.68014I$
$u = 0.24730 + 1.43914I$ $a = 0.342403 - 0.242192I$ $b = 0.835724 - 0.187359I$	$8.20195 - 4.67633I$	0
$u = 0.24730 - 1.43914I$ $a = 0.342403 + 0.242192I$ $b = 0.835724 + 0.187359I$	$8.20195 + 4.67633I$	0
$u = -0.01911 + 1.46623I$ $a = -0.513457 - 0.986167I$ $b = -1.218970 + 0.402466I$	$5.58893 + 1.41780I$	0
$u = -0.01911 - 1.46623I$ $a = -0.513457 + 0.986167I$ $b = -1.218970 - 0.402466I$	$5.58893 - 1.41780I$	0
$u = 0.07057 + 1.49185I$ $a = 0.206418 + 0.688633I$ $b = -0.036484 - 0.767123I$	$9.22311 - 2.89697I$	0
$u = 0.07057 - 1.49185I$ $a = 0.206418 - 0.688633I$ $b = -0.036484 + 0.767123I$	$9.22311 + 2.89697I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.435690 + 0.236154I$ $a = -1.49896 + 0.88737I$ $b = -1.166600 + 0.114063I$	$-2.34640 - 0.81341I$	$-13.1026 + 8.4479I$
$u = 0.435690 - 0.236154I$ $a = -1.49896 - 0.88737I$ $b = -1.166600 - 0.114063I$	$-2.34640 + 0.81341I$	$-13.1026 - 8.4479I$
$u = -0.27417 + 1.55715I$ $a = -0.099646 - 0.449882I$ $b = -1.372790 - 0.112918I$	$10.02810 + 6.61870I$	0
$u = -0.27417 - 1.55715I$ $a = -0.099646 + 0.449882I$ $b = -1.372790 + 0.112918I$	$10.02810 - 6.61870I$	0
$u = 0.30186 + 1.56039I$ $a = 0.02339 + 2.01745I$ $b = -0.977777 - 0.644002I$	$11.2737 - 9.4013I$	0
$u = 0.30186 - 1.56039I$ $a = 0.02339 - 2.01745I$ $b = -0.977777 + 0.644002I$	$11.2737 + 9.4013I$	0
$u = -0.35789 + 1.55459I$ $a = 0.37718 + 1.87847I$ $b = 1.184010 - 0.683858I$	$14.1914 + 16.2242I$	0
$u = -0.35789 - 1.55459I$ $a = 0.37718 - 1.87847I$ $b = 1.184010 + 0.683858I$	$14.1914 - 16.2242I$	0
$u = 0.24560 + 1.57817I$ $a = 0.94180 - 1.09265I$ $b = -0.684865 + 0.701681I$	$12.16600 - 4.21253I$	0
$u = 0.24560 - 1.57817I$ $a = 0.94180 + 1.09265I$ $b = -0.684865 - 0.701681I$	$12.16600 + 4.21253I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.198432 + 0.335342I$		
$a = 1.51348 + 1.09795I$	$-0.884650 - 0.467058I$	$-11.90822 - 2.02853I$
$b = -0.837871 - 0.313169I$		
$u = -0.198432 - 0.335342I$		
$a = 1.51348 - 1.09795I$	$-0.884650 + 0.467058I$	$-11.90822 + 2.02853I$
$b = -0.837871 + 0.313169I$		
$u = -0.33367 + 1.57837I$		
$a = -0.848602 - 0.806276I$	$16.5334 + 10.1404I$	0
$b = 0.422675 + 0.993588I$		
$u = -0.33367 - 1.57837I$		
$a = -0.848602 + 0.806276I$	$16.5334 - 10.1404I$	0
$b = 0.422675 - 0.993588I$		
$u = -0.22952 + 1.64191I$		
$a = -0.17339 + 1.41527I$	$18.2436 + 4.6595I$	0
$b = 0.671373 - 0.949740I$		
$u = -0.22952 - 1.64191I$		
$a = -0.17339 - 1.41527I$	$18.2436 - 4.6595I$	0
$b = 0.671373 + 0.949740I$		
$u = -0.340813$		
$a = 0.891121$	$-0.576114$	$-17.1030$
$b = -0.149888$		
$u = -0.17712 + 1.65299I$		
$a = -0.520565 - 1.116590I$	$17.1048 - 1.6856I$	0
$b = 1.044360 + 0.795151I$		
$u = -0.17712 - 1.65299I$		
$a = -0.520565 + 1.116590I$	$17.1048 + 1.6856I$	0
$b = 1.044360 - 0.795151I$		



$$\text{II. } I_2^u = \\
(2.95 \times 10^{44} u^{49} + 3.66 \times 10^{44} u^{48} + \dots + 2.96 \times 10^{45} b - 1.69 \times 10^{45}, 2.14 \times 10^{45} u^{49} + \\
1.61 \times 10^{45} u^{48} + \dots + 8.87 \times 10^{45} a - 4.59 \times 10^{45}, u^{50} + 2u^{49} + \dots - 18u + 9)$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -0.241234u^{49} - 0.181326u^{48} + \dots + 0.375683u + 0.516874 \\ -0.0997162u^{49} - 0.123632u^{48} + \dots + 0.184639u + 0.570706 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.340950u^{49} - 0.304958u^{48} + \dots + 0.560322u + 1.08758 \\ -0.0997162u^{49} - 0.123632u^{48} + \dots + 0.184639u + 0.570706 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.196743u^{49} - 0.293319u^{48} + \dots - 13.0617u + 2.90182 \\ -0.0474075u^{49} - 0.0235454u^{48} + \dots - 3.48640u + 0.424677 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -0.0231020u^{49} + 0.328429u^{48} + \dots + 9.25365u - 3.09937 \\ 0.0273358u^{49} + 0.145463u^{48} + \dots + 1.17016u - 1.26078 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^2 + 1 \\ u^4 + 2u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -0.137409u^{49} - 0.303786u^{48} + \dots - 5.99590u + 2.47777 \\ -0.0865588u^{49} - 0.101282u^{48} + \dots - 1.77113u + 0.685381 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0.0471513u^{49} + 0.147673u^{48} + \dots - 7.45718u + 4.92740 \\ -0.100202u^{49} - 0.286035u^{48} + \dots + 0.536308u + 0.519665 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -0.164482u^{49} - 0.228762u^{48} + \dots - 16.5539u + 2.42436 \\ 0.0322612u^{49} + 0.0645573u^{48} + \dots - 1.49216u - 0.477454 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-0.817749u^{49} - 1.70803u^{48} + \dots - 1.83623u - 9.61323$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$(u^{25} + 11u^{24} + \dots - 2u + 1)^2$
$c_2, c_4$	$(u^{25} - 3u^{24} + \dots - 4u + 1)^2$
$c_3, c_8$	$(u^{25} + u^{24} + \dots + 4u - 4)^2$
$c_5, c_6, c_7$ $c_{10}, c_{11}, c_{12}$	$u^{50} + 2u^{49} + \dots - 18u + 9$
$c_9$	$(u^{25} - 8u^{24} + \dots + 11u + 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^{25} + 9y^{24} + \dots - 2y - 1)^2$
$c_2, c_4$	$(y^{25} - 11y^{24} + \dots - 2y - 1)^2$
$c_3, c_8$	$(y^{25} + 15y^{24} + \dots - 88y - 16)^2$
$c_5, c_6, c_7$ $c_{10}, c_{11}, c_{12}$	$y^{50} + 42y^{49} + \dots + 1584y + 81$
$c_9$	$(y^{25} + 20y^{24} + \dots + 251y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.863192 + 0.531967I$ $a = -0.56076 + 1.52524I$ $b = -0.903290 - 0.591334I$	$4.43073 - 5.11531I$	$-8.18255 + 5.48464I$
$u = 0.863192 - 0.531967I$ $a = -0.56076 - 1.52524I$ $b = -0.903290 + 0.591334I$	$4.43073 + 5.11531I$	$-8.18255 - 5.48464I$
$u = 0.790213 + 0.646113I$ $a = 0.322984 - 0.681750I$ $b = -0.781818 + 0.585895I$	$4.81480 - 0.43356I$	$-7.08804 + 0.I$
$u = 0.790213 - 0.646113I$ $a = 0.322984 + 0.681750I$ $b = -0.781818 - 0.585895I$	$4.81480 + 0.43356I$	$-7.08804 + 0.I$
$u = -0.800123 + 0.560428I$ $a = -1.41196 - 0.56327I$ $b = -1.306760 - 0.052319I$	$3.08820 + 2.66172I$	$-6.71477 - 3.57661I$
$u = -0.800123 - 0.560428I$ $a = -1.41196 + 0.56327I$ $b = -1.306760 + 0.052319I$	$3.08820 - 2.66172I$	$-6.71477 + 3.57661I$
$u = -0.125962 + 1.023520I$ $a = 2.16186 - 3.13157I$ $b = -0.819709$	$2.09579$	$-12.44382 + 0.I$
$u = -0.125962 - 1.023520I$ $a = 2.16186 + 3.13157I$ $b = -0.819709$	$2.09579$	$-12.44382 + 0.I$
$u = -0.237534 + 1.042900I$ $a = 0.602799 + 1.091330I$ $b = 1.012760 - 0.537221I$	$1.37392 + 5.41987I$	$-11.35697 - 6.54919I$
$u = -0.237534 - 1.042900I$ $a = 0.602799 - 1.091330I$ $b = 1.012760 + 0.537221I$	$1.37392 - 5.41987I$	$-11.35697 + 6.54919I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.963620 + 0.475288I$		
$a = 1.14015 + 1.21785I$	$7.62261 + 11.39030I$	$-7.28983 - 7.76664I$
$b = 1.139240 - 0.687767I$		
$u = -0.963620 - 0.475288I$		
$a = 1.14015 - 1.21785I$	$7.62261 - 11.39030I$	$-7.28983 + 7.76664I$
$b = 1.139240 + 0.687767I$		
$u = -0.942522 + 0.536594I$		
$a = -0.427504 - 0.100379I$	$9.63785 + 5.44271I$	$-4.49829 - 3.51350I$
$b = 0.479273 + 0.936834I$		
$u = -0.942522 - 0.536594I$		
$a = -0.427504 + 0.100379I$	$9.63785 - 5.44271I$	$-4.49829 + 3.51350I$
$b = 0.479273 - 0.936834I$		
$u = 0.035416 + 1.096400I$		
$a = -0.51282 + 1.51762I$	$-0.175498 - 1.059220I$	$-15.3940 + 0.I$
$b = -1.073950 - 0.294320I$		
$u = 0.035416 - 1.096400I$		
$a = -0.51282 - 1.51762I$	$-0.175498 + 1.059220I$	$-15.3940 + 0.I$
$b = -1.073950 + 0.294320I$		
$u = -0.863688 + 0.730509I$		
$a = 0.349454 + 0.701314I$	$10.21860 + 0.59688I$	$-3.53242 + 0.I$
$b = 0.563663 - 0.911236I$		
$u = -0.863688 - 0.730509I$		
$a = 0.349454 - 0.701314I$	$10.21860 - 0.59688I$	$-3.53242 + 0.I$
$b = 0.563663 + 0.911236I$		
$u = -0.828010 + 0.806350I$		
$a = 0.246724 - 0.383981I$	$8.61369 - 5.36637I$	$-5.53322 + 0.I$
$b = 1.089150 + 0.711472I$		
$u = -0.828010 - 0.806350I$		
$a = 0.246724 + 0.383981I$	$8.61369 + 5.36637I$	$-5.53322 + 0.I$
$b = 1.089150 - 0.711472I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.416306 + 1.118060I$ $a = 0.86554 - 1.47471I$ $b = 0.840318 + 0.621070I$	$5.39169 - 2.44039I$	0
$u = 0.416306 - 1.118060I$ $a = 0.86554 + 1.47471I$ $b = 0.840318 - 0.621070I$	$5.39169 + 2.44039I$	0
$u = -0.080139 + 1.205770I$ $a = 0.372713 - 0.398049I$ $b = 0.144497 + 0.357570I$	$2.95409 + 1.50728I$	0
$u = -0.080139 - 1.205770I$ $a = 0.372713 + 0.398049I$ $b = 0.144497 - 0.357570I$	$2.95409 - 1.50728I$	0
$u = -0.219956 + 1.253270I$ $a = -0.0219369 + 0.1367750I$ $b = 0.706780 + 0.369020I$	$2.66645 + 1.39976I$	0
$u = -0.219956 - 1.253270I$ $a = -0.0219369 - 0.1367750I$ $b = 0.706780 - 0.369020I$	$2.66645 - 1.39976I$	0
$u = 0.307492 + 1.236030I$ $a = -0.815496 + 0.040530I$ $b = 0.840318 - 0.621070I$	$5.39169 + 2.44039I$	0
$u = 0.307492 - 1.236030I$ $a = -0.815496 - 0.040530I$ $b = 0.840318 + 0.621070I$	$5.39169 - 2.44039I$	0
$u = 0.647951 + 0.242324I$ $a = 1.40449 - 0.16649I$ $b = 0.706780 - 0.369020I$	$2.66645 - 1.39976I$	$-7.04278 + 0.06062I$
$u = 0.647951 - 0.242324I$ $a = 1.40449 + 0.16649I$ $b = 0.706780 + 0.369020I$	$2.66645 + 1.39976I$	$-7.04278 - 0.06062I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.396390 + 0.399496I$ $a = 0.963949 - 0.525295I$ $b = 0.144497 - 0.357570I$	$2.95409 - 1.50728I$	$-6.97928 + 4.31266I$
$u = 0.396390 - 0.399496I$ $a = 0.963949 + 0.525295I$ $b = 0.144497 + 0.357570I$	$2.95409 + 1.50728I$	$-6.97928 - 4.31266I$
$u = 0.10841 + 1.43332I$ $a = 0.410688 + 0.375917I$ $b = -1.306760 + 0.052319I$	$3.08820 - 2.66172I$	0
$u = 0.10841 - 1.43332I$ $a = 0.410688 - 0.375917I$ $b = -1.306760 - 0.052319I$	$3.08820 + 2.66172I$	0
$u = -0.05540 + 1.45028I$ $a = 1.23305 + 1.70385I$ $b = -0.781818 - 0.585895I$	$4.81480 + 0.43356I$	0
$u = -0.05540 - 1.45028I$ $a = 1.23305 - 1.70385I$ $b = -0.781818 + 0.585895I$	$4.81480 - 0.43356I$	0
$u = -0.14356 + 1.46162I$ $a = 0.59905 - 2.26807I$ $b = -0.903290 + 0.591334I$	$4.43073 + 5.11531I$	0
$u = -0.14356 - 1.46162I$ $a = 0.59905 + 2.26807I$ $b = -0.903290 - 0.591334I$	$4.43073 - 5.11531I$	0
$u = -0.03744 + 1.51239I$ $a = -0.60761 + 1.77442I$ $b = 1.089150 - 0.711472I$	$8.61369 + 5.36637I$	0
$u = -0.03744 - 1.51239I$ $a = -0.60761 - 1.77442I$ $b = 1.089150 + 0.711472I$	$8.61369 - 5.36637I$	0

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.21031 + 1.50284I$ $a = -0.05347 - 2.08186I$ $b = 1.139240 + 0.687767I$	$7.62261 - 11.39030I$	0
$u = 0.21031 - 1.50284I$ $a = -0.05347 + 2.08186I$ $b = 1.139240 - 0.687767I$	$7.62261 + 11.39030I$	0
$u = 0.02120 + 1.51758I$ $a = -0.64643 - 1.54897I$ $b = 0.563663 + 0.911236I$	$10.21860 - 0.59688I$	0
$u = 0.02120 - 1.51758I$ $a = -0.64643 + 1.54897I$ $b = 0.563663 - 0.911236I$	$10.21860 + 0.59688I$	0
$u = 0.16595 + 1.51068I$ $a = -0.96384 + 1.16614I$ $b = 0.479273 - 0.936834I$	$9.63785 - 5.44271I$	0
$u = 0.16595 - 1.51068I$ $a = -0.96384 - 1.16614I$ $b = 0.479273 + 0.936834I$	$9.63785 + 5.44271I$	0
$u = 0.441747 + 0.053796I$ $a = 0.48121 - 1.49645I$ $b = 1.012760 - 0.537221I$	$1.37392 + 5.41987I$	$-11.35697 - 6.54919I$
$u = 0.441747 - 0.053796I$ $a = 0.48121 + 1.49645I$ $b = 1.012760 + 0.537221I$	$1.37392 - 5.41987I$	$-11.35697 + 6.54919I$
$u = -0.106624 + 0.220666I$ $a = -5.79950 + 1.80662I$ $b = -1.073950 + 0.294320I$	$-0.175498 + 1.059220I$	$-15.3940 - 0.3706I$
$u = -0.106624 - 0.220666I$ $a = -5.79950 - 1.80662I$ $b = -1.073950 - 0.294320I$	$-0.175498 - 1.059220I$	$-15.3940 + 0.3706I$



$$\text{III. } I_3^u = \langle -5.43 \times 10^4 a^5 u + 1.56 \times 10^5 a^4 u + \cdots + 8.39 \times 10^5 a - 1.89 \times 10^5, 2a^5 u - 4a^4 u + \cdots + a - 1, u^2 + 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} a \\ 0.0510511a^5 u - 0.146963a^4 u + \cdots - 0.789201a + 0.177410 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.0510511a^5 u - 0.146963a^4 u + \cdots + 0.210799a + 0.177410 \\ 0.0510511a^5 u - 0.146963a^4 u + \cdots - 0.789201a + 0.177410 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ 0.0269872a^5 u - 0.143796a^4 u + \cdots + 0.311302a + 1.03365 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -0.115515a^5 u + 0.102601a^4 u + \cdots + 0.261687a + 1.46186 \\ -0.0683729a^5 u + 0.141112a^4 u + \cdots + 1.04666a + 0.569012 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -0.0269872a^5 u + 0.143796a^4 u + \cdots - 0.311302a - 1.03365 \\ 0.0989937a^5 u - 0.242195a^4 u + \cdots + 0.477577a - 0.543207 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -1 \\ 0.0862375a^5 u - 0.0931583a^4 u + \cdots + 0.214093a - 0.322042 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u \\ 0.0269872a^5 u - 0.143796a^4 u + \cdots + 0.311302a + 1.03365 \end{pmatrix}$$

(ii) Obstruction class = 1

$$\text{(iii) Cusp Shapes} = -\frac{288672}{1063169}a^5 u + \frac{504748}{1063169}a^4 u + \cdots - \frac{1898092}{1063169}a - \frac{3575656}{1063169}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$(u^6 - 3u^5 + 5u^4 - 4u^3 + 2u^2 - u + 1)^2$
$c_2$	$(u^6 + u^5 - u^4 - 2u^3 + u + 1)^2$
$c_3, c_8$	$u^{12} + 3u^{10} + 5u^8 + 4u^6 + 2u^4 + u^2 + 1$
$c_4$	$(u^6 - u^5 - u^4 + 2u^3 - u + 1)^2$
$c_5, c_6, c_7$ $c_{10}, c_{11}, c_{12}$	$(u^2 + 1)^6$
$c_9$	$u^{12} - u^{10} + 5u^8 + 6u^4 - 3u^2 + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^6 + y^5 + 5y^4 + 6y^2 + 3y + 1)^2$
$c_2, c_4$	$(y^6 - 3y^5 + 5y^4 - 4y^3 + 2y^2 - y + 1)^2$
$c_3, c_8$	$(y^6 + 3y^5 + 5y^4 + 4y^3 + 2y^2 + y + 1)^2$
$c_5, c_6, c_7$ $c_{10}, c_{11}, c_{12}$	$(y + 1)^{12}$
$c_9$	$(y^6 - y^5 + 5y^4 + 6y^2 - 3y + 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.000000I$ $a = -0.477727 + 0.831626I$ $b = 1.073950 - 0.558752I$	$3.28987 + 5.69302I$	$-6.00000 - 5.51057I$
$u = 1.000000I$ $a = 0.214242 - 1.226020I$ $b = 0.428243 + 0.664531I$	$5.18047 + 0.92430I$	$-2.28328 - 0.79423I$
$u = 1.000000I$ $a = 1.16005 - 1.04838I$ $b = 1.073950 + 0.558752I$	$3.28987 - 5.69302I$	$-6.00000 + 5.51057I$
$u = 1.000000I$ $a = -0.382665 - 0.093522I$ $b = 0.428243 - 0.664531I$	$5.18047 - 0.92430I$	$-2.28328 + 0.79423I$
$u = 1.000000I$ $a = 1.39869 + 1.49594I$ $b = -1.002190 - 0.295542I$	$1.39926 - 0.92430I$	$-9.71672 + 0.79423I$
$u = 1.000000I$ $a = -1.91259 - 1.95964I$ $b = -1.002190 + 0.295542I$	$1.39926 + 0.92430I$	$-9.71672 - 0.79423I$
$u = -1.000000I$ $a = -0.477727 - 0.831626I$ $b = 1.073950 + 0.558752I$	$3.28987 - 5.69302I$	$-6.00000 + 5.51057I$
$u = -1.000000I$ $a = 0.214242 + 1.226020I$ $b = 0.428243 - 0.664531I$	$5.18047 - 0.92430I$	$-2.28328 + 0.79423I$
$u = -1.000000I$ $a = 1.16005 + 1.04838I$ $b = 1.073950 - 0.558752I$	$3.28987 + 5.69302I$	$-6.00000 - 5.51057I$
$u = -1.000000I$ $a = -0.382665 + 0.093522I$ $b = 0.428243 + 0.664531I$	$5.18047 + 0.92430I$	$-2.28328 - 0.79423I$

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.000000I$		
$a = 1.39869 - 1.49594I$	$1.39926 + 0.92430I$	$-9.71672 - 0.79423I$
$b = -1.002190 + 0.295542I$		
$u = -1.000000I$		
$a = -1.91259 + 1.95964I$	$1.39926 - 0.92430I$	$-9.71672 + 0.79423I$
$b = -1.002190 - 0.295542I$		

$$\text{IV. } I_4^u = \langle b + 1, u^2 + 2a + u + 3, u^3 + 2u - 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -\frac{1}{2}u^2 - \frac{1}{2}u - \frac{3}{2} \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -\frac{1}{2}u^2 - \frac{1}{2}u - \frac{5}{2} \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -\frac{1}{2}u^2 - \frac{1}{2}u - \frac{3}{2} \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ -u + 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^2 + 1 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -u + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -u + 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u \\ u^2 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-\frac{7}{4}u^2 - \frac{21}{4}u - \frac{57}{4}$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$(u - 1)^3$
$c_3, c_8$	$u^3$
$c_4$	$(u + 1)^3$
$c_5, c_6, c_7$	$u^3 + 2u - 1$
$c_9$	$u^3 - 3u^2 + 5u - 2$
$c_{10}, c_{11}, c_{12}$	$u^3 + 2u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y - 1)^3$
$c_3, c_8$	$y^3$
$c_5, c_6, c_7$ $c_{10}, c_{11}, c_{12}$	$y^3 + 4y^2 + 4y - 1$
$c_9$	$y^3 + y^2 + 13y - 4$



(vi) Complex Volumes and Cusp Shapes

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.22670 + 1.46771I$ $a = -0.335258 - 0.401127I$ $b = -1.00000$	$7.79580 + 5.13794I$	$-9.37996 - 6.54094I$
$u = -0.22670 - 1.46771I$ $a = -0.335258 + 0.401127I$ $b = -1.00000$	$7.79580 - 5.13794I$	$-9.37996 + 6.54094I$
$u = 0.453398$ $a = -1.82948$ $b = -1.00000$	$-2.43213$	$-16.9900$

$$\mathbf{V. } I_5^u = \langle b + 1, u^3 + u^2 + a + u + 2, u^4 + u^3 + 2u^2 + 2u + 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^3 - u^2 - u - 2 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^3 - u^2 - u - 3 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^3 - u^2 - u - 2 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^2 + 1 \\ -u^3 - 2u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^3 + 2u \\ u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^3 + 2u \\ u^3 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -2u^3 - u^2 - 3u - 3 \\ -u^3 - u^2 - u - 2 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-4u^3 - 4u - 15$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$(u - 1)^4$
$c_3, c_8$	$u^4$
$c_4$	$(u + 1)^4$
$c_5, c_6, c_7$	$u^4 + u^3 + 2u^2 + 2u + 1$
$c_9$	$(u^2 + u + 1)^2$
$c_{10}, c_{11}, c_{12}$	$u^4 - u^3 + 2u^2 - 2u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y - 1)^4$
$c_3, c_8$	$y^4$
$c_5, c_6, c_7$ $c_{10}, c_{11}, c_{12}$	$y^4 + 3y^3 + 2y^2 + 1$
$c_9$	$(y^2 + y + 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_5^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.621744 + 0.440597I$ $a = -1.69244 - 0.31815I$ $b = -1.00000$	$1.64493 + 2.02988I$	$-13.00000 - 3.46410I$
$u = -0.621744 - 0.440597I$ $a = -1.69244 + 0.31815I$ $b = -1.00000$	$1.64493 - 2.02988I$	$-13.00000 + 3.46410I$
$u = 0.121744 + 1.306620I$ $a = 0.192440 + 0.547877I$ $b = -1.00000$	$1.64493 - 2.02988I$	$-13.00000 + 3.46410I$
$u = 0.121744 - 1.306620I$ $a = 0.192440 - 0.547877I$ $b = -1.00000$	$1.64493 + 2.02988I$	$-13.00000 - 3.46410I$

## VI. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u-1)^7(u^6 - 3u^5 + 5u^4 - 4u^3 + 2u^2 - u + 1)^2$ $\cdot ((u^{25} + 11u^{24} + \dots - 2u + 1)^2)(u^{39} + 18u^{38} + \dots + 817u + 16)$
$c_2$	$((u-1)^7)(u^6 + u^5 + \dots + u + 1)^2(u^{25} - 3u^{24} + \dots - 4u + 1)^2$ $\cdot (u^{39} - 4u^{38} + \dots + 13u + 4)$
$c_3, c_8$	$u^7(u^{12} + 3u^{10} + \dots + u^2 + 1)(u^{25} + u^{24} + \dots + 4u - 4)^2$ $\cdot (u^{39} - 3u^{38} + \dots - 8u + 32)$
$c_4$	$((u+1)^7)(u^6 - u^5 + \dots - u + 1)^2(u^{25} - 3u^{24} + \dots - 4u + 1)^2$ $\cdot (u^{39} - 4u^{38} + \dots + 13u + 4)$
$c_5, c_6, c_7$	$((u^2 + 1)^6)(u^3 + 2u - 1)(u^4 + u^3 + \dots + 2u + 1)(u^{39} + 25u^{37} + \dots + u + 1)$ $\cdot (u^{50} + 2u^{49} + \dots - 18u + 9)$
$c_9$	$(u^2 + u + 1)^2(u^3 - 3u^2 + 5u - 2)(u^{12} - u^{10} + 5u^8 + 6u^4 - 3u^2 + 1)$ $\cdot ((u^{25} - 8u^{24} + \dots + 11u + 1)^2)(u^{39} + 24u^{38} + \dots + 132148u + 10276)$
$c_{10}, c_{11}, c_{12}$	$((u^2 + 1)^6)(u^3 + 2u + 1)(u^4 - u^3 + \dots - 2u + 1)(u^{39} + 25u^{37} + \dots + u + 1)$ $\cdot (u^{50} + 2u^{49} + \dots - 18u + 9)$

## VII. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y-1)^7)(y^6 + y^5 + \dots + 3y + 1)^2(y^{25} + 9y^{24} + \dots - 2y - 1)^2$ $\cdot (y^{39} + 10y^{38} + \dots + 507201y - 256)$
$c_2, c_4$	$(y-1)^7(y^6 - 3y^5 + 5y^4 - 4y^3 + 2y^2 - y + 1)^2$ $\cdot ((y^{25} - 11y^{24} + \dots - 2y - 1)^2)(y^{39} - 18y^{38} + \dots + 817y - 16)$
$c_3, c_8$	$y^7(y^6 + 3y^5 + 5y^4 + 4y^3 + 2y^2 + y + 1)^2$ $\cdot ((y^{25} + 15y^{24} + \dots - 88y - 16)^2)(y^{39} + 21y^{38} + \dots - 3776y - 1024)$
$c_5, c_6, c_7$ $c_{10}, c_{11}, c_{12}$	$(y+1)^{12}(y^3 + 4y^2 + 4y - 1)(y^4 + 3y^3 + 2y^2 + 1)$ $\cdot (y^{39} + 50y^{38} + \dots - 3y - 1)(y^{50} + 42y^{49} + \dots + 1584y + 81)$
$c_9$	$(y^2 + y + 1)^2(y^3 + y^2 + 13y - 4)(y^6 - y^5 + 5y^4 + 6y^2 - 3y + 1)^2$ $\cdot (y^{25} + 20y^{24} + \dots + 251y - 1)^2$ $\cdot (y^{39} + 18y^{38} + \dots - 277125320y - 105596176)$