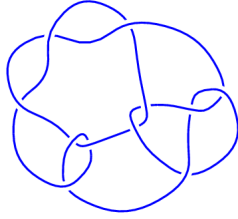
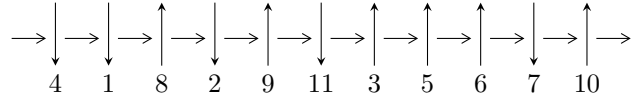


11a₃₃ (K11a₃₃)

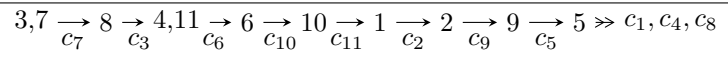


1

Arc Sequences



Solving Sequence



Representation Ideals

$$I = I_1^u \cap I_1^v$$

$$I_1^u = \langle u^{52} + u^{51} + \dots - 232u^2 + 32, \\ - 2.80455 \times 10^{71}u^{51} - 8.84488 \times 10^{70}u^{50} + \dots + 1.82929 \times 10^{71}a - 1.41514 \times 10^{73}, \\ - 3.59162 \times 10^{71}u^{51} - 6.81177 \times 10^{70}u^{50} + \dots + 3.65857 \times 10^{71}b - 1.51817 \times 10^{73} \rangle$$

$$I_1^v = \langle b^5 + 2b^4 + 3b^3 + 2b^2 + 2b + 1, -b^4 - 2b^3 - 3b^2 - b + v - 1, a \rangle$$

There are 2 irreducible components with 57 representations.

¹The knot diagram image is adapter from “C. Livingston and A. H. Moore, KnotInfo: Table of Knot Invariants, <http://www.indiana.edu/~knotinfo>”

$$\mathbf{I. } I_1^u = \langle u^{52} + u^{51} + \dots - 232u^2 + 32, -2.80 \times 10^{71} u^{51} - 8.84 \times 10^{70} u^{50} + \dots + 1.83 \times 10^{71} a - 1.42 \times 10^{73}, -3.59 \times 10^{71} u^{51} - 6.81 \times 10^{70} u^{50} + \dots + 3.66 \times 10^{71} b - 1.52 \times 10^{73} \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1.53314u^{51} + 0.483515u^{50} + \dots - 115.343u + 77.3601 \\ 0.981700u^{51} + 0.186187u^{50} + \dots - 59.2802u + 41.4962 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1.19425u^{51} + 0.481246u^{50} + \dots - 105.268u + 66.6624 \\ -0.198263u^{51} + 0.0892578u^{50} + \dots + 14.3724u - 11.3632 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1.53314u^{51} + 0.483515u^{50} + \dots - 115.343u + 77.3601 \\ 0.291067u^{51} + 0.0291784u^{50} + \dots - 10.2198u + 7.90835 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0.196295u^{51} - 0.00549239u^{50} + \dots - 23.5061u + 20.3598 \\ -0.117453u^{51} - 0.0692387u^{50} + \dots + 9.18679u - 4.42523 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.154147u^{51} - 0.0397948u^{50} + \dots - 20.0268u + 17.5330 \\ -0.241668u^{51} - 0.208983u^{50} + \dots + 11.8129u - 3.67724 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -0.828488u^{51} - 0.493482u^{50} + \dots + 70.9484u - 33.7554 \\ 0.125795u^{51} - 0.105171u^{50} + \dots - 13.0041u + 13.1784 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -0.321903u^{51} - 0.139407u^{50} + \dots + 26.4114u - 18.3279 \\ -0.125608u^{51} - 0.144899u^{50} + \dots + 2.90533u + 2.03198 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -0.321903u^{51} - 0.139407u^{50} + \dots + 26.4114u - 18.3279 \\ -0.125608u^{51} - 0.144899u^{50} + \dots + 2.90533u + 2.03198 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.41956 - 0.37842I$		
$a = 0.592117 - 0.130057I$	$9.80914 + 2.73925I$	$5.98913 - 0.86649I$
$b = 0.891165 - 0.384837I$		
$u = -1.41956 + 0.37842I$		
$a = 0.592117 + 0.130057I$	$9.80914 - 2.73925I$	$5.98913 + 0.86649I$
$b = 0.891165 + 0.384837I$		
$u = -1.38824 - 0.60897I$		
$a = 0.593747 + 0.651040I$	$12.02741 + 4.30908I$	$7.47308 - 2.21383I$
$b = -0.27948 + 2.56319I$		
$u = -1.38824 + 0.60897I$		
$a = 0.593747 - 0.651040I$	$12.02741 - 4.30908I$	$7.47308 + 2.21383I$
$b = -0.27948 - 2.56319I$		
$u = -1.35988 - 0.65311I$		
$a = -0.058130 - 0.886872I$	$11.4963 + 13.8946I$	$6.59320 - 8.24119I$
$b = -0.39139 - 3.66290I$		
$u = -1.35988 + 0.65311I$		
$a = -0.058130 + 0.886872I$	$11.4963 - 13.8946I$	$6.59320 + 8.24119I$
$b = -0.39139 + 3.66290I$		
$u = -1.260839 - 0.032726I$		
$a = -0.218091 - 0.886432I$	$5.88940 - 2.23703I$	$9.81871 + 3.17171I$
$b = 0.07148 - 2.21557I$		
$u = -1.260839 + 0.032726I$		
$a = -0.218091 + 0.886432I$	$5.88940 + 2.23703I$	$9.81871 - 3.17171I$
$b = 0.07148 + 2.21557I$		
$u = -1.153569 - 0.455280I$		
$a = -0.577895 - 0.088468I$	$0.72885 + 5.40223I$	$0.76570 - 5.29849I$
$b = -0.123541 + 0.688937I$		
$u = -1.153569 + 0.455280I$		
$a = -0.577895 + 0.088468I$	$0.72885 - 5.40223I$	$0.76570 + 5.29849I$
$b = -0.123541 - 0.688937I$		

Solution to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.087850 - 0.046512I$ $a = 0.376309 - 1.154149I$ $b = 0.08249 - 3.57499I$	$6.39075 + 4.67632I$	$6.63994 - 3.34452I$
$u = -1.087850 + 0.046512I$ $a = 0.376309 + 1.154149I$ $b = 0.08249 + 3.57499I$	$6.39075 - 4.67632I$	$6.63994 + 3.34452I$
$u = -1.086042 - 0.309013I$ $a = -0.134864 + 1.017298I$ $b = 0.96499 + 2.04338I$	$4.31532 + 4.63289I$	$7.37710 - 5.03996I$
$u = -1.086042 + 0.309013I$ $a = -0.134864 - 1.017298I$ $b = 0.96499 - 2.04338I$	$4.31532 - 4.63289I$	$7.37710 + 5.03996I$
$u = -1.029524 - 0.333804I$ $a = 0.273111 - 0.744365I$ $b = -1.062748 - 0.265689I$	$-0.40755 + 4.20725I$	$0.31053 - 6.85372I$
$u = -1.029524 + 0.333804I$ $a = 0.273111 + 0.744365I$ $b = -1.062748 + 0.265689I$	$-0.40755 - 4.20725I$	$0.31053 + 6.85372I$
$u = -0.628086 - 0.011759I$ $a = -0.76361 - 1.86660I$ $b = 0.511707 - 0.778773I$	$5.00504 - 4.26604I$	$11.11018 + 2.65342I$
$u = -0.628086 + 0.011759I$ $a = -0.76361 + 1.86660I$ $b = 0.511707 + 0.778773I$	$5.00504 + 4.26604I$	$11.11018 - 2.65342I$
$u = -0.480287 - 0.488293I$ $a = -0.864357 - 0.262015I$ $b = -1.207531 + 0.101260I$	$-2.08809 - 0.78607I$	$-3.98062 - 1.52380I$
$u = -0.480287 + 0.488293I$ $a = -0.864357 + 0.262015I$ $b = -1.207531 - 0.101260I$	$-2.08809 + 0.78607I$	$-3.98062 + 1.52380I$

Solution to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.347952 - 0.680449I$ $a = -0.145116 - 0.640559I$ $b = -0.550550 - 0.741461I$	$-1.79468 - 0.95889I$	$-4.14280 + 1.57937I$
$u = -0.347952 + 0.680449I$ $a = -0.145116 + 0.640559I$ $b = -0.550550 + 0.741461I$	$-1.79468 + 0.95889I$	$-4.14280 - 1.57937I$
$u = -0.248057 - 1.187933I$ $a = -1.080896 + 0.174432I$ $b = 1.48256 + 0.53189I$	$7.94604 - 7.28946I$	$5.85423 + 5.70080I$
$u = -0.248057 + 1.187933I$ $a = -1.080896 - 0.174432I$ $b = 1.48256 - 0.53189I$	$7.94604 + 7.28946I$	$5.85423 - 5.70080I$
$u = -0.169899 - 1.183751I$ $a = 0.977658 + 0.522136I$ $b = -1.24731 + 0.93979I$	$8.11586 + 2.13977I$	$6.28937 - 0.51740I$
$u = -0.169899 + 1.183751I$ $a = 0.977658 - 0.522136I$ $b = -1.24731 - 0.93979I$	$8.11586 - 2.13977I$	$6.28937 + 0.51740I$
$u = 0.010942 - 0.814358I$ $a = 1.204071 - 0.360898I$ $b = -0.142030 - 0.656396I$	$0.986067 - 0.922209I$	$5.57805 + 0.78370I$
$u = 0.010942 + 0.814358I$ $a = 1.204071 + 0.360898I$ $b = -0.142030 + 0.656396I$	$0.986067 + 0.922209I$	$5.57805 - 0.78370I$
$u = 0.213178 - 1.155909I$ $a = 0.113479 + 0.723602I$ $b = -0.063002 + 0.215299I$	$4.28726 + 2.50747I$	$2.75724 - 2.68671I$
$u = 0.213178 + 1.155909I$ $a = 0.113479 - 0.723602I$ $b = -0.063002 - 0.215299I$	$4.28726 - 2.50747I$	$2.75724 + 2.68671I$

Solution to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.301724 - 0.398387I$ $a = 0.95370 - 1.34817I$ $b = 0.290241 - 0.488400I$	$0.450033 - 1.234717I$	$4.74084 + 5.50358I$
$u = 0.301724 + 0.398387I$ $a = 0.95370 + 1.34817I$ $b = 0.290241 + 0.488400I$	$0.450033 + 1.234717I$	$4.74084 - 5.50358I$
$u = 0.371907 - 0.887604I$ $a = -1.124251 - 0.005251I$ $b = 0.266407 - 0.850009I$	$-0.04250 + 4.54357I$	$1.88793 - 7.26372I$
$u = 0.371907 + 0.887604I$ $a = -1.124251 + 0.005251I$ $b = 0.266407 + 0.850009I$	$-0.04250 - 4.54357I$	$1.88793 + 7.26372I$
$u = 0.611417$ $a = 1.15720$ $b = -0.0192669$	1.69898	7.12316
$u = 0.723834 - 0.276102I$ $a = 0.016422 + 1.324742I$ $b = -0.61718 + 2.91051I$	$-0.88919 - 2.40502I$	$4.23135 + 7.49678I$
$u = 0.723834 + 0.276102I$ $a = 0.016422 - 1.324742I$ $b = -0.61718 - 2.91051I$	$-0.88919 + 2.40502I$	$4.23135 - 7.49678I$
$u = 0.961653 - 0.221131I$ $a = -0.684968 + 0.680475I$ $b = 0.961581 - 0.230355I$	$-0.0437779 + 0.0269953I$	$1.92084 - 0.19212I$
$u = 0.961653 + 0.221131I$ $a = -0.684968 - 0.680475I$ $b = 0.961581 + 0.230355I$	$-0.0437779 - 0.0269953I$	$1.92084 + 0.19212I$
$u = 1.035659 - 0.105451I$ $a = 0.619944 - 0.157919I$ $b = 0.049581 + 0.344007I$	$1.98030 - 0.48005I$	$3.97181 + 0.10468I$

Solution to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.035659 + 0.105451I$ $a = 0.619944 + 0.157919I$ $b = 0.049581 - 0.344007I$	$1.98030 + 0.48005I$	$3.97181 - 0.10468I$
$u = 1.04965$ $a = -0.808700$ $b = -1.42937$	2.68190	3.52272
$u = 1.187855 - 0.537240I$ $a = 0.033870 + 0.877672I$ $b = -1.29133 + 2.25907I$	$2.58119 - 9.82991I$	$3.68059 + 9.74649I$
$u = 1.187855 + 0.537240I$ $a = 0.033870 - 0.877672I$ $b = -1.29133 - 2.25907I$	$2.58119 + 9.82991I$	$3.68059 - 9.74649I$
$u = 1.279685 - 0.359861I$ $a = 0.348404 - 0.778179I$ $b = -0.14985 - 2.12750I$	$5.10574 - 3.32861I$	$8.68775 + 2.82645I$
$u = 1.279685 + 0.359861I$ $a = 0.348404 + 0.778179I$ $b = -0.14985 + 2.12750I$	$5.10574 + 3.32861I$	$8.68775 - 2.82645I$
$u = 1.35677 - 0.62431I$ $a = -0.557359 - 0.207593I$ $b = -0.855811 - 0.619829I$	$7.94022 - 8.91057I$	$3.69132 + 5.27448I$
$u = 1.35677 + 0.62431I$ $a = -0.557359 + 0.207593I$ $b = -0.855811 + 0.619829I$	$7.94022 + 8.91057I$	$3.69132 - 5.27448I$
$u = 1.43065 - 0.41648I$ $a = -0.079812 - 0.898014I$ $b = 0.36339 - 3.60048I$	$13.4799 - 7.6731I$	$8.99342 + 3.94688I$
$u = 1.43065 + 0.41648I$ $a = -0.079812 + 0.898014I$ $b = 0.36339 + 3.60048I$	$13.4799 + 7.6731I$	$8.99342 - 3.94688I$
Solution to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.45538 - 0.35264I$ $a = -0.487731 + 0.750918I$ $b = 0.27049 + 2.93111I$	$13.79828 + 1.96896I$	$9.43817 - 2.22913I$
$u = 1.45538 + 0.35264I$ $a = -0.487731 - 0.750918I$ $b = 0.27049 - 2.93111I$	$13.79828 - 1.96896I$	$9.43817 + 2.22913I$

$$\text{II. } I_1^v = \langle b^5 + 2b^4 + 3b^3 + 2b^2 + 2b + 1, -b^4 - 2b^3 - 3b^2 - b + v - 1, a \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} b^4 + 2b^3 + 3b^2 + b + 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} b^4 + 2b^3 + 3b^2 + b + 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ b \end{pmatrix}$$

$$a_6 = \begin{pmatrix} b^4 + 2b^3 + 3b^2 + b + 1 \\ b^3 + b^2 + b \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -b^4 - b^3 - b^2 + b \\ b \end{pmatrix}$$

$$a_1 = \begin{pmatrix} b^4 + 2b^3 + 2b^2 - 1 \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} b^4 + 2b^3 + 2b^2 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -b^4 - 2b^3 - 2b^2 + 1 \\ -b^4 - 2b^3 - 3b^2 - b - 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -b^4 - 2b^3 - 2b^2 + 1 \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -b^4 - 2b^3 - 2b^2 + 1 \\ 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_1^v	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = 0.309916 + 0.549911I$ $a = 0$ $b = -0.871221 - 1.107662I$	$-1.31583 + 1.53058I$	$0.02124 - 2.62456I$
$v = 0.309916 - 0.549911I$ $a = 0$ $b = -0.871221 + 1.107662I$	$-1.31583 - 1.53058I$	$0.02124 + 2.62456I$
$v = 1.21774$ $a = 0$ $b = -0.629714$	0.756147	-2.67610
$v = -1.41878 - 0.21917I$ $a = 0$ $b = 0.186078 - 0.874646I$	$4.22763 + 4.40083I$	$0.31681 - 3.97407I$
$v = -1.41878 + 0.21917I$ $a = 0$ $b = 0.186078 + 0.874646I$	$4.22763 - 4.40083I$	$0.31681 + 3.97407I$

III. u-Polynomials

Crossings	u-Polynomials at each crossings
c_1	$(u - 1)^5(u^{52} + 6u^{51} + \dots - 5u - 1)$
c_2	$(u + 1)^5(u^{52} + 22u^{51} + \dots - 11u + 1)$
c_3, c_7	$u^5(u^{52} + u^{51} + \dots - 232u^2 + 32)$
c_4	$(u + 1)^5(u^{52} + 6u^{51} + \dots - 5u - 1)$
c_5	$(u^5 - u^4 + \dots + u + 1)(u^{52} + 2u^{51} + \dots + 25u - 17)$
c_6	$(u^5 + u^4 + \dots + u + 1)(u^{52} + 2u^{51} + \dots - u - 1)$
c_8, c_9	$(u^5 + u^4 + \dots + u - 1)(u^{52} + 2u^{51} + \dots + 25u - 17)$
c_{10}	$(u^5 - u^4 + \dots + u - 1)(u^{52} + 2u^{51} + \dots - u - 1)$
c_{11}	$(u^5 - 3u^4 + \dots - u + 1)(u^{52} + 30u^{51} + \dots + 5u + 1)$

IV. Riley Polynomials

Crossings	Riley Polynomials at each crossings
c_1, c_4	$(y - 1)^5(y^{52} - 22y^{51} + \dots + 11y + 1)$
c_2	$(y - 1)^5(y^{52} + 22y^{51} + \dots - 349y + 1)$
c_3, c_7	$y^5(y^{52} - 33y^{51} + \dots - 14848y + 1024)$
c_5	1.000000000000000 $(1y^5 - 5.000000000000000y^4 + \dots - y - 1.000000000000000)$ $(1.00y^{52} - 58.0y^{51} + \dots - 2.29 \times 10^3y + 289.)$
c_6	1.000000000000000 $(1y^5 + 3.0000000000y^4 + \dots - y - 1.000000000000000)$ $(1y^{52} + 30.000000000y^{51} + \dots + 5.0000000000y + 1.000000000000000)$
c_8	$(y^5 - 5y^4 + \dots - y - 1)(y^{52} - 58y^{51} + \dots - 2291y + 289)$
c_9	1.000000000000000 $(1y^5 - 5.000000000000000y^4 + \dots - y - 1.000000000000000)$ $(1.00y^{52} - 58.0y^{51} + \dots - 2.29 \times 10^3y + 289.)$
c_{10}	$(y^5 + 3y^4 + \dots - y - 1)(y^{52} + 30y^{51} + \dots + 5y + 1)$
c_{11}	1.000000000000000 $(1y^5 - y^4 + \dots + 3.000000000000000y - 1.000000000000000)$ $(1.00y^{52} - 14.0y^{51} + \dots + 21.0y + 1.00)$