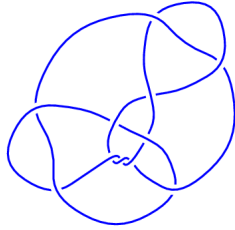
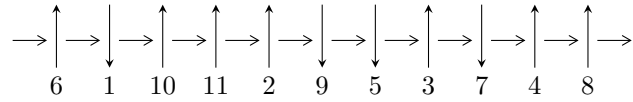


11a₁₅₁ (K11a₁₅₁)

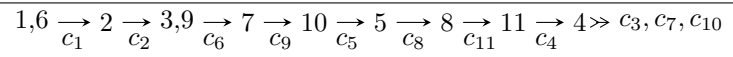


1

Arc Sequences



Solving Sequence



Representation Ideals

$$I = \bigcap_{i=1}^2 I_i^u$$

$$I_1^u = \langle u^3 + u^2 + 2u + 1, -u^2 + a - u - 2, u^2 + 7b + 6u + 4 \rangle$$

$$I_2^u = \langle u^{66} + 2u^{65} + \dots + 4u + 1, 5.94710 \times 10^{52}u^{65} + 1.17236 \times 10^{53}u^{64} + \dots + 8.35081 \times 10^{52}b + 2.54635 \times 10^{53} \\ - 8.47686 \times 10^{52}u^{65} - 1.39894 \times 10^{53}u^{64} + \dots + 1.19297 \times 10^{52}a - 2.19440 \times 10^{53} \rangle$$

There are 2 irreducible components with 69 representations.

¹The knot diagram image is adapter from “C. Livingston and A. H. Moore, KnotInfo: Table of Knot Invariants, <http://www.indiana.edu/~knotinfo>”

$$\text{I. } I_1^u = \langle u^3 + u^2 + 2u + 1, -u^2 + a - u - 2, u^2 + 7b + 6u + 4 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^2 + u + 2 \\ -\frac{1}{7}u^2 - \frac{6}{7}u - \frac{4}{7} \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^2 + u + 2 \\ -\frac{1}{7}u^2 + \frac{1}{7}u - \frac{4}{7} \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ -u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u \\ -u^2 - u - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} \frac{4}{7}u^2 + \frac{3}{7}u + \frac{9}{7} \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^2 + 1 \\ -u^2 - u - 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^2 + 1 \\ -u^2 - u - 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.569840$ $a = 1.75488$ $b = -0.129382$	-0.531480	2.84969
$u = -0.215080 - 1.307141I$ $a = 0.122561 - 0.744862I$ $b = -0.149595 + 1.040081I$	$-4.66906 + 2.82812I$	$-1.67995 - 11.45076I$
$u = -0.215080 + 1.307141I$ $a = 0.122561 + 0.744862I$ $b = -0.149595 - 1.040081I$	$-4.66906 - 2.82812I$	$-1.67995 + 11.45076I$

$$\text{II. } I_2^u = \langle u^{66} + 2u^{65} + \dots + 4u + 1, 5.95 \times 10^{52}u^{65} + 1.17 \times 10^{53}u^{64} + \dots + 8.35 \times 10^{52}b + 2.55 \times 10^{53}, -8.48 \times 10^{52}u^{65} - 1.40 \times 10^{53}u^{64} + \dots + 1.19 \times 10^{52}a - 2.19 \times 10^{53} \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 7.10566u^{65} + 11.7265u^{64} + \dots + 31.4641u + 18.3944 \\ -0.712158u^{65} - 1.40388u^{64} + \dots - 2.74081u - 3.04922 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 8.72726u^{65} + 14.2298u^{64} + \dots + 35.4678u + 22.1382 \\ -2.15625u^{65} - 3.59400u^{64} + \dots - 6.93271u - 6.34045 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -5.31162u^{65} - 8.22686u^{64} + \dots - 15.8436u - 12.2934 \\ 3.63832u^{65} + 5.58995u^{64} + \dots + 12.4635u + 8.35519 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 7.66328u^{65} + 12.2341u^{64} + \dots + 30.8189u + 18.9851 \\ -1.32415u^{65} - 2.02616u^{64} + \dots - 2.81894u - 3.05516 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -8.35519u^{65} - 13.0721u^{64} + \dots - 33.0049u - 20.9573 \\ 2.39639u^{65} + 3.80632u^{64} + \dots + 8.95306u + 5.31162 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 9.70575u^{65} + 15.5979u^{64} + \dots + 36.1966u + 23.0110 \\ -3.81358u^{65} - 6.82103u^{64} + \dots - 15.8119u - 9.70575 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 9.70575u^{65} + 15.5979u^{64} + \dots + 36.1966u + 23.0110 \\ -3.81358u^{65} - 6.82103u^{64} + \dots - 15.8119u - 9.70575 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.893203 - 0.332658I$ $a = -1.067726 - 0.068534I$ $b = 0.060619 + 0.632472I$	$0.93680 - 1.27321I$	$6.69528 + 2.55768I$
$u = -0.893203 + 0.332658I$ $a = -1.067726 + 0.068534I$ $b = 0.060619 - 0.632472I$	$0.93680 + 1.27321I$	$6.69528 - 2.55768I$
$u = -0.886940 - 0.437138I$ $a = -1.43804 - 0.06126I$ $b = 0.278206 + 1.239242I$	$6.34153 - 10.49840I$	$7.22778 + 5.33949I$
$u = -0.886940 + 0.437138I$ $a = -1.43804 + 0.06126I$ $b = 0.278206 - 1.239242I$	$6.34153 + 10.49840I$	$7.22778 - 5.33949I$
$u = -0.789339 - 0.681407I$ $a = -0.170305 + 0.711151I$ $b = 0.612194 - 0.634929I$	$1.79345 + 2.44057I$	$6.79170 - 5.63627I$
$u = -0.789339 + 0.681407I$ $a = -0.170305 - 0.711151I$ $b = 0.612194 + 0.634929I$	$1.79345 - 2.44057I$	$6.79170 + 5.63627I$
$u = -0.742966 - 0.521978I$ $a = 0.391741 + 1.288387I$ $b = 0.73070 - 1.45249I$	$9.13813 - 4.00163I$	$10.02198 + 1.95783I$
$u = -0.742966 + 0.521978I$ $a = 0.391741 - 1.288387I$ $b = 0.73070 + 1.45249I$	$9.13813 + 4.00163I$	$10.02198 - 1.95783I$
$u = -0.648304 - 1.133232I$ $a = -0.040925 + 1.149182I$ $b = 1.78851 - 1.92707I$	$4.2340 + 16.1582I$	$4.67083 - 9.06843I$
$u = -0.648304 + 1.133232I$ $a = -0.040925 - 1.149182I$ $b = 1.78851 + 1.92707I$	$4.2340 - 16.1582I$	$4.67083 + 9.06843I$

Solution to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.640786 - 0.965266I$ $a = -0.478037 - 0.069398I$ $b = -0.261638 + 0.444397I$	$0.94099 + 2.93508I$	$4.73839 - 0.63684I$
$u = -0.640786 + 0.965266I$ $a = -0.478037 + 0.069398I$ $b = -0.261638 - 0.444397I$	$0.94099 - 2.93508I$	$4.73839 + 0.63684I$
$u = -0.627293 - 1.165176I$ $a = -0.102093 + 0.901979I$ $b = 1.22622 - 1.56395I$	$-1.53699 + 6.84958I$	$2.00507 - 5.82058I$
$u = -0.627293 + 1.165176I$ $a = -0.102093 - 0.901979I$ $b = 1.22622 + 1.56395I$	$-1.53699 - 6.84958I$	$2.00507 + 5.82058I$
$u = -0.618729 - 1.050954I$ $a = -1.057994 - 0.338143I$ $b = -0.12777 + 1.65559I$	$7.56649 + 9.18924I$	$7.11738 - 7.19339I$
$u = -0.618729 + 1.050954I$ $a = -1.057994 + 0.338143I$ $b = -0.12777 - 1.65559I$	$7.56649 - 9.18924I$	$7.11738 + 7.19339I$
$u = -0.516301 - 1.034956I$ $a = -0.396217 - 1.250801I$ $b = -1.66301 + 1.61916I$	$1.42288 + 7.01342I$	$2.46904 - 8.54237I$
$u = -0.516301 + 1.034956I$ $a = -0.396217 + 1.250801I$ $b = -1.66301 - 1.61916I$	$1.42288 - 7.01342I$	$2.46904 + 8.54237I$
$u = -0.503518 - 0.347045I$ $a = 1.95488 + 0.23615I$ $b = -0.551149 - 1.270422I$	$3.23237 - 2.81118I$	$6.49138 + 3.43190I$
$u = -0.503518 + 0.347045I$ $a = 1.95488 - 0.23615I$ $b = -0.551149 + 1.270422I$	$3.23237 + 2.81118I$	$6.49138 - 3.43190I$

Solution to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.477372 - 0.943179I$ $a = 0.324367 - 0.983761I$ $b = -1.73724 + 2.48467I$	$-2.01954 + 2.54235I$	$9.35040 + 6.65492I$
$u = -0.477372 + 0.943179I$ $a = 0.324367 + 0.983761I$ $b = -1.73724 - 2.48467I$	$-2.01954 - 2.54235I$	$9.35040 - 6.65492I$
$u = -0.427074$ $a = -0.433828$ $b = -0.336075$	0.801791	12.7100
$u = -0.422028 - 1.013152I$ $a = 0.42251 - 1.48918I$ $b = -1.47500 + 1.02933I$	$-0.83525 + 3.14253I$	$-0.65111 - 4.39876I$
$u = -0.422028 + 1.013152I$ $a = 0.42251 + 1.48918I$ $b = -1.47500 - 1.02933I$	$-0.83525 - 3.14253I$	$-0.65111 + 4.39876I$
$u = -0.407213$ $a = 3.44853$ $b = -1.05852$	1.47039	6.43281
$u = -0.386686 - 0.758034I$ $a = 0.593747 - 0.711855I$ $b = 0.586006 - 1.214527I$	$-1.32206 + 1.19867I$	$-0.30232 - 8.95765I$
$u = -0.386686 + 0.758034I$ $a = 0.593747 + 0.711855I$ $b = 0.586006 + 1.214527I$	$-1.32206 - 1.19867I$	$-0.30232 + 8.95765I$
$u = -0.301350 - 0.971582I$ $a = 1.01800 - 1.10633I$ $b = -0.559633 - 0.170616I$	$0.012797 - 0.793621I$	$-0.540072 + 0.843099I$
$u = -0.301350 + 0.971582I$ $a = 1.01800 + 1.10633I$ $b = -0.559633 + 0.170616I$	$0.012797 + 0.793621I$	$-0.540072 - 0.843099I$

Solution to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.263360 - 1.365466I$ $a = -0.207188 + 0.642987I$ $b = 0.127253 - 0.960247I$	$-4.52691 + 2.53329I$	$9.64246 + 10.16006I$
$u = -0.263360 + 1.365466I$ $a = -0.207188 - 0.642987I$ $b = 0.127253 + 0.960247I$	$-4.52691 - 2.53329I$	$9.64246 - 10.16006I$
$u = -0.073346 - 1.249265I$ $a = -0.459853 + 0.956008I$ $b = -0.043571 - 0.947032I$	$0.33897 - 7.84486I$	$1.41108 + 5.52703I$
$u = -0.073346 + 1.249265I$ $a = -0.459853 - 0.956008I$ $b = -0.043571 + 0.947032I$	$0.33897 + 7.84486I$	$1.41108 - 5.52703I$
$u = 0.010647 - 0.950386I$ $a = 0.878581 - 0.110969I$ $b = 0.018046 - 0.954751I$	$4.00663 - 3.04870I$	$3.98275 + 2.96326I$
$u = 0.010647 + 0.950386I$ $a = 0.878581 + 0.110969I$ $b = 0.018046 + 0.954751I$	$4.00663 + 3.04870I$	$3.98275 - 2.96326I$
$u = 0.104431 - 1.298246I$ $a = 0.292746 + 0.847286I$ $b = -0.003012 - 0.940640I$	$-5.91703 + 3.42293I$	$-2.52268 - 7.14492I$
$u = 0.104431 + 1.298246I$ $a = 0.292746 - 0.847286I$ $b = -0.003012 + 0.940640I$	$-5.91703 - 3.42293I$	$-2.52268 + 7.14492I$
$u = 0.127139 - 0.784024I$ $a = -0.776775 - 0.573919I$ $b = -0.042614 - 0.780889I$	$-1.72069 + 1.07315I$	$-1.43813 - 5.39557I$
$u = 0.127139 + 0.784024I$ $a = -0.776775 + 0.573919I$ $b = -0.042614 + 0.780889I$	$-1.72069 - 1.07315I$	$-1.43813 + 5.39557I$

Solution to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.308392 - 0.295184I$ $a = -2.16318 - 0.94286I$ $b = 0.436188 - 0.731540I$	$-1.70503 + 0.88678I$	$-1.07228 - 2.74548I$
$u = 0.308392 + 0.295184I$ $a = -2.16318 + 0.94286I$ $b = 0.436188 + 0.731540I$	$-1.70503 - 0.88678I$	$-1.07228 + 2.74548I$
$u = 0.372330 - 0.966152I$ $a = -0.71705 - 1.22172I$ $b = 0.635335 + 0.613059I$	$-4.16615 - 1.29044I$	$-6.42044 + 1.41575I$
$u = 0.372330 + 0.966152I$ $a = -0.71705 + 1.22172I$ $b = 0.635335 - 0.613059I$	$-4.16615 + 1.29044I$	$-6.42044 - 1.41575I$
$u = 0.490775 - 1.009753I$ $a = 0.050202 - 1.234535I$ $b = 1.73077 + 1.49983I$	$-3.33981 - 4.65284I$	$-3.86882 + 8.36996I$
$u = 0.490775 + 1.009753I$ $a = 0.050202 + 1.234535I$ $b = 1.73077 - 1.49983I$	$-3.33981 + 4.65284I$	$-3.86882 - 8.36996I$
$u = 0.496332 - 0.710814I$ $a = -0.254141 - 0.800937I$ $b = 0.81193 - 2.11193I$	$4.10544 - 2.40688I$	$5.61601 + 0.93346I$
$u = 0.496332 + 0.710814I$ $a = -0.254141 + 0.800937I$ $b = 0.81193 + 2.11193I$	$4.10544 + 2.40688I$	$5.61601 - 0.93346I$
$u = 0.538866 - 0.909098I$ $a = -0.472812 - 0.706075I$ $b = 5.56489 - 0.30058I$	$3.51441 - 1.89915I$	$-6.74058 + 10.60084I$
$u = 0.538866 + 0.909098I$ $a = -0.472812 + 0.706075I$ $b = 5.56489 + 0.30058I$	$3.51441 + 1.89915I$	$-6.74058 - 10.60084I$

Solution to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.564876 - 1.135128I$ $a = -0.073078 + 0.707525I$ $b = -0.58777 - 1.86360I$	$6.26544 - 3.61924I$	$7.55383 + 5.69986I$
$u = 0.564876 + 1.135128I$ $a = -0.073078 - 0.707525I$ $b = -0.58777 + 1.86360I$	$6.26544 + 3.61924I$	$7.55383 - 5.69986I$
$u = 0.612668 - 1.023978I$ $a = 0.794130 - 0.357693I$ $b = 0.395162 + 1.268381I$	$1.33847 - 6.45954I$	$4.27383 + 8.40284I$
$u = 0.612668 + 1.023978I$ $a = 0.794130 + 0.357693I$ $b = 0.395162 - 1.268381I$	$1.33847 + 6.45954I$	$4.27383 - 8.40284I$
$u = 0.644245 - 1.145513I$ $a = 0.094859 + 1.051465I$ $b = -1.59384 - 1.71257I$	$-2.16297 - 12.09952I$	$1.13718 + 9.18819I$
$u = 0.644245 + 1.145513I$ $a = 0.094859 - 1.051465I$ $b = -1.59384 + 1.71257I$	$-2.16297 + 12.09952I$	$1.13718 - 9.18819I$
$u = 0.706967 - 0.574992I$ $a = -0.344274 + 0.907805I$ $b = -0.497576 - 1.179167I$	$2.68558 + 1.37819I$	$7.68512 - 2.61183I$
$u = 0.706967 + 0.574992I$ $a = -0.344274 - 0.907805I$ $b = -0.497576 + 1.179167I$	$2.68558 - 1.37819I$	$7.68512 + 2.61183I$
$u = 0.721856 - 1.027072I$ $a = 0.704898 + 0.295214I$ $b = -0.614618 + 0.468031I$	$6.10958 + 0.48289I$	$8.03921 - 2.23159I$
$u = 0.721856 + 1.027072I$ $a = 0.704898 - 0.295214I$ $b = -0.614618 - 0.468031I$	$6.10958 - 0.48289I$	$8.03921 + 2.23159I$

Solution to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.747809 - 0.382078I$	$8.51869 - 1.38556I$	$10.68003 + 0.04077I$
$a = 0.982939 - 0.436312I$		
$b = 0.605214 + 0.686874I$		
$u = 0.747809 + 0.382078I$	$8.51869 + 1.38556I$	$10.68003 - 0.04077I$
$a = 0.982939 + 0.436312I$		
$b = 0.605214 - 0.686874I$		
$u = 0.861313 - 0.608674I$	$7.36680 - 6.32316I$	$8.51632 + 6.52961I$
$a = 0.420830 + 0.985449I$		
$b = -1.035075 - 0.573403I$		
$u = 0.861313 + 0.608674I$	$7.36680 + 6.32316I$	$8.51632 - 6.52961I$
$a = 0.420830 - 0.985449I$		
$b = -1.035075 + 0.573403I$		
$u = 0.900019 - 0.409306I$	$0.06237 + 6.42817I$	$3.87818 - 5.79651I$
$a = 1.287907 - 0.018413I$		
$b = -0.259301 + 0.971541I$		
$u = 0.900019 + 0.409306I$	$0.06237 - 6.42817I$	$3.87818 + 5.79651I$
$a = 1.287907 + 0.018413I$		
$b = -0.259301 - 0.971541I$		

III. u-Polynomials

Crossings	u-Polynomials at each crossings
c_1	$(u^3 + u^2 + 2u + 1)(u^{66} + 2u^{65} + \dots + 4u + 1)$
c_2	$(u^3 + 3u^2 + 2u - 1)(u^{66} + 30u^{65} + \dots + 2u + 1)$
c_3	$(u^3 + u^2 - 1)(u^{66} + 2u^{65} + \dots - u^2 - 1)$
c_4	$(u^3 + u^2 - 1)(u^{66} + 2u^{65} + \dots - u^2 - 1)$
c_5	$(u^3 - u^2 + 2u - 1)(u^{66} + 2u^{65} + \dots + 4u + 1)$
c_6	$(u - 1)^3(u^{66} + 4u^{65} + \dots - 491u - 49)$
c_7	$(7u^3 + u^2 - 4u + 1)(7u^{66} + 18u^{65} + \dots - 13446u - 999)$
c_8	$(7u^3 - u^2 + u + 1)(7u^{66} + 10u^{65} + \dots - 1391u + 241)$
c_9	$(u + 1)^3(u^{66} + 4u^{65} + \dots - 491u - 49)$
c_{10}	$(u^3 - u^2 + 1)(u^{66} + 2u^{65} + \dots - u^2 - 1)$
c_{11}	$u^3(u^{66} + 5u^{65} + \dots + 3108u + 392)$

IV. Riley Polynomials

Crossings	Riley Polynomials at each crossings
c_1, c_5	$(y^3 + 3y^2 + 2y - 1)(y^{66} + 30y^{65} + \dots + 2y + 1)$
c_2	$(y^3 - 5y^2 + 10y - 1)(y^{66} + 14y^{65} + \dots + 14y + 1)$
c_3	$(y^3 - y^2 + 2y - 1)(y^{66} - 62y^{65} + \dots + 2y + 1)$
c_4	$(y^3 - y^2 + 2y - 1)(y^{66} - 62y^{65} + \dots + 2y + 1)$
c_6	$(y - 1)^3(y^{66} - 36y^{65} + \dots - 105155y + 2401)$
c_7	$(49y^3 - 57y^2 + 14y - 1)$ $(49y^{66} + 2434y^{65} + \dots - 82043766y + 998001)$
c_8	$(49y^3 + 13y^2 + 3y - 1)(49y^{66} + 880y^{65} + \dots - 442127y + 58081)$
c_9	$(y - 1)^3(y^{66} - 36y^{65} + \dots - 105155y + 2401)$
c_{10}	$(y^3 - y^2 + 2y - 1)(y^{66} - 62y^{65} + \dots + 2y + 1)$
c_{11}	$y^3(y^{66} - 21y^{65} + \dots - 925904y + 153664)$