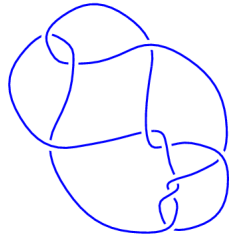
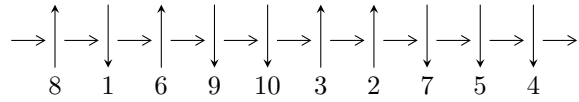


10₂₉ (K10a₅₃)

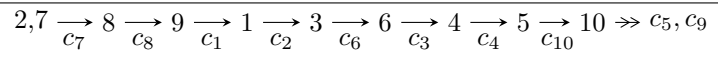


1

Arc Sequences



Solving Sequence



Representation Ideals

$$I = I_1^u$$

$$I_1^u = \langle u^{31} - u^{30} + \dots + 2u^2 + 1 \rangle$$

There are 1 irreducible components with 31 representations.

¹The knot diagram image is adapter from “C. Livingston and A. H. Moore, KnotInfo: Table of Knot Invariants, <http://www.indiana.edu/~knotinfo>”

$$\mathbf{I. } I_1^u = \langle u^{31} - u^{30} + \dots + 2u^2 + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^4 + u^2 + 1 \\ u^4 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^9 - 2u^7 - 3u^5 - 2u^3 - u \\ -u^9 - u^7 - u^5 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^{14} + 3u^{12} + 6u^{10} + 7u^8 + 6u^6 + 4u^4 + 2u^2 + 1 \\ u^{14} + 2u^{12} + 3u^{10} + 2u^8 - u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^{18} + 3u^{16} + 8u^{14} + 13u^{12} + 17u^{10} + 17u^8 + 12u^6 + 8u^4 + 3u^2 + 1 \\ u^{20} + 4u^{18} + 10u^{16} + 18u^{14} + 23u^{12} + 24u^{10} + 18u^8 + 10u^6 + 5u^4 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^{26} + 5u^{24} + \dots + 3u^2 + 1 \\ u^{26} + 4u^{24} + \dots - 2u^4 + u^2 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$\begin{aligned} &= -4u^{30} - 20u^{28} - 4u^{27} - 68u^{26} - 20u^{25} - 160u^{24} - 64u^{23} - 300u^{22} - 144u^{21} - 460u^{20} - \\ &252u^{19} - 592u^{18} - 364u^{17} - 660u^{16} - 436u^{15} - 628u^{14} - 452u^{13} - 528u^{12} - 396u^{11} - \\ &380u^{10} - 296u^9 - 236u^8 - 188u^7 - 128u^6 - 92u^5 - 52u^4 - 40u^3 - 20u^2 - 12u - 6 \end{aligned}$$

(iv) Complex Volumes and Cusp Shapes

Solution to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.752643 - 0.616875I$	$0.72976 - 2.73446I$	$-0.23310 + 3.38925I$
$u = -0.752643 + 0.616875I$	$0.72976 + 2.73446I$	$-0.23310 - 3.38925I$
$u = -0.709633 - 0.857826I$	$3.99591 + 2.71284I$	$3.89942 - 3.44665I$
$u = -0.709633 + 0.857826I$	$3.99591 - 2.71284I$	$3.89942 + 3.44665I$
$u = -0.696118 - 0.446614I$	$-5.89237 + 3.33239I$	$-5.23670 - 3.21859I$
$u = -0.696118 + 0.446614I$	$-5.89237 - 3.33239I$	$-5.23670 + 3.21859I$
$u = -0.673649 - 1.023568I$	$-0.47562 + 8.17190I$	$-2.44268 - 8.00325I$
$u = -0.673649 + 1.023568I$	$-0.47562 - 8.17190I$	$-2.44268 + 8.00325I$
$u = -0.611328 - 1.036445I$	$-7.51197 + 1.64856I$	$-8.01509 - 2.12263I$
$u = -0.611328 + 1.036445I$	$-7.51197 - 1.64856I$	$-8.01509 + 2.12263I$
$u = -0.495857$	-2.75281	-1.58212
$u = -0.307711 - 0.890519I$	$-5.22411 + 2.56488I$	$-9.16453 - 4.43258I$
$u = -0.307711 + 0.890519I$	$-5.22411 - 2.56488I$	$-9.16453 + 4.43258I$
$u = -0.048600 - 1.113390I$	$-11.00386 + 5.04935I$	$-11.12529 - 3.42516I$
$u = -0.048600 + 1.113390I$	$-11.00386 - 5.04935I$	$-11.12529 + 3.42516I$
$u = 0.028596 - 1.074733I$	$-4.89690 - 1.99617I$	$-7.89924 + 3.62729I$
$u = 0.028596 + 1.074733I$	$-4.89690 + 1.99617I$	$-7.89924 - 3.62729I$
$u = 0.330533 - 0.488116I$	$-0.107136 - 1.026304I$	$-1.81008 + 6.41690I$
$u = 0.330533 + 0.488116I$	$-0.107136 + 1.026304I$	$-1.81008 - 6.41690I$
$u = 0.630136 - 0.611565I$	$0.007927 - 0.929922I$	$-2.40372 + 3.68841I$
$u = 0.630136 + 0.611565I$	$0.007927 + 0.929922I$	$-2.40372 - 3.68841I$
$u = 0.642253 - 1.006365I$	$-1.14145 - 4.14236I$	$-4.20039 + 2.04013I$
$u = 0.642253 + 1.006365I$	$-1.14145 + 4.14236I$	$-4.20039 - 2.04013I$
$u = 0.680810 - 1.043631I$	$-6.33335 - 11.60291I$	$-6.34947 + 7.70694I$
$u = 0.680810 + 1.043631I$	$-6.33335 + 11.60291I$	$-6.34947 - 7.70694I$
$u = 0.711244 - 0.915096I$	$0.12823 - 5.89464I$	$-1.94513 + 6.44091I$
$u = 0.711244 + 0.915096I$	$0.12823 + 5.89464I$	$-1.94513 - 6.44091I$
$u = 0.730031 - 0.790482I$	$0.502956 + 0.402984I$	$-0.929300 - 0.528315I$
$u = 0.730031 + 0.790482I$	$0.502956 - 0.402984I$	$-0.929300 + 0.528315I$
$u = 0.794006 - 0.593785I$	$-4.99237 + 6.04082I$	$-4.35365 - 3.16093I$

Solution to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.794006 + 0.593785I$	$-4.99237 - 6.04082I$	$-4.35365 + 3.16093I$

II. u-Polynomials

Crossings	u-Polynomials at each crossings
c_1, c_7	$(u^{31} + u^{30} + \dots - 2u^2 - 1)$
c_2, c_8	$(u^{31} + 11u^{30} + \dots - 4u - 1)$
c_3, c_6	$(u^{31} + 5u^{30} + \dots + 40u + 7)$
c_4, c_5, c_9	$(u^{31} + u^{30} + \dots + 2u + 1)$
c_{10}	$(u^{31} + 3u^{30} + \dots - 13u + 16)$

III. Riley Polynomials

Crossings	Riley Polynomials at each crossings
c_1, c_7	$(y^{31} + 11y^{30} + \dots - 4y - 1)$
c_2, c_8	$(y^{31} + 19y^{30} + \dots - 8y - 1)$
c_3, c_6	$(y^{31} + 23y^{30} + \dots - 640y - 49)$
c_4, c_5, c_9	$(y^{31} - 29y^{30} + \dots - 4y - 1)$
c_{10}	$(y^{31} - 9y^{30} + \dots + 1481y - 256)$