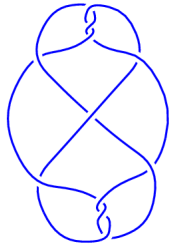
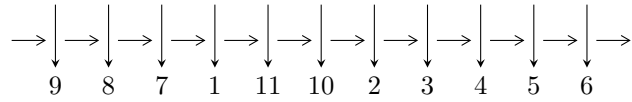


11a₃₅₇ (K11a₃₅₇)

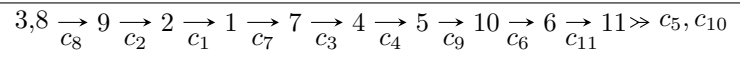


1

Arc Sequences



Solving Sequence



Representation Ideals

$$I = \bigcap_{i=1}^2 I_i^u$$

$$I_1^u = \langle u^9 - 4u^7 + 5u^5 + u^2 - 3u - 1 \rangle$$

$$I_2^u = \langle u^{36} - u^{35} + \dots - 4u^3 + 1 \rangle$$

There are 2 irreducible components with 45 representations.

¹The knot diagram image is adapter from “C. Livingston and A. H. Moore, KnotInfo: Table of Knot Invariants, <http://www.indiana.edu/~knotinfo>”

$$\text{I. } I_1^u = \langle u^9 - 4u^7 + 5u^5 + u^2 - 3u - 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^4 + u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^4 + u^2 + 1 \\ u^6 - 2u^4 + u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^7 - 2u^5 - u^4 + u^2 + u + 1 \\ -u^7 + u^6 + 3u^5 - 2u^4 - 2u^3 + u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^7 + 2u^5 - u^4 + u^2 - 2u \\ u^7 + u^6 - 3u^5 - 2u^4 + 2u^3 + u^2 + u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^8 + u^7 - 3u^6 - 2u^5 + 2u^4 + u^2 + 2u \\ -u^7 + 2u^5 + u^4 + u^3 - u^2 - 3u - 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^8 - u^7 + 2u^6 + 3u^5 - u^4 - u^3 - 3u \\ u^8 - 2u^6 - u^5 + u^3 + u^2 + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^8 - u^7 + 2u^6 + 3u^5 - u^4 - u^3 - 3u \\ u^8 - 2u^6 - u^5 + u^3 + u^2 + u \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.37937$	-11.3909	-21.8268
$u = -1.188582 - 0.361061I$	$0.69960 - 3.87858I$	$-10.64109 + 3.78555I$
$u = -1.188582 + 0.361061I$	$0.69960 + 3.87858I$	$-10.64109 - 3.78555I$
$u = -0.306233$	-0.504287	-19.6540
$u = 0.098375 - 0.814801I$	$7.35406 + 4.61617I$	$-4.22495 - 4.01969I$
$u = 0.098375 + 0.814801I$	$7.35406 - 4.61617I$	$-4.22495 + 4.01969I$
$u = 1.18251$	-5.71950	-15.9090
$u = 1.341754 - 0.354713I$	$-1.71371 + 13.05001I$	$-13.4391 - 8.3124I$
$u = 1.341754 + 0.354713I$	$-1.71371 - 13.05001I$	$-13.4391 + 8.3124I$

$$\text{II. } I_2^u = \langle u^{36} - u^{35} + \dots - 4u^3 + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^4 + u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^4 + u^2 + 1 \\ u^6 - 2u^4 + u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^{14} + 5u^{12} - 8u^{10} + u^8 + 8u^6 - 4u^4 - 2u^2 + 1 \\ u^{14} - 6u^{12} + 13u^{10} - 10u^8 - 2u^6 + 4u^4 + u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^{11} - 4u^9 + 4u^7 + 2u^5 - 3u^3 - 2u \\ -u^{13} + 5u^{11} - 9u^9 + 6u^7 - u^3 + u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^{21} - 8u^{19} + \dots + 6u^3 + u \\ -u^{23} + 9u^{21} + \dots - 4u^3 + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^{35} - 14u^{33} + \dots - 3u + 1 \\ -u^{34} + 14u^{32} + \dots + 2u - 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^{35} - 14u^{33} + \dots - 3u + 1 \\ -u^{34} + 14u^{32} + \dots + 2u - 1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.347925 - 0.085501I$	$-2.91493 - 2.96900I$	$-12.88830 + 4.22200I$
$u = -1.347925 + 0.085501I$	$-2.91493 + 2.96900I$	$-12.88830 - 4.22200I$
$u = -1.335909 - 0.303663I$	$-7.50591 - 6.65729I$	$-18.0029 + 5.6815I$
$u = -1.335909 + 0.303663I$	$-7.50591 + 6.65729I$	$-18.0029 - 5.6815I$
$u = -1.332130 - 0.356156I$	$2.86466 - 8.83442I$	$-8.85054 + 6.32425I$
$u = -1.332130 + 0.356156I$	$2.86466 + 8.83442I$	$-8.85054 - 6.32425I$
$u = -1.253707 - 0.284832I$	$-1.22218 - 2.17847I$	$-11.24475 - 0.74332I$
$u = -1.253707 + 0.284832I$	$-1.22218 + 2.17847I$	$-11.24475 + 0.74332I$
$u = -1.137595 - 0.360537I$	$-0.25332 + 4.56891I$	$-11.76762 - 2.55639I$
$u = -1.137595 + 0.360537I$	$-0.25332 - 4.56891I$	$-11.76762 + 2.55639I$
$u = -0.488414 - 0.379131I$	$-1.69882 - 5.26707I$	$-12.9078 + 7.0444I$
$u = -0.488414 + 0.379131I$	$-1.69882 + 5.26707I$	$-12.9078 - 7.0444I$
$u = -0.330280 - 0.456150I$	$-1.22218 + 2.17847I$	$-11.24475 + 0.74332I$
$u = -0.330280 + 0.456150I$	$-1.22218 - 2.17847I$	$-11.24475 - 0.74332I$
$u = -0.114880 - 0.814996I$	$2.86466 - 8.83442I$	$-8.85054 + 6.32425I$
$u = -0.114880 + 0.814996I$	$2.86466 + 8.83442I$	$-8.85054 - 6.32425I$
$u = -0.075687 - 0.812840I$	$4.10849 - 0.36044I$	$-7.24415 + 0.04898I$
$u = -0.075687 + 0.812840I$	$4.10849 + 0.36044I$	$-7.24415 - 0.04898I$
$u = -0.042366 - 0.732635I$	$2.49914 - 1.48028I$	$-7.39740 + 4.69129I$
$u = -0.042366 + 0.732635I$	$2.49914 + 1.48028I$	$-7.39740 - 4.69129I$
$u = 0.125186 - 0.707270I$	$-2.91493 + 2.96900I$	$-12.88830 - 4.22200I$
$u = 0.125186 + 0.707270I$	$-2.91493 - 2.96900I$	$-12.88830 + 4.22200I$
$u = 0.410957 - 0.392187I$	$2.49914 + 1.48028I$	$-7.39740 - 4.69129I$
$u = 0.410957 + 0.392187I$	$2.49914 - 1.48028I$	$-7.39740 + 4.69129I$
$u = 0.629383$	-5.41700	-18.3114
$u = 1.161329 - 0.360877I$	$4.10849 - 0.36044I$	$-7.24415 + 0.04898I$
$u = 1.161329 + 0.360877I$	$4.10849 + 0.36044I$	$-7.24415 - 0.04898I$
$u = 1.294406 - 0.195773I$	-6.07645	-17.0816
$u = 1.294406 + 0.195773I$	-6.07645	-17.0816
$u = 1.299395 - 0.312670I$	$-1.69882 + 5.26707I$	$-12.9078 - 7.0444I$
Solution to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.299395 + 0.312670I$	$-1.69882 - 5.26707I$	$-12.9078 + 7.0444I$
$u = 1.31676$	-5.41700	-18.3114
$u = 1.317493 - 0.356084I$	$-0.25332 + 4.56891I$	$-11.76762 - 2.55639I$
$u = 1.317493 + 0.356084I$	$-0.25332 - 4.56891I$	$-11.76762 + 2.55639I$
$u = 1.377056 - 0.080377I$	$-7.50591 + 6.65729I$	$-18.0029 - 5.6815I$
$u = 1.377056 + 0.080377I$	$-7.50591 - 6.65729I$	$-18.0029 + 5.6815I$

III. u-Polynomials

Crossings	u-Polynomials at each crossings
c_1, c_3, c_4 c_6	$(u^9 + 4u^7 - 2u^6 + 5u^5 - 6u^4 - 2u^3 - 5u^2 - 5u - 1)$ $(u^{36} + 3u^{35} + \dots - 12u - 7)$
c_2, c_5, c_7 c_8, c_{10}, c_{11}	$(u^9 - 4u^7 + \dots - 3u + 1)(u^{36} + u^{35} + \dots + 4u^3 + 1)$
c_9	$(u^9 + 7u^8 + 25u^7 + 54u^6 + 74u^5 + 55u^4 + u^3 - 42u^2 - 36u - 8)$ $(1 - 7u + 9u^2 - 13u^3 + 9u^4 - u^5 + 4u^6 - 9u^7 + 22u^8 - 25u^9 + 21u^{10} - 31u^{11} + 44u^{12} - 30u^{13} + 17u^{14} - 7u^{15} + 2u^{16} - u^{17})$

IV. Riley Polynomials

Crossings	Riley Polynomials at each crossings
c_1, c_3, c_4 c_6	$(y^9 + 8y^8 + 26y^7 + 32y^6 - 25y^5 - 116y^4 - 110y^3 - 17y^2 + 15y - 1)$ $(y^{36} + 23y^{35} + \dots - 340y + 49)$
c_2, c_5, c_7 c_8, c_{10}, c_{11}	$(y^9 - 8y^8 + 26y^7 - 40y^6 + 19y^5 + 24y^4 - 30y^3 - y^2 + 11y - 1)$ $(y^{36} - 29y^{35} + \dots + 8y^2 + 1)$
c_9	$(y^9 + y^8 + 17y^7 + 16y^6 + 102y^5 - 29y^4 + 157y^3 - 956y^2 + 624y - 64)$ $(1 - 31y - 83y^2 - 13y^3 + 45y^4 - 75y^5 - 224y^6 + 21y^7 + 354y^8 + 207y^9 + 449y^{10} + 25y^{11} + 6)$