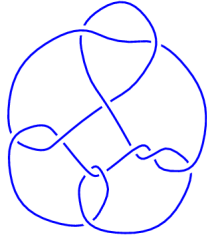
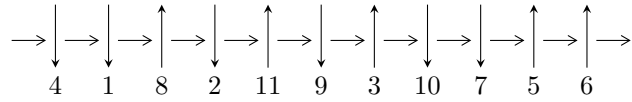


11a₄₇ (K11a₄₇)

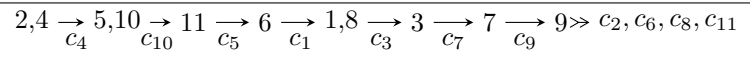


1

Arc Sequences



Solving Sequence



Representation Ideals

$$I = \bigcap_{i=1}^8 I_i^u \bigcap I_1^v$$

¹The knot diagram image is adapter from “C. Livingston and A. H. Moore, KnotInfo: Table of Knot Invariants, <http://www.indiana.edu/~knotinfo>”

$$I_1^u = \langle a, u - 1, d + c - 1, cb + 1 \rangle$$

$$I_2^u = \langle a, c, b - 1, d - 1, u - 1 \rangle$$

$$I_3^u = \langle a, c - 1, u - 1, d + 1, b + 1 \rangle$$

$$I_4^u = \langle u^4 + b, -u^2 + d, u^2 + c - 1, -u^4 + u^2 + a - 1, u^6 + u^5 - u^4 - 2u^3 + u + 1 \rangle$$

$$I_5^u = \langle c^{12} + 7c^{11} + 37c^{10} + 125c^9 + 301c^8 + 563c^7 + 855c^6 + 1020c^5 + 986c^4 + 748c^3 + 504c^2 + 277c + 137, \\ - 360449610467c^{11} - 2239492377762c^{10} + \dots + 16501719305943a - 35208293717353, \\ 56083107757c^{11} + 408621304548c^{10} + \dots + 5500573101981b + 9355307354771, \\ - 137214226835c^{11} + 16501719305943d + \dots + 23477181903284c + 13375366451981, \\ - 92559389066c^{11} + 16501719305943u + \dots + 14724871632887c + 15975316836953 \rangle$$

$$I_6^u = \langle -u^2 + d, u^2 + c - 1, u^7 - 2u^5 - u^4 + u^2 + a + 2u + 1, -u^9 + u^7 + 2u^6 + u^5 - u^4 - 2u^3 - 2u^2 + b - u, \\ u^{12} - u^{11} - 4u^{10} + 2u^9 + 7u^8 + u^7 - 5u^6 - 5u^5 - u^4 + 3u^3 + 2u^2 + 1 \rangle$$

$$I_7^u = \langle u^{16} + u^{15} - 3u^{14} - 5u^{13} + 3u^{12} + 9u^{11} + 2u^{10} - 8u^9 - 6u^8 + 2u^7 + 5u^6 + u^5 - u^4 + 2u^3 + 3u^2 - 4u - 4, \\ - 271u^{15} - 165u^{14} + \dots + 2360a + 162, -581u^{15} + 93u^{14} + \dots + 1180b + 3350, \\ - 99u^{15} - 197u^{14} + \dots + 2360c - 34, 173u^{15} + 57u^{14} + \dots + 590d - 204 \rangle$$

$$I_8^u = \langle u^{17} - 3u^{15} - 2u^{14} + 4u^{13} + 4u^{12} + u^{11} - 4u^{10} - 5u^9 - 2u^8 + 5u^7 + 4u^6 + u^5 - u^4 - u^3 + 4u^2 + 4d + u - 3, \\ u^{18} + u^{17} + \dots + 2b - 1, u^{19} + 2u^{18} + \dots + 3u + 1, -2u^{18} - 3u^{17} + \dots + 2a - 4, \\ - u^{18} - 2u^{17} + \dots + 2c - 5 \rangle$$

$$I_1^v = \langle b, c, d - 1, v - 1, a - 1 \rangle$$

There are 9 irreducible components with 68 representations.

There are 1 irreducible components of $\dim_{\mathbb{C}} = 1$ for $11a_{47}$

$$\text{I. } I_1^u = \langle a, u - 1, d + c - 1, cb + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} c \\ -c + 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} c + 1 \\ -c \end{pmatrix}$$

$$a_6 = \begin{pmatrix} c \\ -c + 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ b \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ b \end{pmatrix}$$

$$a_9 = \begin{pmatrix} c \\ -c + b + 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} c \\ -c + b + 1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = \dots$		
$a = \dots$		
$b = \dots$	-1.64493	-1.106145 + 0.511900 <i>I</i>
$c = \dots$		
$d = \dots$		

$$\text{II. } I_2^u = \langle a, c, b - 1, d - 1, u - 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$		
$a = 0$		
$b = 1.00000$	0	0
$c = 0$		
$d = 1.00000$		

$$\text{III. } I_3^u = \langle a, c - 1, u - 1, d + 1, b + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -2 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$		
$a = 0$		
$b = -1.00000$	-3.28987	-12.0000
$c = 1.00000$		
$d = -1.00000$		

IV.

$$I_4^u = \langle u^4 + b, -u^2 + d, u^2 + c - 1, -u^4 + u^2 + a - 1, u^6 + u^5 - u^4 - 2u^3 + u + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^4 - u^2 + 1 \\ -u^4 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^2 + 1 \\ u^4 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ -u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_4^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.073950 - 0.558752I$ $a = -0.573950 + 0.818891I$ $b = 0.73279 - 2.01903I$ $c = 0.158836 - 1.200143I$ $d = 0.84116 + 1.20014I$	$-5.69302I$	$5.51057I$
$u = -1.073950 + 0.558752I$ $a = -0.573950 - 0.818891I$ $b = 0.73279 + 2.01903I$ $c = 0.158836 + 1.200143I$ $d = 0.84116 - 1.20014I$	$5.69302I$	$-5.51057I$
$u = -0.428243 - 0.664531I$ $a = 1.000936 - 0.863088I$ $b = 0.257273 + 0.293926I$ $c = 1.258209 - 0.569162I$ $d = -0.258209 + 0.569162I$	$1.89061 + 0.92430I$	$3.71672 - 0.79423I$
$u = -0.428243 + 0.664531I$ $a = 1.000936 + 0.863088I$ $b = 0.257273 - 0.293926I$ $c = 1.258209 + 0.569162I$ $d = -0.258209 - 0.569162I$	$1.89061 - 0.92430I$	$3.71672 + 0.79423I$
$u = 1.002193 - 0.295542I$ $a = 0.573013 - 0.494098I$ $b = -0.490059 + 1.086478I$ $c = 0.082955 + 0.592379I$ $d = 0.917045 - 0.592379I$	$-1.89061 + 0.92430I$	$-3.71672 - 0.79423I$
$u = 1.002193 + 0.295542I$ $a = 0.573013 + 0.494098I$ $b = -0.490059 - 1.086478I$ $c = 0.082955 - 0.592379I$ $d = 0.917045 + 0.592379I$	$-1.89061 - 0.92430I$	$-3.71672 + 0.79423I$

$$\mathbf{V. } I_5^u = \langle c^{12} + 7c^{11} + \dots + 277c + 137, -3.60 \times 10^{11}c^{11} - 2.24 \times 10^{12}c^{10} + \dots + 1.65 \times 10^{13}a - 3.52 \times 10^{13}, 5.61 \times 10^{10}c^{11} + 4.09 \times 10^{11}c^{10} + \dots + 5.50 \times 10^{12}b + 9.36 \times 10^{12}, 1.65 \times 10^{13}d - 1.37 \times 10^{11}c^{11} + \dots + 2.35 \times 10^{13}c + 1.34 \times 10^{13}, 1.65 \times 10^{13}u - 9.26 \times 10^{10}c^{11} + \dots + 1.47 \times 10^{13}c + 1.60 \times 10^{13} \rangle$$

(i) Arc colorings

$$\begin{aligned} a_2 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 0 \\ 0.00560908c^{11} + 0.0192675c^{10} + \dots - 0.892323c - 0.968100 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -0.00560908c^{11} - 0.0192675c^{10} + \dots + 0.892323c + 0.968100 \\ 0.00560908c^{11} + 0.0192675c^{10} + \dots - 0.892323c - 0.968100 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} c \\ 0.00831515c^{11} + 0.0396045c^{10} + \dots - 1.42271c - 0.810544 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -0.00184239c^{11} - 0.00931661c^{10} + \dots + 0.279479c + 0.285527 \\ 0.0101575c^{11} + 0.0489212c^{10} + \dots - 0.702190c - 1.09607 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -0.000872373c^{11} + 0.0198965c^{10} + \dots + 2.00425c + 1.76513 \\ -0.00700307c^{11} - 0.0495165c^{10} + \dots - 1.93598c - 0.956306 \end{pmatrix} \\ a_1 &= \begin{pmatrix} 1 \\ 0.0116473c^{11} + 0.0614256c^{10} + \dots + 0.422287c - 0.567174 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 0.0218432c^{11} + 0.135713c^{10} + \dots + 3.86882c + 2.13361 \\ -0.0101959c^{11} - 0.0742870c^{10} + \dots - 3.44653c - 1.70079 \end{pmatrix} \\ a_3 &= \begin{pmatrix} 0.0116473c^{11} + 0.0614256c^{10} + \dots + 0.422287c + 0.432826 \\ 0.0101959c^{11} + 0.0742870c^{10} + \dots + 3.44653c + 1.70079 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 0.00560908c^{11} + 0.0192675c^{10} + \dots - 0.892323c - 0.968100 \\ -0.00560908c^{11} - 0.0192675c^{10} + \dots + 0.892323c + 0.968100 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -0.00184239c^{11} - 0.00931661c^{10} + \dots + 0.279479c + 0.285527 \\ 0.0101575c^{11} + 0.0489212c^{10} + \dots - 0.702190c - 1.09607 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -0.00184239c^{11} - 0.00931661c^{10} + \dots + 0.279479c + 0.285527 \\ 0.0101575c^{11} + 0.0489212c^{10} + \dots - 0.702190c - 1.09607 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_5^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.428243 + 0.664531I$ $a = 1.000936 + 0.863088I$ $b = 0.257273 - 0.293926I$ $c = -1.64624 - 0.72836I$ $d = 0.590678 - 0.583006I$	$1.89061 - 0.92430I$	$3.71672 + 0.79423I$
$u = -0.428243 - 0.664531I$ $a = 1.000936 - 0.863088I$ $b = 0.257273 + 0.293926I$ $c = -1.64624 + 0.72836I$ $d = 0.590678 + 0.583006I$	$1.89061 + 0.92430I$	$3.71672 - 0.79423I$
$u = -0.428243 - 0.664531I$ $a = 1.000936 - 0.863088I$ $b = 0.257273 + 0.293926I$ $c = -0.931516 - 0.756104I$ $d = 0.987076 - 0.555260I$	$1.89061 + 0.92430I$	$3.71672 - 0.79423I$
$u = -0.428243 + 0.664531I$ $a = 1.000936 + 0.863088I$ $b = 0.257273 - 0.293926I$ $c = -0.931516 + 0.756104I$ $d = 0.987076 + 0.555260I$	$1.89061 - 0.92430I$	$3.71672 + 0.79423I$
$u = 1.002193 + 0.295542I$ $a = 0.573013 + 0.494098I$ $b = -0.490059 - 1.086478I$ $c = -0.86373 - 3.45204I$ $d = -0.14460 + 3.94091I$	$-1.89061 - 0.92430I$	$-3.71672 + 0.79423I$
$u = 1.002193 - 0.295542I$ $a = 0.573013 - 0.494098I$ $b = -0.490059 + 1.086478I$ $c = -0.86373 + 3.45204I$ $d = -0.14460 - 3.94091I$	$-1.89061 + 0.92430I$	$-3.71672 - 0.79423I$

Solution to I_5^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.073950 + 0.558752I$ $a = -0.573950 - 0.818891I$ $b = 0.73279 + 2.01903I$ $c = -0.509721 - 1.113504I$ $d = 0.40051 + 1.82841I$	5.69302I	- 5.51057I
$u = -1.073950 - 0.558752I$ $a = -0.573950 + 0.818891I$ $b = 0.73279 - 2.01903I$ $c = -0.509721 + 1.113504I$ $d = 0.40051 - 1.82841I$	- 5.69302I	5.51057I
$u = -1.073950 - 0.558752I$ $a = -0.573950 + 0.818891I$ $b = 0.73279 - 2.01903I$ $c = 0.13413 - 1.55114I$ $d = -1.02492 + 2.26605I$	- 5.69302I	5.51057I
$u = -1.073950 + 0.558752I$ $a = -0.573950 - 0.818891I$ $b = 0.73279 + 2.01903I$ $c = 0.13413 + 1.55114I$ $d = -1.02492 - 2.26605I$	5.69302I	- 5.51057I
$u = 1.002193 - 0.295542I$ $a = 0.573013 - 0.494098I$ $b = -0.490059 + 1.086478I$ $c = 0.317076 - 0.733138I$ $d = -0.308747 + 1.222005I$	-1.89061 + 0.92430I	-3.71672 - 0.79423I
$u = 1.002193 + 0.295542I$ $a = 0.573013 + 0.494098I$ $b = -0.490059 - 1.086478I$ $c = 0.317076 + 0.733138I$ $d = -0.308747 - 1.222005I$	-1.89061 - 0.92430I	-3.71672 + 0.79423I

$$\text{VI. } I_6^u = \langle -u^2 + d, u^2 + c - 1, u^7 - 2u^5 + \dots + a + 1, -u^9 + u^7 + \dots + b - u, u^{12} - u^{11} + \dots + 2u^2 + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^7 + 2u^5 + u^4 - u^2 - 2u - 1 \\ u^9 - u^7 - 2u^6 - u^5 + u^4 + 2u^3 + 2u^2 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^2 + 1 \\ u^4 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^{10} - 3u^8 - 2u^7 + 2u^6 + 4u^5 + 3u^4 - 3u^2 - 3u - 1 \\ -u^{11} - 2u^{10} + 4u^9 + 7u^8 - u^7 - 9u^6 - 7u^5 + 5u^3 + 4u^2 + u + 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^{11} + 4u^9 + 2u^8 - 6u^7 - 6u^6 + 2u^5 + 6u^4 + 3u^3 - 2u^2 - 2u \\ 2u^{11} - 6u^9 - 4u^8 + 6u^7 + 8u^6 + 2u^5 - 4u^4 - 4u^3 - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^{11} + 4u^9 + 2u^8 - 6u^7 - 6u^6 + 2u^5 + 6u^4 + 3u^3 - 2u^2 - 2u \\ 2u^{11} - 6u^9 - 4u^8 + 6u^7 + 8u^6 + 2u^5 - 4u^4 - 4u^3 - 1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_6^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.155020 - 0.191936I$ $a = -0.267765 + 0.619837I$ $b = -0.38259 - 3.72805I$ $c = -0.297233 - 0.443379I$ $d = 1.297233 + 0.443379I$	$-1.89061 + 0.92430I$	$-3.71672 - 0.79423I$
$u = -1.155020 + 0.191936I$ $a = -0.267765 - 0.619837I$ $b = -0.38259 + 3.72805I$ $c = -0.297233 + 0.443379I$ $d = 1.297233 - 0.443379I$	$-1.89061 - 0.92430I$	$-3.71672 + 0.79423I$
$u = -0.895235 - 0.524661I$ $a = 0.689262 - 0.734076I$ $b = -0.14376 + 1.46753I$ $c = 0.473823 - 0.939391I$ $d = 0.526177 + 0.939391I$	$1.89061 - 0.92430I$	$3.71672 + 0.79423I$
$u = -0.895235 + 0.524661I$ $a = 0.689262 + 0.734076I$ $b = -0.14376 - 1.46753I$ $c = 0.473823 + 0.939391I$ $d = 0.526177 - 0.939391I$	$1.89061 + 0.92430I$	$3.71672 - 0.79423I$
$u = -0.282166 - 0.828798I$ $a = -0.999480 + 0.955518I$ $b = -0.416114 - 0.026273I$ $c = 1.60729 - 0.46772I$ $d = -0.607288 + 0.467717I$	$5.69302I$	$-5.51057I$
$u = -0.282166 + 0.828798I$ $a = -0.999480 - 0.955518I$ $b = -0.416114 + 0.026273I$ $c = 1.60729 + 0.46772I$ $d = -0.607288 - 0.467717I$	$-5.69302I$	$5.51057I$

Solution to I_6^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.152828 - 0.487477I$ $a = -0.99044 + 1.18900I$ $b = -0.497742 - 0.515052I$ $c = 1.214278 + 0.149000I$ $d = -0.214278 - 0.149000I$	$-1.89061 - 0.92430I$	$-3.71672 + 0.79423I$
$u = 0.152828 + 0.487477I$ $a = -0.99044 - 1.18900I$ $b = -0.497742 + 0.515052I$ $c = 1.214278 - 0.149000I$ $d = -0.214278 + 0.149000I$	$-1.89061 + 0.92430I$	$-3.71672 - 0.79423I$
$u = 1.323479 - 0.139870I$ $a = -0.772216 + 0.141696I$ $b = 1.72245 - 0.63219I$ $c = -0.732032 + 0.370229I$ $d = 1.73203 - 0.37023I$	$1.89061 - 0.92430I$	$3.71672 + 0.79423I$
$u = 1.323479 + 0.139870I$ $a = -0.772216 - 0.141696I$ $b = 1.72245 + 0.63219I$ $c = -0.732032 - 0.370229I$ $d = 1.73203 + 0.37023I$	$1.89061 + 0.92430I$	$3.71672 - 0.79423I$
$u = 1.356115 - 0.270046I$ $a = 0.840643 - 0.244625I$ $b = -1.78224 + 1.23026I$ $c = -0.766124 + 0.732426I$ $d = 1.76612 - 0.73243I$	$-5.69302I$	$5.51057I$
$u = 1.356115 + 0.270046I$ $a = 0.840643 + 0.244625I$ $b = -1.78224 - 1.23026I$ $c = -0.766124 - 0.732426I$ $d = 1.76612 + 0.73243I$	$5.69302I$	$-5.51057I$

$$\text{VII. } I_7^u = \langle u^{16} + u^{15} + \dots - 4u - 4, -271u^{15} - 165u^{14} + \dots + 2360a + 162, -581u^{15} + 93u^{14} + \dots + 1180b + 3350, -99u^{15} - 197u^{14} + \dots + 2360c - 34, 173u^{15} + 57u^{14} + \dots + 590d - 204 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.0419492u^{15} + 0.0834746u^{14} + \dots + 0.210593u + 0.0144068 \\ -0.293220u^{15} - 0.0966102u^{14} + \dots - 0.245763u + 0.345763 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.102119u^{15} + 0.0614407u^{14} + \dots + 0.158051u + 0.966949 \\ -0.149153u^{15} - 0.0745763u^{14} + \dots - 0.193220u - 0.606780 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.151695u^{15} - 0.300847u^{14} + \dots - 0.163559u + 0.413559 \\ 0.163559u^{15} + 0.456780u^{14} + \dots + 0.558475u - 0.408475 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0.114831u^{15} + 0.0699153u^{14} + \dots + 0.693644u - 0.0686441 \\ 0.492373u^{15} - 0.0788136u^{14} + \dots - 0.211017u - 2.83898 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^2 + 1 \\ u^4 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.0936441u^{15} - 0.115678u^{14} + \dots + 0.674153u - 0.199153 \\ 0.336441u^{15} + 0.0432203u^{14} + \dots + 0.941525u - 1.59153 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.146610u^{15} + 0.0483051u^{14} + \dots + 0.622881u - 0.172881 \\ 0.353390u^{15} - 0.0483051u^{14} + \dots - 0.122881u - 2.32712 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.146610u^{15} + 0.0483051u^{14} + \dots + 0.622881u - 0.172881 \\ 0.353390u^{15} - 0.0483051u^{14} + \dots - 0.122881u - 2.32712 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_7^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.157569 - 0.635502I$ $a = 0.557421 - 0.896927I$ $b = -1.27411 + 2.07243I$ $c = 0.63638 - 1.29602I$ $d = -1.46293 + 2.03683I$	$5.44991 - 9.88301I$	$3.28252 + 6.06963I$
$u = -1.157569 + 0.635502I$ $a = 0.557421 + 0.896927I$ $b = -1.27411 - 2.07243I$ $c = 0.63638 + 1.29602I$ $d = -1.46293 - 2.03683I$	$5.44991 + 9.88301I$	$3.28252 - 6.06963I$
$u = -1.076279 - 0.402850I$ $a = 0.496617 - 0.712709I$ $b = -0.12673 + 2.50547I$ $c = 0.018628 + 1.062865I$ $d = -0.10060 - 1.65754I$	$-4.77492 - 2.26376I$	$-6.05872 + 4.53378I$
$u = -1.076279 + 0.402850I$ $a = 0.496617 + 0.712709I$ $b = -0.12673 - 2.50547I$ $c = 0.018628 - 1.062865I$ $d = -0.10060 + 1.65754I$	$-4.77492 + 2.26376I$	$-6.05872 - 4.53378I$
$u = -0.783583$ $a = -0.701860$ $b = -2.11028$ $c = 0.560255$ $d = -0.122887$	-2.57083	2.16015
$u = -0.754559 - 0.841472I$ $a = -0.820135 + 0.914602I$ $b = 0.604123 - 0.352309I$ $c = -0.535511 + 0.275794I$ $d = -0.355898 + 0.718293I$	10.1546	6.33746

Solution to I_7^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.754559 + 0.841472I$ $a = -0.820135 - 0.914602I$ $b = 0.604123 + 0.352309I$ $c = -0.535511 - 0.275794I$ $d = -0.355898 - 0.718293I$	10.1546	6.33746
$u = -0.270006 - 0.967768I$ $a = 0.980795 - 0.982086I$ $b = 0.487066 - 0.220623I$ $c = -1.28957 + 1.26937I$ $d = 0.589201 + 0.010347I$	$5.44991 + 9.88301I$	$3.28252 - 6.06963I$
$u = -0.270006 + 0.967768I$ $a = 0.980795 + 0.982086I$ $b = 0.487066 + 0.220623I$ $c = -1.28957 - 1.26937I$ $d = 0.589201 - 0.010347I$	$5.44991 - 9.88301I$	$3.28252 + 6.06963I$
$u = 0.365525 - 0.776365I$ $a = 0.923174 - 0.991527I$ $b = 0.895563 + 0.792065I$ $c = -1.43774 - 0.96789I$ $d = 0.544344 - 0.362514I$	$2.93531 - 3.55755I$	$2.52739 + 2.62489I$
$u = 0.365525 + 0.776365I$ $a = 0.923174 + 0.991527I$ $b = 0.895563 - 0.792065I$ $c = -1.43774 + 0.96789I$ $d = 0.544344 + 0.362514I$	$2.93531 + 3.55755I$	$2.52739 - 2.62489I$
$u = 0.993914 - 0.569061I$ $a = -0.795774 + 0.630139I$ $b = 0.15894 - 1.76185I$ $c = -0.257812 + 1.346396I$ $d = -0.68234 - 2.09325I$	$2.93531 + 3.55755I$	$2.52739 - 2.62489I$

Solution to I_7^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.993914 + 0.569061I$ $a = -0.795774 - 0.630139I$ $b = 0.15894 + 1.76185I$ $c = -0.257812 - 1.346396I$ $d = -0.68234 + 2.09325I$	$2.93531 - 3.55755I$	$2.52739 + 2.62489I$
$u = 1.12630$ $a = 0.488295$ $b = -0.878073$ $c = 1.95645$ $d = -2.26074$	-2.57083	2.16015
$u = 1.227616 - 0.270214I$ $a = -0.735315 + 0.300028I$ $b = 1.24932 - 1.12484I$ $c = 0.60727 - 1.55946I$ $d = -0.83996 + 2.05652I$	$-4.77492 - 2.26376I$	$-6.05872 + 4.53378I$
$u = 1.227616 + 0.270214I$ $a = -0.735315 - 0.300028I$ $b = 1.24932 + 1.12484I$ $c = 0.60727 + 1.55946I$ $d = -0.83996 - 2.05652I$	$-4.77492 + 2.26376I$	$-6.05872 - 4.53378I$

VIII. $I_8^u = \langle u^{17} - 3u^{15} + \dots + 4d - 3, u^{18} + u^{17} + \dots + 2b - 1, u^{19} + 2u^{18} + \dots + 3u + 1, -2u^{18} - 3u^{17} + \dots + 2a - 4, -u^{18} - 2u^{17} + \dots + 2c - 5 \rangle$

(i) Arc colorings

$$\begin{aligned}
a_2 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\
a_4 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\
a_5 &= \begin{pmatrix} -u \\ u \end{pmatrix} \\
a_{10} &= \begin{pmatrix} \frac{1}{2}u^{18} + u^{17} + \dots - u + \frac{5}{2} \\ -\frac{1}{4}u^{17} + \frac{3}{4}u^{15} + \dots - \frac{1}{4}u + \frac{3}{4} \end{pmatrix} \\
a_{11} &= \begin{pmatrix} \frac{1}{2}u^{18} + \frac{3}{4}u^{17} + \dots - \frac{3}{4}u + \frac{11}{4} \\ -\frac{1}{2}u^{15} + 2u^{13} + \dots - \frac{1}{2}u + \frac{1}{2} \end{pmatrix} \\
a_6 &= \begin{pmatrix} -\frac{1}{2}u^{18} - u^{17} + \dots + u - 2 \\ -\frac{1}{4}u^{18} - \frac{1}{2}u^{17} + \dots + \frac{5}{4}u - \frac{1}{2} \end{pmatrix} \\
a_1 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\
a_8 &= \begin{pmatrix} u^{18} + \frac{3}{2}u^{17} + \dots - \frac{1}{2}u + 2 \\ -\frac{1}{2}u^{18} - \frac{1}{2}u^{17} + \dots - \frac{1}{2}u + \frac{1}{2} \end{pmatrix} \\
a_3 &= \begin{pmatrix} -u^2 + 1 \\ u^4 \end{pmatrix} \\
a_7 &= \begin{pmatrix} \frac{1}{2}u^{18} + u^{17} + \dots - \frac{1}{2}u + \frac{3}{2} \\ -\frac{1}{2}u^{15} + u^{13} + \dots - \frac{1}{2}u + \frac{1}{2} \end{pmatrix} \\
a_9 &= \begin{pmatrix} \frac{1}{2}u^{18} + u^{17} + \dots - u + 2 \\ -\frac{1}{4}u^{17} - \frac{1}{2}u^{16} + \dots + \frac{1}{4}u + \frac{3}{4} \end{pmatrix} \\
a_9 &= \begin{pmatrix} \frac{1}{2}u^{18} + u^{17} + \dots - u + 2 \\ -\frac{1}{4}u^{17} - \frac{1}{2}u^{16} + \dots + \frac{1}{4}u + \frac{3}{4} \end{pmatrix}
\end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_g^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.219915 - 0.612443I$ $a = -0.516047 + 0.911869I$ $b = 1.40218 - 2.37571I$ $c = 0.88613 - 1.46384I$ $d = -1.68494 + 2.18403I$	$2.5538 - 15.5977I$	$0.09598 + 9.40344I$
$u = -1.219915 + 0.612443I$ $a = -0.516047 - 0.911869I$ $b = 1.40218 + 2.37571I$ $c = 0.88613 + 1.46384I$ $d = -1.68494 - 2.18403I$	$2.5538 + 15.5977I$	$0.09598 - 9.40344I$
$u = -1.163712 - 0.575900I$ $a = 0.528681 - 0.867726I$ $b = -1.07974 + 2.29207I$ $c = -0.55106 + 1.42435I$ $d = 0.38413 - 2.13228I$	$-2.61225 - 10.89709I$	$-3.23641 + 8.50579I$
$u = -1.163712 + 0.575900I$ $a = 0.528681 + 0.867726I$ $b = -1.07974 - 2.29207I$ $c = -0.55106 - 1.42435I$ $d = 0.38413 + 2.13228I$	$-2.61225 + 10.89709I$	$-3.23641 - 8.50579I$
$u = -0.892218 - 0.798617I$ $a = 0.745739 - 0.908893I$ $b = -0.917511 + 0.756234I$ $c = -0.171773 - 0.152659I$ $d = -0.711062 + 1.057967I$	$9.74824 - 5.99256I$	$5.35093 + 5.49640I$
$u = -0.892218 + 0.798617I$ $a = 0.745739 + 0.908893I$ $b = -0.917511 - 0.756234I$ $c = -0.171773 + 0.152659I$ $d = -0.711062 - 1.057967I$	$9.74824 + 5.99256I$	$5.35093 - 5.49640I$

Solution to I_g^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.713652 - 0.621261I$ $a = -0.837060 + 0.785608I$ $b = 0.081748 - 0.770811I$ $c = -0.755312 + 0.014797I$ $d = 0.830029 - 0.977305I$	$2.40223 - 3.63220I$	$3.52732 + 6.81616I$
$u = -0.713652 + 0.621261I$ $a = -0.837060 - 0.785608I$ $b = 0.081748 + 0.770811I$ $c = -0.755312 - 0.014797I$ $d = 0.830029 + 0.977305I$	$2.40223 + 3.63220I$	$3.52732 - 6.81616I$
$u = -0.379493 - 0.913957I$ $a = -0.963127 + 0.958960I$ $b = -0.245388 + 0.138357I$ $c = -1.20852 + 1.09732I$ $d = 0.418501 + 0.149638I$	$7.80660 + 4.21764I$	$6.24313 - 1.77538I$
$u = -0.379493 + 0.913957I$ $a = -0.963127 - 0.958960I$ $b = -0.245388 - 0.138357I$ $c = -1.20852 - 1.09732I$ $d = 0.418501 - 0.149638I$	$7.80660 - 4.21764I$	$6.24313 + 1.77538I$
$u = -0.266152$ $a = 1.86845$ $b = 0.545293$ $c = 2.41374$ $d = 0.742345$	1.20822	9.19790
$u = 0.587370 - 0.660248I$ $a = -0.821562 + 0.916371I$ $b = -0.609822 - 1.161649I$ $c = -1.43138 - 0.24528I$ $d = 0.357611 - 0.863012I$	$4.14406 + 1.22871I$	$4.10945 - 3.37998I$

Solution to I_g^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.587370 + 0.660248I$ $a = -0.821562 - 0.916371I$ $b = -0.609822 + 1.161649I$ $c = -1.43138 + 0.24528I$ $d = 0.357611 + 0.863012I$	$4.14406 - 1.22871I$	$4.10945 + 3.37998I$
$u = 0.710407 - 0.203370I$ $a = 0.342230 - 0.841271I$ $b = -0.002742 + 0.868397I$ $c = 0.339488 + 0.027126I$ $d = 0.176169 + 0.449965I$	$-1.32552 + 1.22673I$	$-3.58366 - 5.47914I$
$u = 0.710407 + 0.203370I$ $a = 0.342230 + 0.841271I$ $b = -0.002742 - 0.868397I$ $c = 0.339488 - 0.027126I$ $d = 0.176169 - 0.449965I$	$-1.32552 - 1.22673I$	$-3.58366 + 5.47914I$
$u = 1.085303 - 0.470880I$ $a = -0.766359 + 0.526722I$ $b = 0.55681 - 1.65227I$ $c = -0.209548 - 1.125546I$ $d = 0.11074 + 1.77582I$	$-4.29720 + 4.85510I$	$-5.63265 - 5.33490I$
$u = 1.085303 + 0.470880I$ $a = -0.766359 - 0.526722I$ $b = 0.55681 + 1.65227I$ $c = -0.209548 + 1.125546I$ $d = 0.11074 - 1.77582I$	$-4.29720 - 4.85510I$	$-5.63265 + 5.33490I$
$u = 1.118985 - 0.584861I$ $a = 0.853281 - 0.557689I$ $b = -0.45818 + 2.04080I$ $c = 0.39510 + 1.48312I$ $d = -1.25236 - 2.20391I$	$0.71510 + 8.68076I$	$-0.47305 - 6.48182I$
Solution to I_g^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.118985 + 0.584861I$ $a = 0.853281 + 0.557689I$ $b = -0.45818 - 2.04080I$ $c = 0.39510 - 1.48312I$ $d = -1.25236 + 2.20391I$	$0.71510 - 8.68076I$	$-0.47305 + 6.48182I$

$$\text{IX. } I_1^v = \langle b, c, d - 1, v - 1, a - 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_1^v	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = 1.00000$		
$a = 1.00000$		
$b = 0$	0	0
$c = 0$		
$d = 1.00000$		

X. u-Polynomials

Crossings	u-Polynomials at each crossings
c_1, c_4	$u(u-1)^3(u^6 + u^5 - u^4 - 2u^3 + u + 1)^3$ $(u^{12} - u^{11} - 4u^{10} + 2u^9 + 7u^8 + u^7 - 5u^6 - 5u^5 - u^4 + 3u^3 + 2u^2 + 1)$ $(u^{16} + u^{15} + \dots - 4u - 4)(u^{19} + 2u^{18} + \dots + 3u + 1)$
c_2	$u(u+1)^3(u^6 + 3u^5 + 5u^4 + 4u^3 + 2u^2 + u + 1)^3$ $(u^{12} + 9u^{11} + \dots - 4u + 1)(u^{16} + 7u^{15} + \dots + 40u + 16)$ $(u^{19} + 8u^{18} + \dots + 19u + 1)$
c_3, c_7	$u^4(u^6 + u^5 - u^4 - 2u^3 + u + 1)^5$ $(u^8 - 3u^7 + 3u^6 + 2u^5 - 8u^4 + 9u^3 - 3u^2 - 2u + 2)^2$ $(u^{19} + 2u^{18} + \dots + 4u^2 - 8)$
c_5	$u(u-1)(u+1)^2(u^6 - u^5 - u^4 + 2u^3 - u + 1)$ $(u^8 + u^7 - 4u^6 - 3u^5 + 5u^4 + u^3 - u^2 + 3u - 1)^2$ $(u^{12} + u^{11} - 4u^{10} - 2u^9 + 7u^8 - u^7 - 5u^6 + 5u^5 - u^4 - 3u^3 + 2u^2 + 1)^2$ $(u^{19} + 2u^{18} + \dots - 8u - 4)$
c_6, c_9	$u(u-1)^2(u+1)(u^6 + u^5 - u^4 - 2u^3 + u + 1)^3$ $(u^{12} - u^{11} - 4u^{10} + 2u^9 + 7u^8 + u^7 - 5u^6 - 5u^5 - u^4 + 3u^3 + 2u^2 + 1)$ $(u^{16} + u^{15} + \dots - 4u - 4)(u^{19} + 2u^{18} + \dots + 3u + 1)$
c_8	$u(u-1)(u+1)^2(u^6 + 3u^5 + 5u^4 + 4u^3 + 2u^2 + u + 1)^3$ $(u^{12} + 9u^{11} + \dots - 4u + 1)(u^{16} + 7u^{15} + \dots + 40u + 16)$ $(u^{19} + 8u^{18} + \dots + 19u + 1)$
c_{10}, c_{11}	$u(u+1)^3(u^6 - u^5 - u^4 + 2u^3 - u + 1)$ $(u^8 + u^7 - 4u^6 - 3u^5 + 5u^4 + u^3 - u^2 + 3u - 1)^2$ $(u^{12} + u^{11} - 4u^{10} - 2u^9 + 7u^8 - u^7 - 5u^6 + 5u^5 - u^4 - 3u^3 + 2u^2 + 1)^2$ $(u^{19} + 2u^{18} + \dots - 8u - 4)$

XI. Riley Polynomials

Crossings	Riley Polynomials at each crossings
c_1, c_4, c_6 c_9	$y(y-1)^3(y^6 - 3y^5 + 5y^4 - 4y^3 + 2y^2 - y + 1)^3$ $(y^{12} - 9y^{11} + \dots + 4y + 1)(y^{16} - 7y^{15} + \dots - 40y + 16)$ $(y^{19} - 8y^{18} + \dots + 19y - 1)$
c_2, c_8	$y(y-1)^3(y^6 + y^5 + 5y^4 + 6y^2 + 3y + 1)^3$ $(y^{12} - 13y^{11} + \dots - 12y + 1)(y^{16} + y^{15} + \dots - 544y + 256)$ $(y^{19} + 12y^{18} + \dots + 195y - 1)$
c_3, c_7	$y^4(y^6 - 3y^5 + 5y^4 - 4y^3 + 2y^2 - y + 1)^5$ $(y^8 - 3y^7 + 5y^6 - 4y^5 + 2y^4 - 13y^3 + 13y^2 - 16y + 4)^2$ $(y^{19} - 6y^{18} + \dots + 64y - 64)$
c_5, c_{10}, c_{11}	$y(y-1)^3(y^6 - 3y^5 + 5y^4 - 4y^3 + 2y^2 - y + 1)$ $(y^8 - 9y^7 + 32y^6 - 53y^5 + 31y^4 + 15y^3 - 15y^2 - 7y + 1)^2$ $(1 + 4y + 2y^2 - 23y^3 + 25y^4 - y^5 - 5y^6 - 33y^7 + 73y^8 - 68y^9 + 34y^{10} - 9y^{11} + y^{12})^2$ $(y^{19} - 18y^{18} + \dots + 88y - 16)$