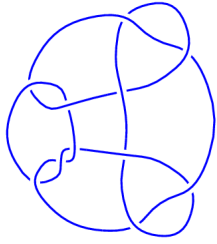
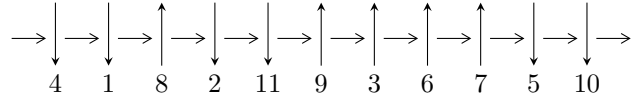


11a₄₄ (K11a₄₄)

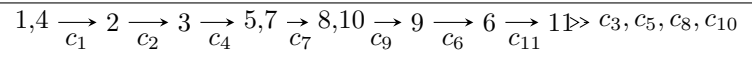


1

Arc Sequences



Solving Sequence



Representation Ideals

$$I = \bigcap_{i=1}^8 I_i^u \bigcap I_1^v$$

¹The knot diagram image is adapter from “C. Livingston and A. H. Moore, KnotInfo: Table of Knot Invariants, <http://www.indiana.edu/~knotinfo>”

$$\begin{aligned}
I_1^u &= \langle a, u-1, d+1, cb+1 \rangle \\
I_2^u &= \langle a, c, u-1, d+1, b+1 \rangle \\
I_3^u &= \langle a, d, b-1, c-1, u-1 \rangle \\
I_4^u &= \langle a+u, u^2+d, u^3+b-u, -2u^4-2u^3+c+2u+1, u^6+u^5-u^4-2u^3+u+1 \rangle \\
I_5^u &= \langle d^{12}+9d^{11}+34d^{10}+68d^9+73d^8+33d^7-5d^6+d^5+25d^4+23d^3+2d^2-4d+1, \\
&\quad -22d^{11}-148d^{10}+\dots+69a+40, 56d^{11}+452d^{10}+\dots+69b-14, \\
&\quad -10d^{11}-61d^{10}+\dots+69c-101, \\
&\quad 22d^{11}+148d^{10}+374d^9+370d^8-88d^7-523d^6-408d^5+46d^4+182d^3-77d^2-126d+69u-40 \rangle \\
I_6^u &= \langle u^2+d, u^{17}+u^{16}+\dots+2b+1, -u^{18}-2u^{17}+\dots+4c-4, u^{19}+2u^{18}+\dots+3u+1, \\
&\quad u^{18}+2u^{17}+\dots+2a+3 \rangle \\
I_7^u &= \langle u^{10}-3u^8-2u^7+2u^6+4u^5+3u^4-3u^2+a-3u-1, -u^{10}+2u^8+2u^7-u^6-2u^5-2u^4-u^3+u^2+b \\
&\quad u^{11}-3u^9-2u^8+2u^7+4u^6+3u^5-3u^3-3u^2+d-u, \\
&\quad u^{12}-u^{11}-4u^{10}+2u^9+7u^8+u^7-5u^6-5u^5-u^4+3u^3+2u^2+1, \\
&\quad u^{11}-4u^9-2u^8+6u^7+6u^6-2u^5-6u^4-3u^3+2u^2+c+2u-1 \rangle \\
I_8^u &= \langle u^{16}+u^{15}-3u^{14}-5u^{13}+3u^{12}+9u^{11}+2u^{10}-8u^9-6u^8+2u^7+5u^6+u^5-u^4+2u^3+3u^2-4u-4, \\
&\quad 221u^{15}-273u^{14}+\dots+2360a-470, 727u^{15}+393u^{14}+\dots+1180b-2866, \\
&\quad -593u^{15}-31u^{14}+\dots+2360c+850, -85u^{15}-13u^{14}+\dots+590d+1152 \rangle \\
I_1^v &= \langle b, c, v-1, d+1, a-1 \rangle
\end{aligned}$$

There are 9 irreducible components with 68 representations.
There are 1 irreducible components of $\dim_{\mathbb{C}} = 1$ for $11a_{44}$

$$\mathbf{I. } I_1^u = \langle a, u - 1, d + 1, cb + 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ b \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ b \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} c \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} c \\ -b - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} c \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} c + 1 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} c + 1 \\ -1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = \dots$		
$a = \dots$		
$b = \dots$	-1.64493	-2.82963 - 0.26612I
$c = \dots$		
$d = \dots$		

$$\text{II. } I_2^u = \langle a, c, u - 1, d + 1, b + 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$		
$a = 0$		
$b = -1.00000$	-3.28987	-12.0000
$c = 0$		
$d = -1.00000$		

$$\text{III. } I_3^u = \langle a, d, b - 1, c - 1, u - 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$		
$a = 0$		
$b = 1.00000$	0	0
$c = 1.00000$		
$d = 0$		

IV.

$$I_4^u = \langle a+u, u^2+d, u^3+b-u, -2u^4-2u^3+c+2u+1, u^6+u^5-u^4-2u^3+u+1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^2+1 \\ u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u \\ -u^3+u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u \\ -u^3+u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^4+u^2-1 \\ u^5+u^4-2u^3-u^2+u+1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 2u^4+2u^3-2u-1 \\ -u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 2u^4+2u^3-u^2-2u-1 \\ -u^4 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -2u^5-2u^4+u^3+2u^2 \\ u^5-u^3+u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 2u^4+2u^3-u^2-2u-1 \\ -u^4 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 2u^4+2u^3-u^2-2u-1 \\ -u^4 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_4^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.073950 - 0.558752I$ $a = 1.073950 + 0.558752I$ $b = -0.84116 + 1.20014I$ $c = -0.78324 + 1.63778I$ $d = -0.84116 - 1.20014I$	$-5.69302I$	$5.51057I$
$u = -1.073950 + 0.558752I$ $a = 1.073950 - 0.558752I$ $b = -0.84116 - 1.20014I$ $c = -0.78324 - 1.63778I$ $d = -0.84116 + 1.20014I$	$5.69302I$	$-5.51057I$
$u = -0.428243 - 0.664531I$ $a = 0.428243 + 0.664531I$ $b = -0.917045 - 0.592379I$ $c = 0.319544 + 0.596907I$ $d = 0.258209 - 0.569162I$	$1.89061 + 0.92430I$	$3.71672 - 0.79423I$
$u = -0.428243 + 0.664531I$ $a = 0.428243 - 0.664531I$ $b = -0.917045 + 0.592379I$ $c = 0.319544 - 0.596907I$ $d = 0.258209 + 0.569162I$	$1.89061 - 0.92430I$	$3.71672 + 0.79423I$
$u = 1.002193 - 0.295542I$ $a = -1.002193 + 0.295542I$ $b = 0.258209 + 0.569162I$ $c = -0.53630 - 3.31128I$ $d = -0.917045 + 0.592379I$	$-1.89061 + 0.92430I$	$-3.71672 - 0.79423I$
$u = 1.002193 + 0.295542I$ $a = -1.002193 - 0.295542I$ $b = 0.258209 - 0.569162I$ $c = -0.53630 + 3.31128I$ $d = -0.917045 - 0.592379I$	$-1.89061 - 0.92430I$	$-3.71672 + 0.79423I$

V.

$$I_5^u = \langle d^{12} + 9d^{11} + \dots - 4d + 1, -22d^{11} - 148d^{10} + \dots + 69a + 40, 56d^{11} + 452d^{10} + \dots + 69b - 14, -10d^{11} - 61d^{10} + \dots + 69c - 101, 22d^{11} + 69u + \dots - 126d - 40 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ -0.318841d^{11} - 2.14493d^{10} + \dots + 1.82609d + 0.579710 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ 0.275362d^{11} + 2.57971d^{10} + \dots + 0.695652d + 0.681159 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -0.275362d^{11} - 2.57971d^{10} + \dots - 0.695652d + 0.318841 \\ 0.275362d^{11} + 2.57971d^{10} + \dots + 0.695652d + 0.681159 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0.318841d^{11} + 2.14493d^{10} + \dots - 1.82609d - 0.579710 \\ -0.811594d^{11} - 6.55072d^{10} + \dots + 0.739130d + 0.202899 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.318841d^{11} + 2.14493d^{10} + \dots - 1.82609d - 0.579710 \\ -0.811594d^{11} - 6.55072d^{10} + \dots + 0.739130d + 0.202899 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -0.376812d^{11} - 2.89855d^{10} + \dots - 0.478261d - 0.405797 \\ d^3 + 2d^2 + d \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.144928d^{11} + 0.884058d^{10} + \dots - 1.73913d + 1.46377 \\ d \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.420290d^{11} + 3.46377d^{10} + \dots - 2.04348d + 1.14493 \\ -d^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.188406d^{11} - 1.44928d^{10} + \dots + 0.260870d - 1.20290 \\ 1.39130d^{11} + 10.0870d^{10} + \dots - 5.69565d + 1.65217 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.420290d^{11} + 3.46377d^{10} + \dots - 2.04348d + 1.14493 \\ -d^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.420290d^{11} + 3.46377d^{10} + \dots - 2.04348d + 1.14493 \\ -d^2 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_5^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.073950 + 0.558752I$ $a = 1.073950 - 0.558752I$ $b = -0.84116 - 1.20014I$ $c = 0.109214 - 0.714907I$ $d = -1.76612 - 0.73243I$	5.69302I	- 5.51057I
$u = -1.073950 - 0.558752I$ $a = 1.073950 + 0.558752I$ $b = -0.84116 + 1.20014I$ $c = 0.109214 + 0.714907I$ $d = -1.76612 + 0.73243I$	- 5.69302I	5.51057I
$u = -0.428243 - 0.664531I$ $a = 0.428243 + 0.664531I$ $b = -0.917045 - 0.592379I$ $c = -0.055560 + 1.311364I$ $d = -1.73203 - 0.37023I$	1.89061 + 0.92430I	3.71672 - 0.79423I
$u = -0.428243 + 0.664531I$ $a = 0.428243 - 0.664531I$ $b = -0.917045 + 0.592379I$ $c = -0.055560 - 1.311364I$ $d = -1.73203 + 0.37023I$	1.89061 - 0.92430I	3.71672 + 0.79423I
$u = 1.002193 - 0.295542I$ $a = -1.002193 + 0.295542I$ $b = 0.258209 + 0.569162I$ $c = -0.008329 - 0.488867I$ $d = -1.297233 - 0.443379I$	-1.89061 + 0.92430I	-3.71672 - 0.79423I
$u = 1.002193 + 0.295542I$ $a = -1.002193 - 0.295542I$ $b = 0.258209 - 0.569162I$ $c = -0.008329 + 0.488867I$ $d = -1.297233 + 0.443379I$	-1.89061 - 0.92430I	-3.71672 + 0.79423I

Solution to I_5^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.428243 + 0.664531I$ $a = 0.428243 - 0.664531I$ $b = -0.917045 + 0.592379I$ $c = 1.05556 + 1.31136I$ $d = -0.526177 - 0.939391I$	$1.89061 - 0.92430I$	$3.71672 + 0.79423I$
$u = -0.428243 - 0.664531I$ $a = 0.428243 + 0.664531I$ $b = -0.917045 - 0.592379I$ $c = 1.05556 - 1.31136I$ $d = -0.526177 + 0.939391I$	$1.89061 + 0.92430I$	$3.71672 - 0.79423I$
$u = 1.002193 - 0.295542I$ $a = -1.002193 + 0.295542I$ $b = 0.258209 + 0.569162I$ $c = 1.008329 + 0.488867I$ $d = 0.214278 - 0.149000I$	$-1.89061 + 0.92430I$	$-3.71672 - 0.79423I$
$u = 1.002193 + 0.295542I$ $a = -1.002193 - 0.295542I$ $b = 0.258209 - 0.569162I$ $c = 1.008329 - 0.488867I$ $d = 0.214278 + 0.149000I$	$-1.89061 - 0.92430I$	$-3.71672 + 0.79423I$
$u = -1.073950 + 0.558752I$ $a = 1.073950 - 0.558752I$ $b = -0.84116 - 1.20014I$ $c = 0.890786 + 0.714907I$ $d = 0.607288 - 0.467717I$	$5.69302I$	$-5.51057I$
$u = -1.073950 - 0.558752I$ $a = 1.073950 + 0.558752I$ $b = -0.84116 + 1.20014I$ $c = 0.890786 - 0.714907I$ $d = 0.607288 + 0.467717I$	$-5.69302I$	$5.51057I$

$$\text{VI. } I_6^u = \langle u^2 + d, u^{17} + u^{16} + \dots + 2b + 1, -u^{18} - 2u^{17} + \dots + 4c - 4, u^{19} + 2u^{18} + \dots + 3u + 1, u^{18} + 2u^{17} + \dots + 2a + 3 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -\frac{1}{2}u^{18} - u^{17} + \dots + \frac{1}{2}u - \frac{3}{2} \\ -\frac{1}{2}u^{17} - \frac{1}{2}u^{16} + \dots + u - \frac{1}{2} \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^{18} - \frac{3}{2}u^{17} + \dots + \frac{1}{2}u - 2 \\ -\frac{1}{2}u^{17} + 2u^{15} + \dots + \frac{9}{2}u^2 - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} \frac{1}{4}u^{18} + \frac{1}{2}u^{17} + \dots - \frac{1}{4}u + 1 \\ -u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} \frac{1}{2}u^{18} + \frac{3}{4}u^{17} + \dots - \frac{3}{4}u + \frac{9}{4} \\ \frac{1}{2}u^{18} + \frac{3}{4}u^{17} + \dots + \frac{1}{4}u + \frac{3}{4} \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -\frac{1}{4}u^{17} - \frac{1}{2}u^{16} + \dots - \frac{5}{4}u + \frac{1}{4} \\ u^5 - u^3 + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} \frac{1}{4}u^{18} + \frac{1}{2}u^{17} + \dots - \frac{1}{4}u + 1 \\ -u^4 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} \frac{1}{4}u^{18} + \frac{1}{2}u^{17} + \dots - \frac{1}{4}u + 1 \\ -u^4 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_6^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.219915 - 0.612443I$ $a = 1.84038 + 0.77324I$ $b = -1.97753 + 1.24306I$ $c = -1.10074 + 1.33083I$ $d = -1.11311 - 1.49426I$	$2.5538 - 15.5977I$	$0.09598 + 9.40344I$
$u = -1.219915 + 0.612443I$ $a = 1.84038 - 0.77324I$ $b = -1.97753 - 1.24306I$ $c = -1.10074 - 1.33083I$ $d = -1.11311 + 1.49426I$	$2.5538 + 15.5977I$	$0.09598 - 9.40344I$
$u = -1.163712 - 0.575900I$ $a = -1.49922 - 0.61081I$ $b = 1.46155 - 1.34018I$ $c = -1.02511 + 1.49171I$ $d = -1.02256 - 1.34036I$	$-2.61225 - 10.89709I$	$-3.23641 + 8.50579I$
$u = -1.163712 + 0.575900I$ $a = -1.49922 + 0.61081I$ $b = 1.46155 + 1.34018I$ $c = -1.02511 - 1.49171I$ $d = -1.02256 + 1.34036I$	$-2.61225 + 10.89709I$	$-3.23641 - 8.50579I$
$u = -0.892218 - 0.798617I$ $a = 0.118380 - 1.254991I$ $b = 0.031342 + 0.273386I$ $c = -0.385453 + 1.040442I$ $d = -0.15826 - 1.42508I$	$9.74824 - 5.99256I$	$5.35093 + 5.49640I$
$u = -0.892218 + 0.798617I$ $a = 0.118380 + 1.254991I$ $b = 0.031342 - 0.273386I$ $c = -0.385453 - 1.040442I$ $d = -0.15826 + 1.42508I$	$9.74824 + 5.99256I$	$5.35093 - 5.49640I$

Solution to I_6^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.713652 - 0.621261I$ $a = -0.078489 + 0.212487I$ $b = 0.548223 + 0.458686I$ $c = 0.127668 + 1.140610I$ $d = -0.123333 - 0.886728I$	$2.40223 - 3.63220I$	$3.52732 + 6.81616I$
$u = -0.713652 + 0.621261I$ $a = -0.078489 - 0.212487I$ $b = 0.548223 - 0.458686I$ $c = 0.127668 - 1.140610I$ $d = -0.123333 + 0.886728I$	$2.40223 + 3.63220I$	$3.52732 - 6.81616I$
$u = -0.379493 - 0.913957I$ $a = -1.49556 - 0.97073I$ $b = 1.46152 + 0.68811I$ $c = 0.012242 + 0.415167I$ $d = 0.691302 - 0.693681I$	$7.80660 + 4.21764I$	$6.24313 - 1.77538I$
$u = -0.379493 + 0.913957I$ $a = -1.49556 + 0.97073I$ $b = 1.46152 - 0.68811I$ $c = 0.012242 - 0.415167I$ $d = 0.691302 + 0.693681I$	$7.80660 - 4.21764I$	$6.24313 + 1.77538I$
$u = -0.266152$ $a = -1.40639$ $b = -0.642422$ $c = 1.15247$ $d = -0.0708367$	1.20822	9.19790
$u = 0.587370 - 0.660248I$ $a = 1.52616 - 2.19030I$ $b = -1.002697 + 0.800999I$ $c = 0.217752 - 0.865792I$ $d = 0.090924 + 0.775620I$	$4.14406 + 1.22871I$	$4.10945 - 3.37998I$

Solution to I_6^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.587370 + 0.660248I$ $a = 1.52616 + 2.19030I$ $b = -1.002697 - 0.800999I$ $c = 0.217752 + 0.865792I$ $d = 0.090924 - 0.775620I$	$4.14406 - 1.22871I$	$4.10945 + 3.37998I$
$u = 0.710407 - 0.203370I$ $a = -0.573689 + 1.178553I$ $b = 0.246691 - 0.049771I$ $c = 1.88912 - 1.55551I$ $d = -0.463319 + 0.288950I$	$-1.32552 + 1.22673I$	$-3.58366 - 5.47914I$
$u = 0.710407 + 0.203370I$ $a = -0.573689 - 1.178553I$ $b = 0.246691 + 0.049771I$ $c = 1.88912 + 1.55551I$ $d = -0.463319 - 0.288950I$	$-1.32552 - 1.22673I$	$-3.58366 + 5.47914I$
$u = 1.085303 - 0.470880I$ $a = 1.74507 + 0.02900I$ $b = -0.757420 - 1.122886I$ $c = -0.91621 - 1.95317I$ $d = -0.956154 + 1.022095I$	$-4.29720 + 4.85510I$	$-5.63265 - 5.33490I$
$u = 1.085303 + 0.470880I$ $a = 1.74507 - 0.02900I$ $b = -0.757420 + 1.122886I$ $c = -0.91621 + 1.95317I$ $d = -0.956154 - 1.022095I$	$-4.29720 - 4.85510I$	$-5.63265 + 5.33490I$
$u = 1.118985 - 0.584861I$ $a = -2.37984 - 0.16413I$ $b = 1.30952 + 1.42851I$ $c = -0.89551 - 1.52082I$ $d = -0.91007 + 1.30890I$	$0.71510 + 8.68076I$	$-0.47305 - 6.48182I$
Solution to I_6^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.118985 + 0.584861I$ $a = -2.37984 + 0.16413I$ $b = 1.30952 - 1.42851I$ $c = -0.89551 + 1.52082I$ $d = -0.91007 - 1.30890I$	$0.71510 - 8.68076I$	$-0.47305 + 6.48182I$

$$\text{VII. } I_7^u = \langle u^{10} - 3u^8 + \dots + a - 1, -u^{10} + 2u^8 + \dots + b + u, u^{11} - 3u^9 + \dots + d - u, u^{12} - u^{11} + \dots + 2u^2 + 1, u^{11} - 4u^9 + \dots + c - 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_1 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_2 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix} \\ a_7 &= \begin{pmatrix} -u^{10} + 3u^8 + 2u^7 - 2u^6 - 4u^5 - 3u^4 + 3u^2 + 3u + 1 \\ u^{10} - 2u^8 - 2u^7 + u^6 + 2u^5 + 2u^4 + u^3 - u^2 - u \end{pmatrix} \\ a_8 &= \begin{pmatrix} u^7 - 2u^5 - u^4 + u^2 + 2u + 1 \\ -u^7 + u^6 + u^5 - u^2 - u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -u^{11} + 4u^9 + 2u^8 - 6u^7 - 6u^6 + 2u^5 + 6u^4 + 3u^3 - 2u^2 - 2u + 1 \\ -u^{11} + 3u^9 + 2u^8 - 2u^7 - 4u^6 - 3u^5 + 3u^3 + 3u^2 + u \end{pmatrix} \\ a_9 &= \begin{pmatrix} -2u^{11} + 7u^9 + 4u^8 - 8u^7 - 10u^6 - u^5 + 6u^4 + 6u^3 + u^2 - u + 1 \\ u^9 - u^7 - 2u^6 - u^5 + u^4 + 2u^3 + 2u^2 + u \end{pmatrix} \\ a_6 &= \begin{pmatrix} 2u^{11} - 8u^9 - 3u^8 + 10u^7 + 9u^6 - 7u^4 - 7u^3 + 2u - 1 \\ -u^8 + 2u^6 + u^5 - u^3 - 2u^2 - u \end{pmatrix} \\ a_{11} &= \begin{pmatrix} u^9 - 4u^7 - 2u^6 + 5u^5 + 6u^4 - 4u^2 - 3u \\ -u^9 + 3u^7 + 2u^6 - 3u^5 - 4u^4 + 2u^2 + u \end{pmatrix} \\ a_{11} &= \begin{pmatrix} u^9 - 4u^7 - 2u^6 + 5u^5 + 6u^4 - 4u^2 - 3u \\ -u^9 + 3u^7 + 2u^6 - 3u^5 - 4u^4 + 2u^2 + u \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_7^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.155020 - 0.191936I$ $a = 0.689693 - 0.627483I$ $b = 0.15460 + 3.71488I$ $c = 0.197010 + 0.389313I$ $d = -0.917045 + 0.592379I$	$-1.89061 + 0.92430I$	$-3.71672 - 0.79423I$
$u = -1.155020 + 0.191936I$ $a = 0.689693 + 0.627483I$ $b = 0.15460 - 3.71488I$ $c = 0.197010 - 0.389313I$ $d = -0.917045 - 0.592379I$	$-1.89061 - 0.92430I$	$-3.71672 + 0.79423I$
$u = -0.895235 - 0.524661I$ $a = -0.492029 - 0.347410I$ $b = -0.103539 - 0.942817I$ $c = 1.032251 - 0.761198I$ $d = 0.258209 + 0.569162I$	$1.89061 - 0.92430I$	$3.71672 + 0.79423I$
$u = -0.895235 + 0.524661I$ $a = -0.492029 + 0.347410I$ $b = -0.103539 + 0.942817I$ $c = 1.032251 + 0.761198I$ $d = 0.258209 - 0.569162I$	$1.89061 + 0.92430I$	$3.71672 - 0.79423I$
$u = -0.282166 - 0.828798I$ $a = -0.98800 - 1.35129I$ $b = 1.16959 + 0.91104I$ $c = 0.79119 - 1.36688I$ $d = -0.84116 + 1.20014I$	$5.69302I$	$-5.51057I$
$u = -0.282166 + 0.828798I$ $a = -0.98800 + 1.35129I$ $b = 1.16959 - 0.91104I$ $c = 0.79119 + 1.36688I$ $d = -0.84116 - 1.20014I$	$-5.69302I$	$5.51057I$

Solution to I_7^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.152828 - 0.487477I$ $a = 0.56945 - 2.05973I$ $b = 0.101098 + 0.828455I$ $c = 1.03484 + 2.04495I$ $d = -0.917045 - 0.592379I$	$-1.89061 - 0.92430I$	$-3.71672 + 0.79423I$
$u = 0.152828 + 0.487477I$ $a = 0.56945 + 2.05973I$ $b = 0.101098 - 0.828455I$ $c = 1.03484 - 2.04495I$ $d = -0.917045 + 0.592379I$	$-1.89061 + 0.92430I$	$-3.71672 - 0.79423I$
$u = 1.323479 - 0.139870I$ $a = 0.147997 + 0.445691I$ $b = 1.18901 - 0.78206I$ $c = 0.627522 + 0.462745I$ $d = 0.258209 + 0.569162I$	$1.89061 - 0.92430I$	$3.71672 + 0.79423I$
$u = 1.323479 + 0.139870I$ $a = 0.147997 - 0.445691I$ $b = 1.18901 + 0.78206I$ $c = 0.627522 - 0.462745I$ $d = 0.258209 - 0.569162I$	$1.89061 + 0.92430I$	$3.71672 - 0.79423I$
$u = 1.356115 - 0.270046I$ $a = -0.427109 - 0.970037I$ $b = -1.01075 + 1.59090I$ $c = 0.317192 - 0.547993I$ $d = -0.84116 - 1.20014I$	$-5.69302I$	$5.51057I$
$u = 1.356115 + 0.270046I$ $a = -0.427109 + 0.970037I$ $b = -1.01075 - 1.59090I$ $c = 0.317192 + 0.547993I$ $d = -0.84116 + 1.20014I$	$5.69302I$	$-5.51057I$

$$\text{VIII. } I_{\mathfrak{g}}^u = \langle u^{16} + u^{15} + \dots - 4u - 4, 221u^{15} - 273u^{14} + \dots + 2360a - 470, 727u^{15} + 393u^{14} + \dots + 1180b - 2866, -593u^{15} - 31u^{14} + \dots + 2360c + 850, -85u^{15} - 13u^{14} + \dots + 590d + 1152 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.0936441u^{15} + 0.115678u^{14} + \dots - 0.674153u + 0.199153 \\ -0.616102u^{15} - 0.333051u^{14} + \dots - 0.478814u + 2.42881 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -0.114831u^{15} - 0.0699153u^{14} + \dots - 0.693644u + 0.0686441 \\ -0.639831u^{15} - 0.0449153u^{14} + \dots - 0.0686441u + 3.01864 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.251271u^{15} + 0.0131356u^{14} + \dots + 0.0351695u - 0.360169 \\ 0.144068u^{15} + 0.0220339u^{14} + \dots + 0.0525424u - 1.95254 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.146610u^{15} + 0.0483051u^{14} + \dots + 0.622881u - 0.172881 \\ 0.502542u^{15} + 0.0262712u^{14} + \dots + 0.0703390u - 2.72034 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.127966u^{15} + 0.0110169u^{14} + \dots + 0.626271u + 0.423729 \\ -0.529661u^{15} - 0.239831u^{14} + \dots - 0.687288u + 2.13729 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.107203u^{15} - 0.00889831u^{14} + \dots - 0.0173729u + 0.592373 \\ 0.427119u^{15} + 0.0135593u^{14} + \dots + 0.0169492u - 2.41695 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.107203u^{15} - 0.00889831u^{14} + \dots - 0.0173729u + 0.592373 \\ 0.427119u^{15} + 0.0135593u^{14} + \dots + 0.0169492u - 2.41695 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_g^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.157569 - 0.635502I$ $a = -1.48614 - 0.93475I$ $b = 1.57665 - 0.90527I$ $c = 0.826549 - 0.740811I$ $d = 0.863672 + 0.522607I$	$5.44991 - 9.88301I$	$3.28252 + 6.06963I$
$u = -1.157569 + 0.635502I$ $a = -1.48614 + 0.93475I$ $b = 1.57665 + 0.90527I$ $c = 0.826549 + 0.740811I$ $d = 0.863672 - 0.522607I$	$5.44991 + 9.88301I$	$3.28252 - 6.06963I$
$u = -1.076279 - 0.402850I$ $a = -0.985091 - 0.001978I$ $b = 0.32411 - 2.07852I$ $c = 0.081976 + 0.594679I$ $d = -1.43403 + 0.66344I$	$-4.77492 - 2.26376I$	$-6.05872 + 4.53378I$
$u = -1.076279 + 0.402850I$ $a = -0.985091 + 0.001978I$ $b = 0.32411 + 2.07852I$ $c = 0.081976 - 0.594679I$ $d = -1.43403 - 0.66344I$	$-4.77492 + 2.26376I$	$-6.05872 - 4.53378I$
$u = -0.783583$ $a = 0.489574$ $b = 2.20354$ $c = -0.437368$ $d = -1.26855$	-2.57083	2.16015
$u = -0.754559 - 0.841472I$ $a = -0.760920 + 0.848566I$ $b = 0.636148 - 0.242515I$ $c = 0.891409 - 0.994087I$ $d = 0.138717 + 1.269881I$	10.1546	6.33746

Solution to I_g^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.754559 + 0.841472I$ $a = -0.760920 - 0.848566I$ $b = 0.636148 + 0.242515I$ $c = 0.891409 + 0.994087I$ $d = 0.138717 - 1.269881I$	10.1546	6.33746
$u = -0.270006 - 0.967768I$ $a = 1.64151 + 1.62176I$ $b = -1.56027 - 1.09581I$ $c = 0.70037 - 1.27972I$ $d = -0.93610 + 1.47128I$	$5.44991 + 9.88301I$	$3.28252 - 6.06963I$
$u = -0.270006 + 0.967768I$ $a = 1.64151 - 1.62176I$ $b = -1.56027 + 1.09581I$ $c = 0.70037 + 1.27972I$ $d = -0.93610 - 1.47128I$	$5.44991 - 9.88301I$	$3.28252 + 6.06963I$
$u = 0.365525 - 0.776365I$ $a = -0.90049 + 2.82232I$ $b = 0.50994 - 1.48491I$ $c = 0.89340 + 1.33041I$ $d = -0.664034 - 1.131195I$	$2.93531 - 3.55755I$	$2.52739 + 2.62489I$
$u = 0.365525 + 0.776365I$ $a = -0.90049 - 2.82232I$ $b = 0.50994 + 1.48491I$ $c = 0.89340 - 1.33041I$ $d = -0.664034 + 1.131195I$	$2.93531 + 3.55755I$	$2.52739 - 2.62489I$
$u = 0.993914 - 0.569061I$ $a = 2.16175 - 0.50363I$ $b = -1.27697 - 0.76242I$ $c = 0.940155 + 0.746855I$ $d = 0.469134 - 0.567562I$	$2.93531 + 3.55755I$	$2.52739 - 2.62489I$

Solution to I_g^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.993914 + 0.569061I$ $a = 2.16175 + 0.50363I$ $b = -1.27697 + 0.76242I$ $c = 0.940155 - 0.746855I$ $d = 0.469134 + 0.567562I$	$2.93531 - 3.55755I$	$2.52739 + 2.62489I$
$u = 1.12630$ $a = -0.340604$ $b = -0.439006$ $c = 0.304284$ $d = -0.614002$	-2.57083	2.16015
$u = 1.227616 - 0.270214I$ $a = 0.754892 + 0.491159I$ $b = 0.408126 - 1.151443I$ $c = 0.232685 - 0.497052I$ $d = -0.996088 - 0.867158I$	$-4.77492 - 2.26376I$	$-6.05872 + 4.53378I$
$u = 1.227616 + 0.270214I$ $a = 0.754892 - 0.491159I$ $b = 0.408126 + 1.151443I$ $c = 0.232685 + 0.497052I$ $d = -0.996088 + 0.867158I$	$-4.77492 + 2.26376I$	$-6.05872 - 4.53378I$

$$\text{IX. } I_1^v = \langle b, c, v - 1, d + 1, a - 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_1^v	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = 1.00000$		
$a = 1.00000$		
$b = 0$	0	0
$c = 0$		
$d = -1.00000$		

X. u-Polynomials

Crossings	u-Polynomials at each crossings
c_1	$u(u-1)^3(u^6 + u^5 - u^4 - 2u^3 + u + 1)^3$ $(u^{12} - u^{11} - 4u^{10} + 2u^9 + 7u^8 + u^7 - 5u^6 - 5u^5 - u^4 + 3u^3 + 2u^2 + 1)$ $(u^{16} + u^{15} + \dots - 4u - 4)(u^{19} + 2u^{18} + \dots + 3u + 1)$
c_2, c_{11}	$u(u+1)^3(u^6 + 3u^5 + 5u^4 + 4u^3 + 2u^2 + u + 1)^3$ $(u^{12} + 9u^{11} + \dots - 4u + 1)(u^{16} + 7u^{15} + \dots + 40u + 16)$ $(u^{19} + 8u^{18} + \dots + 19u + 1)$
c_3, c_7	$u^4(u^6 + u^5 - u^4 - 2u^3 + u + 1)^5$ $(u^8 - 3u^7 + 3u^6 + 2u^5 - 8u^4 + 9u^3 - 3u^2 - 2u + 2)^2$ $(u^{19} + 2u^{18} + \dots + 4u^2 - 8)$
c_4	$u(u-1)^2(u+1)(u^6 + u^5 - u^4 - 2u^3 + u + 1)^3$ $(u^{12} - u^{11} - 4u^{10} + 2u^9 + 7u^8 + u^7 - 5u^6 - 5u^5 - u^4 + 3u^3 + 2u^2 + 1)$ $(u^{16} + u^{15} + \dots - 4u - 4)(u^{19} + 2u^{18} + \dots + 3u + 1)$
c_5	$u(u+1)^3(u^6 + u^5 - u^4 - 2u^3 + u + 1)^3$ $(u^{12} - u^{11} - 4u^{10} + 2u^9 + 7u^8 + u^7 - 5u^6 - 5u^5 - u^4 + 3u^3 + 2u^2 + 1)$ $(u^{16} + u^{15} + \dots - 4u - 4)(u^{19} + 2u^{18} + \dots + 3u + 1)$
c_6	$u(u-1)(u+1)^2(u^6 - u^5 - u^4 + 2u^3 - u + 1)$ $(u^8 + u^7 - 4u^6 - 3u^5 + 5u^4 + u^3 - u^2 + 3u - 1)^2$ $(u^{12} + u^{11} - 4u^{10} - 2u^9 + 7u^8 - u^7 - 5u^6 + 5u^5 - u^4 - 3u^3 + 2u^2 + 1)^2$ $(u^{19} + 2u^{18} + \dots - 8u - 4)$
c_8, c_9	$u(u-1)^3(u^6 - u^5 - u^4 + 2u^3 - u + 1)$ $(u^8 + u^7 - 4u^6 - 3u^5 + 5u^4 + u^3 - u^2 + 3u - 1)^2$ $(u^{12} + u^{11} - 4u^{10} - 2u^9 + 7u^8 - u^7 - 5u^6 + 5u^5 - u^4 - 3u^3 + 2u^2 + 1)^2$ $(u^{19} + 2u^{18} + \dots - 8u - 4)$
c_{10}	$u(u-1)(u+1)^2(u^6 + u^5 - u^4 - 2u^3 + u + 1)^3$ $(u^{12} - u^{11} - 4u^{10} + 2u^9 + 7u^8 + u^7 - 5u^6 - 5u^5 - u^4 + 3u^3 + 2u^2 + 1)$ $(u^{16} + u^{15} + \dots - 4u - 4)(u^{19} + 2u^{18} + \dots + 3u + 1)$

XI. Riley Polynomials

Crossings	Riley Polynomials at each crossings
c_1, c_4, c_5 c_{10}	$y(y-1)^3(y^6 - 3y^5 + 5y^4 - 4y^3 + 2y^2 - y + 1)^3$ $(y^{12} - 9y^{11} + \dots + 4y + 1)(y^{16} - 7y^{15} + \dots - 40y + 16)$ $(y^{19} - 8y^{18} + \dots + 19y - 1)$
c_2, c_{11}	$y(y-1)^3(y^6 + y^5 + 5y^4 + 6y^2 + 3y + 1)^3$ $(y^{12} - 13y^{11} + \dots - 12y + 1)(y^{16} + y^{15} + \dots - 544y + 256)$ $(y^{19} + 12y^{18} + \dots + 195y - 1)$
c_3, c_7	$y^4(y^6 - 3y^5 + 5y^4 - 4y^3 + 2y^2 - y + 1)^5$ $(y^8 - 3y^7 + 5y^6 - 4y^5 + 2y^4 - 13y^3 + 13y^2 - 16y + 4)^2$ $(y^{19} - 6y^{18} + \dots + 64y - 64)$
c_6, c_8, c_9	$y(y-1)^3(y^6 - 3y^5 + 5y^4 - 4y^3 + 2y^2 - y + 1)$ $(y^8 - 9y^7 + 32y^6 - 53y^5 + 31y^4 + 15y^3 - 15y^2 - 7y + 1)^2$ $(1 + 4y + 2y^2 - 23y^3 + 25y^4 - y^5 - 5y^6 - 33y^7 + 73y^8 - 68y^9 + 34y^{10} - 9y^{11} + y^{12})^2$ $(y^{19} - 18y^{18} + \dots + 88y - 16)$