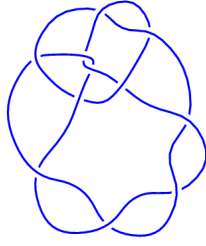
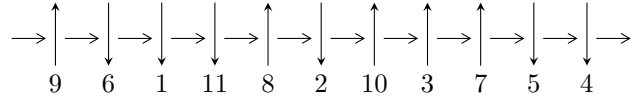


11a₃₂₃ (K11a₃₂₃)

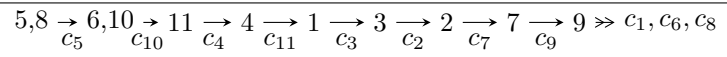


1

Arc Sequences



Solving Sequence



Representation Ideals

$$I = \bigcap_{i=1}^2 I_i^u$$

$$I_1^u = \langle 5u^3 + 7u^2 + 4u + 1, 5u^2 + a + 7u + 4, 5u^2 + b + 7u + 3 \rangle$$

$$I_2^u = \langle 5u^{44} - 2u^{43} + \dots + 23513u + 5383,$$

$$1.87940 \times 10^{129}u^{43} - 2.53353 \times 10^{129}u^{42} + \dots + 3.49617 \times 10^{129}b + 2.14240 \times 10^{132},$$

$$- 6.80107 \times 10^{133}u^{43} + 9.67201 \times 10^{133}u^{42} + \dots + 9.40995 \times 10^{133}a - 7.19988 \times 10^{136} \rangle$$

There are 2 irreducible components with 47 representations.

¹The knot diagram image is adapter from “C. Livingston and A. H. Moore, KnotInfo: Table of Knot Invariants, <http://www.indiana.edu/~knotinfo>”

$$\text{I. } I_1^u = \langle 5u^3 + 7u^2 + 4u + 1, 5u^2 + a + 7u + 4, 5u^2 + b + 7u + 3 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -5u^2 - 7u - 4 \\ -5u^2 - 7u - 3 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -1 \\ -5u^2 - 7u - 3 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -5u^2 - 7u - 2 \\ -10u^2 - 9u - 2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -5u^2 - 2u \\ -5u^2 - 2u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ -5u^2 - 2u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -5u^2 - 2u \\ -2u^2 + u + 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 5u^2 + 7u + 4 \\ 5u^2 + 8u + 3 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.637007$ $a = -1.56984$ $b = -0.569840$	0.531480	-3.13592
$u = -0.381496 - 0.410401I$ $a = -1.21508 + 1.30714I$ $b = -0.215080 + 1.307141I$	$4.66906 + 2.82812I$	$9.94796 - 2.62108I$
$u = -0.381496 + 0.410401I$ $a = -1.21508 - 1.30714I$ $b = -0.215080 - 1.307141I$	$4.66906 - 2.82812I$	$9.94796 + 2.62108I$

$$\text{II. } I_2^u = \langle 5u^{44} - 2u^{43} + \dots + 23513u + 5383, 1.88 \times 10^{129}u^{43} - 2.53 \times 10^{129}u^{42} + \dots + 3.50 \times 10^{129}b + 2.14 \times 10^{132}, -6.80 \times 10^{133}u^{43} + 9.67 \times 10^{133}u^{42} + \dots + 9.41 \times 10^{133}a - 7.20 \times 10^{136} \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.722752u^{43} - 1.02785u^{42} + \dots + 2586.58u + 765.134 \\ -0.537558u^{43} + 0.724658u^{42} + \dots - 2021.84u - 612.784 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1.26031u^{43} - 1.75251u^{42} + \dots + 4608.42u + 1377.92 \\ -0.537558u^{43} + 0.724658u^{42} + \dots - 2021.84u - 612.784 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -0.0515498u^{43} - 0.0263977u^{42} + \dots - 443.995u - 166.981 \\ -0.411238u^{43} + 0.637229u^{42} + \dots - 1344.60u - 383.990 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.784662u^{43} + 1.16662u^{42} + \dots - 2663.67u - 762.790 \\ 1.01355u^{43} - 1.47148u^{42} + \dots + 3540.83u + 1033.08 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -0.653754u^{43} + 0.913813u^{42} + \dots - 2393.61u - 721.619 \\ 0.411203u^{43} - 0.631638u^{42} + \dots + 1350.46u + 384.109 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.907644u^{43} + 1.23871u^{42} + \dots - 3406.87u - 1039.79 \\ 0.613833u^{43} - 0.903617u^{42} + \dots + 2127.42u + 624.562 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.293195u^{43} + 0.309363u^{42} + \dots - 1323.05u - 426.247 \\ 0.425716u^{43} - 0.569926u^{42} + \dots + 1625.33u + 498.237 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -0.329464u^{43} + 0.326857u^{42} + \dots - 1567.67u - 522.281 \\ -0.517227u^{43} + 0.801484u^{42} + \dots - 1666.33u - 464.586 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -0.329464u^{43} + 0.326857u^{42} + \dots - 1567.67u - 522.281 \\ -0.517227u^{43} + 0.801484u^{42} + \dots - 1666.33u - 464.586 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.76327 - 0.92521I$		
$a = 0.820451 - 0.133626I$	$18.5526 + 13.4473I$	$7.67631 - 6.21892I$
$b = 0.15119 - 1.69109I$		
$u = -1.76327 + 0.92521I$		
$a = 0.820451 + 0.133626I$	$18.5526 - 13.4473I$	$7.67631 + 6.21892I$
$b = 0.15119 + 1.69109I$		
$u = -1.47948 - 0.71625I$		
$a = 0.922862 - 0.156791I$	$9.4938 + 10.7466I$	$6.37940 - 7.40860I$
$b = 0.531615 - 0.932164I$		
$u = -1.47948 + 0.71625I$		
$a = 0.922862 + 0.156791I$	$9.4938 - 10.7466I$	$6.37940 + 7.40860I$
$b = 0.531615 + 0.932164I$		
$u = -1.44023 - 0.74181I$		
$a = -0.605643 + 0.449292I$	$4.32587 - 0.97456I$	$-0.21065 + 1.62578I$
$b = -0.265508 - 0.254499I$		
$u = -1.44023 + 0.74181I$		
$a = -0.605643 - 0.449292I$	$4.32587 + 0.97456I$	$-0.21065 - 1.62578I$
$b = -0.265508 + 0.254499I$		
$u = -1.210861 - 0.409862I$		
$a = 1.105903 - 0.132214I$	$6.50673 + 6.32792I$	$4.03492 - 4.79564I$
$b = 0.797364 - 0.047017I$		
$u = -1.210861 + 0.409862I$		
$a = 1.105903 + 0.132214I$	$6.50673 - 6.32792I$	$4.03492 + 4.79564I$
$b = 0.797364 + 0.047017I$		
$u = -1.196397 - 0.475903I$		
$a = 1.076943 - 0.370447I$	$17.9861 + 1.4504I$	$9.54859 - 0.45700I$
$b = 0.17519 - 1.69800I$		
$u = -1.196397 + 0.475903I$		
$a = 1.076943 + 0.370447I$	$17.9861 - 1.4504I$	$9.54859 + 0.45700I$
$b = 0.17519 + 1.69800I$		

Solution to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.128223 - 0.022553I$ $a = 1.232015 - 0.124519I$ $b = 0.604409 - 0.897873I$	$9.03616 - 1.64979I$	$8.22123 + 0.49453I$
$u = -1.128223 + 0.022553I$ $a = 1.232015 + 0.124519I$ $b = 0.604409 + 0.897873I$	$9.03616 + 1.64979I$	$8.22123 - 0.49453I$
$u = -1.047697 - 0.043518I$ $a = -0.233660 - 0.845090I$ $b = -0.06818 + 1.63407I$	$8.58047 + 3.25505I$	$1.41297 - 2.89644I$
$u = -1.047697 + 0.043518I$ $a = -0.233660 + 0.845090I$ $b = -0.06818 - 1.63407I$	$8.58047 - 3.25505I$	$1.41297 + 2.89644I$
$u = -0.872611 - 0.476152I$ $a = -2.00665 + 0.23740I$ $b = -0.02340 + 1.67896I$	$16.7506 + 2.5780I$	$11.49091 - 2.59989I$
$u = -0.872611 + 0.476152I$ $a = -2.00665 - 0.23740I$ $b = -0.02340 - 1.67896I$	$16.7506 - 2.5780I$	$11.49091 + 2.59989I$
$u = -0.822646 - 0.066084I$ $a = -1.97484 - 0.53323I$ $b = -0.102848 + 0.888493I$	$7.69062 + 2.11031I$	$11.34242 - 3.52324I$
$u = -0.822646 + 0.066084I$ $a = -1.97484 + 0.53323I$ $b = -0.102848 - 0.888493I$	$7.69062 - 2.11031I$	$11.34242 + 3.52324I$
$u = -0.537650 - 0.192122I$ $a = -0.457711 - 0.938356I$ $b = -0.305152 + 0.698148I$	$0.43661 + 1.95503I$	$-1.24229 - 4.92252I$
$u = -0.537650 + 0.192122I$ $a = -0.457711 + 0.938356I$ $b = -0.305152 - 0.698148I$	$0.43661 - 1.95503I$	$-1.24229 + 4.92252I$

Solution to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.053641 - 0.448598I$ $a = -0.521545 - 0.685854I$ $b = -0.454810 - 0.226491I$	$-0.971761 - 0.735222I$	$-7.08962 + 4.08922I$
$u = -0.053641 + 0.448598I$ $a = -0.521545 + 0.685854I$ $b = -0.454810 + 0.226491I$	$-0.971761 + 0.735222I$	$-7.08962 - 4.08922I$
$u = 0.139758 - 0.614578I$ $a = -0.160320 - 1.052852I$ $b = -0.151472 - 1.375049I$	$4.06071 - 2.79744I$	$-3.56462 + 2.17151I$
$u = 0.139758 + 0.614578I$ $a = -0.160320 + 1.052852I$ $b = -0.151472 + 1.375049I$	$4.06071 + 2.79744I$	$-3.56462 - 2.17151I$
$u = 0.676797 - 0.789439I$ $a = 0.669794 - 0.315046I$ $b = 0.458929 + 0.000125I$	$1.39676 - 2.58910I$	$-1.63153 + 3.81812I$
$u = 0.676797 + 0.789439I$ $a = 0.669794 + 0.315046I$ $b = 0.458929 - 0.000125I$	$1.39676 + 2.58910I$	$-1.63153 - 3.81812I$
$u = 0.692318$ $a = 1.29930$ $b = 0.195443$	1.30800	9.71570
$u = 0.853036 - 0.630068I$ $a = 0.893505 - 0.709277I$ $b = 0.305076 + 0.810839I$	$3.79818 - 5.24105I$	$5.59410 + 7.80794I$
$u = 0.853036 + 0.630068I$ $a = 0.893505 + 0.709277I$ $b = 0.305076 - 0.810839I$	$3.79818 + 5.24105I$	$5.59410 - 7.80794I$
$u = 0.991990$ $a = -1.25628$ $b = -0.872602$	1.65108	6.63726

Solution to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00442 - 1.04123I$		
$a = 0.298026 + 0.116607I$	$3.43037 - 0.37049I$	$6.62918 - 1.94701I$
$b = 0.204088 - 0.682624I$		
$u = 1.00442 + 1.04123I$		
$a = 0.298026 - 0.116607I$	$3.43037 + 0.37049I$	$6.62918 + 1.94701I$
$b = 0.204088 + 0.682624I$		
$u = 1.08878 - 0.92273I$		
$a = 0.691482 + 0.380811I$	$3.38183 - 0.95789I$	$3.69098 - 0.13410I$
$b = 0.081349 + 0.763523I$		
$u = 1.08878 + 0.92273I$		
$a = 0.691482 - 0.380811I$	$3.38183 + 0.95789I$	$3.69098 + 0.13410I$
$b = 0.081349 - 0.763523I$		
$u = 1.122747 - 0.475891I$		
$a = 0.750971 - 0.997825I$	$12.42892 - 6.64650I$	$7.33511 + 5.68449I$
$b = 0.07456 + 1.65915I$		
$u = 1.122747 + 0.475891I$		
$a = 0.750971 + 0.997825I$	$12.42892 + 6.64650I$	$7.33511 - 5.68449I$
$b = 0.07456 - 1.65915I$		
$u = 1.128906 - 0.495735I$		
$a = -1.031717 - 0.274472I$	$4.65109 - 4.83905I$	$5.90617 + 6.05459I$
$b = -0.570126 - 0.967451I$		
$u = 1.128906 + 0.495735I$		
$a = -1.031717 + 0.274472I$	$4.65109 + 4.83905I$	$5.90617 - 6.05459I$
$b = -0.570126 + 0.967451I$		
$u = 1.33011 - 1.63777I$		
$a = 0.489092 + 0.377327I$	$11.90429 - 1.28750I$	$3.23124 + 0.95491I$
$b = 0.01583 + 1.65226I$		
$u = 1.33011 + 1.63777I$		
$a = 0.489092 - 0.377327I$	$11.90429 + 1.28750I$	$3.23124 - 0.95491I$
$b = 0.01583 - 1.65226I$		

Solution to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.41376 - 0.86384I$ $a = -0.845394 - 0.270995I$ $b = -0.15533 - 1.70224I$	$13.8777 - 7.6987I$	$5.79500 + 4.46382I$
$u = 1.41376 + 0.86384I$ $a = -0.845394 + 0.270995I$ $b = -0.15533 + 1.70224I$	$13.8777 + 7.6987I$	$5.79500 - 4.46382I$
$u = 2.15224 - 1.06636I$ $a = 0.162714 + 0.175006I$ $b = 0.03581 - 1.62441I$	$11.45345 + 0.37506I$	$8.09368 + 2.16495I$
$u = 2.15224 + 1.06636I$ $a = 0.162714 - 0.175006I$ $b = 0.03581 + 1.62441I$	$11.45345 - 0.37506I$	$8.09368 - 2.16495I$

III. u-Polynomials

Crossings	u-Polynomials at each crossings
c_1	$(5u^3 + 4u^2 - u - 1)(5u^{44} + 21u^{43} + \dots - 864u + 823)$
c_2	$(u^3 + u^2 - 1)(u^{44} + 2u^{43} + \dots + u - 1)$
c_3, c_4	$(u^3 + u^2 + 2u + 1)(u^{44} + 2u^{43} + \dots - 5u - 1)$
c_5	$(5u^3 + 7u^2 + 4u + 1)(5u^{44} + 2u^{43} + \dots - 23513u + 5383)$
c_6	$(u^3 - u^2 + 1)(u^{44} + 2u^{43} + \dots + u - 1)$
c_7	$(u + 1)^3(u^{44} + 4u^{43} + \dots + 16u - 25)$
c_8	$u^3(u^{44} + u^{43} + \dots - 220u + 200)$
c_9	$(u - 1)^3(u^{44} + 4u^{43} + \dots + 16u - 25)$
c_{10}, c_{11}	$(u^3 - u^2 + 2u - 1)(u^{44} + 2u^{43} + \dots - 5u - 1)$

IV. Riley Polynomials

Crossings	Riley Polynomials at each crossings
c_1	$(25y^3 - 26y^2 + 9y - 1)(25y^{44} - 671y^{43} + \dots - 2153826y + 677329)$
c_2, c_6	$(y^3 - y^2 + 2y - 1)(y^{44} + 30y^{43} + \dots - 23y + 1)$
c_3, c_4, c_{10} c_{11}	$(y^3 + 3y^2 + 2y - 1)(y^{44} + 54y^{43} + \dots - 23y + 1)$
c_5	$(25y^3 - 9y^2 + 2y - 1)$ $(25y^{44} - 914y^{43} + \dots - 198282959y + 28976689)$
c_7, c_9	$(y - 1)^3(y^{44} - 40y^{43} + \dots - 9756y + 625)$
c_8	$y^3(y^{44} - 21y^{43} + \dots - 482000y + 40000)$