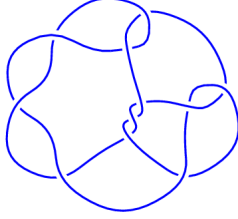
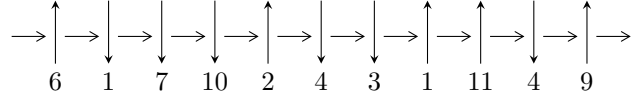


11n<sub>100</sub> (K11n<sub>100</sub>)

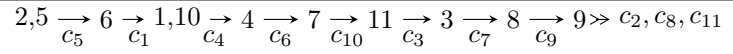


1

**Arc Sequences**



**Solving Sequence**



**Representation Ideals**

$$I = \bigcap_{i=1}^4 I_i^u$$

$$I_1^u = \langle u^2 - u + 1, a - 1, b - u + 1 \rangle$$

$$I_2^u = \langle b^6 + 2b^5 + 7b^4 + 4b^3 + 8b^2 - 2b + 5, -b^5 - 7b^3 - b^2 - 17b + 11u + 3, \\ -16b^5 - 33b^4 - 90b^3 - 49b^2 - 52b + 55a + 15 \rangle$$

$$I_3^u = \langle u^4 + u^3 + 2u^2 + 2u + 1, u^3 + a + 2u + 1, u^3 + u^2 + b + 3u + 2 \rangle$$

$$I_4^u = \langle u^{22} + u^{21} + \dots - 4u + 1, \\ 27401760606u^{21} + 32283303162u^{20} + \dots + 121906198036b + 36114460969, \\ 306481557535u^{21} + 364610096714u^{20} + \dots + 243812396072a - 76785066689 \rangle$$

There are 4 irreducible components with 34 representations.

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<sup>1</sup>The knot diagram image is adapter from “C. Livingston and A. H. Moore, KnotInfo: Table of Knot Invariants, <http://www.indiana.edu/~knotinfo>”

$$\mathbf{I. } I_1^u = \langle u^2 - u + 1, a - 1, b - u + 1 \rangle$$

**(i) Arc colorings**

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u \\ u - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ u - 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ u - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ u + 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u \\ u - 2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ -u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 2u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ -u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ -u \end{pmatrix}$$

**(ii) Obstruction class = -1**

**(iii) Cusp Shapes =unknown**

(iv) Complex Volumes and Cusp Shapes

Solution to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.500000 - 0.866025I$ $a = 1.00000$ $b = -0.500000 - 0.866025I$	$2.02988I$	$-3.46410I$
$u = 0.500000 + 0.866025I$ $a = 1.00000$ $b = -0.500000 + 0.866025I$	$-2.02988I$	$3.46410I$

$$\text{II. } I_2^u = (\overline{b^6 + 2b^5 + 7b^4 + 4b^3 + 8b^2 - 2b + 5}, -b^5 - 7b^3 - b^2 - 17b + 11u + 3, -16b^5 - 33b^4 + \dots + 55a + 15)$$

(i) Arc colorings

$$\begin{aligned} a_2 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 0 \\ 0.0909091b^5 + 0.636364b^3 + \dots + 1.54545b - 0.272727 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 0.0909091b^5 + 0.636364b^3 + \dots + 1.54545b - 0.272727 \\ 0.0909091b^5 + 0.636364b^3 + \dots + 1.54545b - 0.272727 \end{pmatrix} \\ a_1 &= \begin{pmatrix} 0 \\ -1 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} \frac{16}{55}b^5 + \frac{3}{5}b^4 + \dots + \frac{52}{55}b - \frac{3}{11} \\ b \end{pmatrix} \\ a_4 &= \begin{pmatrix} -0.0363636b^5 - 0.200000b^4 + \dots + 0.381818b + 0.909091 \\ -\frac{2}{55}b^5 - \frac{1}{5}b^4 + \dots + \frac{21}{55}b - \frac{1}{11} \end{pmatrix} \\ a_7 &= \begin{pmatrix} \frac{1}{55}b^5 - \frac{2}{5}b^4 + \dots + \frac{17}{55}b - \frac{5}{11} \\ \frac{8}{55}b^5 - \frac{2}{5}b^4 + \dots + \frac{102}{55}b - \frac{8}{11} \end{pmatrix} \\ a_{11} &= \begin{pmatrix} \frac{12}{55}b^5 + \frac{1}{5}b^4 + \dots - \frac{16}{55}b - \frac{16}{11} \\ -\frac{2}{55}b^5 - \frac{1}{5}b^4 + \dots + \frac{21}{55}b - \frac{1}{11} \end{pmatrix} \\ a_3 &= \begin{pmatrix} 1 \\ 1 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -\frac{4}{55}b^5 - \frac{2}{5}b^4 + \dots - \frac{68}{55}b - \frac{2}{11} \\ \frac{1}{55}b^5 - \frac{2}{5}b^4 + \dots + \frac{17}{55}b - \frac{5}{11} \end{pmatrix} \\ a_9 &= \begin{pmatrix} -\frac{4}{55}b^5 - \frac{2}{5}b^4 + \dots - \frac{68}{55}b - \frac{2}{11} \\ 0.0909091b^5 + 0.636364b^3 + \dots + 1.54545b - 0.272727 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -\frac{4}{55}b^5 - \frac{2}{5}b^4 + \dots - \frac{68}{55}b - \frac{2}{11} \\ 0.0909091b^5 + 0.636364b^3 + \dots + 1.54545b - 0.272727 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000I$ $a = -0.877439 - 0.744862I$ $b = -0.77736 - 1.96950I$	$-3.02413 + 2.82812I$	$-3.50976 - 2.97945I$
$u = -1.00000I$ $a = -0.877439 + 0.744862I$ $b = -0.77736 + 1.96950I$	$-3.02413 - 2.82812I$	$-3.50976 + 2.97945I$
$u = -1.00000I$ $a = 0.754878$ $b = -0.56984 - 1.32472I$	1.11345	3.01951
$u = 1.00000I$ $a = 0.754878$ $b = -0.56984 + 1.32472I$	1.11345	3.01951
$u = -1.00000I$ $a = -0.877439 - 0.744862I$ $b = 0.347200 - 0.644782I$	$-3.02413 + 2.82812I$	$-3.50976 - 2.97945I$
$u = 1.00000I$ $a = -0.877439 + 0.744862I$ $b = 0.347200 + 0.644782I$	$-3.02413 - 2.82812I$	$-3.50976 + 2.97945I$

$$\text{III. } I_3^u = \langle u^4 + u^3 + 2u^2 + 2u + 1, u^3 + a + 2u + 1, u^3 + u^2 + b + 3u + 2 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^3 - 2u - 1 \\ -u^3 - u^2 - 3u - 2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^3 \\ -u^3 + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^2 + 1 \\ -u^3 - 2u - 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^3 - u^2 - 2u \\ -u^3 - 2u^2 - 2u - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^3 - 2u - 1 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ -u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ -u \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.621744 - 0.440597I$		
$a = 0.121744 + 1.306622I$	$2.02988I$	$- 3.46410I$
$b = -0.448952 + 1.199342I$		
$u = -0.621744 + 0.440597I$		
$a = 0.121744 - 1.306622I$	$- 2.02988I$	$3.46410I$
$b = -0.448952 - 1.199342I$		
$u = 0.121744 - 1.306622I$		
$a = -0.621744 + 0.440597I$	$- 2.02988I$	$3.46410I$
$b = -0.05105 + 2.06537I$		
$u = 0.121744 + 1.306622I$		
$a = -0.621744 - 0.440597I$	$2.02988I$	$- 3.46410I$
$b = -0.05105 - 2.06537I$		

IV.

$$I_4^u = \langle u^{22} + u^{21} + \dots - 4u + 1, 2.74 \times 10^{10} u^{21} + 3.23 \times 10^{10} u^{20} + \dots + 1.22 \times 10^{11} b + 3.61 \times 10^{10}, 3.06 \times 10^{11} u^{21} + 3.65 \times 10^{11} u^{20} + \dots + 2.44 \times 10^{11} a - 7.68 \times 10^{10} \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1.25704u^{21} - 1.49545u^{20} + \dots - 21.5598u + 0.314935 \\ -0.224777u^{21} - 0.264821u^{20} + \dots - 4.42658u - 0.296248 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -0.520062u^{21} - 0.941512u^{20} + \dots - 6.20121u - 4.83139 \\ 0.0606928u^{21} + 0.0275143u^{20} + \dots + 1.35703u - 1.46367 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -1.80972u^{21} - 1.88500u^{20} + \dots - 30.6024u + 5.10082 \\ -0.421450u^{21} - 0.474311u^{20} + \dots - 5.91163u + 0.520062 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.329536u^{21} - 0.900218u^{20} + \dots - 1.13762u - 7.60006 \\ 0.0752832u^{21} - 0.00470735u^{20} + \dots + 2.13807u - 1.80972 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^4 + u^2 + 1 \\ u^4 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -1.46826u^{21} - 1.49856u^{20} + \dots - 25.1993u + 4.50547 \\ -0.426044u^{21} - 0.448508u^{20} + \dots - 5.90074u + 0.527894 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1.85194u^{21} + 1.93505u^{20} + \dots + 31.9010u - 5.07839 \\ 0.388271u^{21} + 0.410694u^{20} + \dots + 5.69074u - 0.580755 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1.85194u^{21} + 1.93505u^{20} + \dots + 31.9010u - 5.07839 \\ 0.388271u^{21} + 0.410694u^{20} + \dots + 5.69074u - 0.580755 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown



(iv) Complex Volumes and Cusp Shapes

Solution to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.153311 - 0.765089I$		
$a = 0.824436 + 0.428112I$	$9.48603 - 4.13683I$	$2.53393 + 2.55439I$
$b = -1.09341 + 1.04813I$		
$u = -1.153311 + 0.765089I$		
$a = 0.824436 - 0.428112I$	$9.48603 + 4.13683I$	$2.53393 - 2.55439I$
$b = -1.09341 - 1.04813I$		
$u = -1.07708 - 1.03335I$		
$a = -0.536672 - 0.615239I$	$13.19150 + 3.89903I$	$4.72901 - 2.42961I$
$b = 0.98592 - 2.18536I$		
$u = -1.07708 + 1.03335I$		
$a = -0.536672 + 0.615239I$	$13.19150 - 3.89903I$	$4.72901 + 2.42961I$
$b = 0.98592 + 2.18536I$		
$u = -0.90302 - 1.18611I$		
$a = 0.302390 + 0.821075I$	$8.10703 + 11.57362I$	$0.88963 - 6.62056I$
$b = -0.31975 + 2.72877I$		
$u = -0.90302 + 1.18611I$		
$a = 0.302390 - 0.821075I$	$8.10703 - 11.57362I$	$0.88963 + 6.62056I$
$b = -0.31975 - 2.72877I$		
$u = -0.595604 - 0.824126I$		
$a = 0.833215 - 0.205043I$	$-0.94737 + 2.13228I$	$-3.49508 - 3.26961I$
$b = 0.368315 + 0.238347I$		
$u = -0.595604 + 0.824126I$		
$a = 0.833215 + 0.205043I$	$-0.94737 - 2.13228I$	$-3.49508 + 3.26961I$
$b = 0.368315 - 0.238347I$		
$u = -0.217043 - 0.710982I$		
$a = 0.364202 + 0.538543I$	$-0.380875 + 1.140107I$	$-4.34193 - 6.22750I$
$b = -0.340220 + 0.348326I$		
$u = -0.217043 + 0.710982I$		
$a = 0.364202 - 0.538543I$	$-0.380875 - 1.140107I$	$-4.34193 + 6.22750I$
$b = -0.340220 - 0.348326I$		

Solution to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.029711 - 1.049821I$		
$a = -0.806902 - 0.721985I$	$-4.65093 + 2.79195I$	$-9.45575 - 3.06805I$
$b = -0.219039 - 1.369133I$		
$u = -0.029711 + 1.049821I$		
$a = -0.806902 + 0.721985I$	$-4.65093 - 2.79195I$	$-9.45575 + 3.06805I$
$b = -0.219039 + 1.369133I$		
$u = 0.106877 - 0.224236I$		
$a = -1.90450 + 4.32043I$	$-1.42494 - 2.89189I$	$2.45935 + 2.97630I$
$b = -0.711930 + 0.911129I$		
$u = 0.106877 + 0.224236I$		
$a = -1.90450 - 4.32043I$	$-1.42494 + 2.89189I$	$2.45935 - 2.97630I$
$b = -0.711930 - 0.911129I$		
$u = 0.678005 - 0.384923I$		
$a = -0.747656 + 1.056654I$	$3.57528 - 1.09357I$	$5.97662 + 1.94696I$
$b = 1.04546 + 1.57059I$		
$u = 0.678005 + 0.384923I$		
$a = -0.747656 - 1.056654I$	$3.57528 + 1.09357I$	$5.97662 - 1.94696I$
$b = 1.04546 - 1.57059I$		
$u = 0.778255 - 0.824454I$		
$a = 0.283395 - 1.014924I$	$0.39802 - 7.14623I$	$-0.40139 + 7.68801I$
$b = -0.68028 - 2.27208I$		
$u = 0.778255 + 0.824454I$		
$a = 0.283395 + 1.014924I$	$0.39802 + 7.14623I$	$-0.40139 - 7.68801I$
$b = -0.68028 + 2.27208I$		
$u = 0.89009 - 1.10133I$		
$a = 0.704841 + 0.246159I$	$6.44298 - 5.66281I$	$-0.84387 + 2.45088I$
$b = 0.497167 + 0.394085I$		
$u = 0.89009 + 1.10133I$		
$a = 0.704841 - 0.246159I$	$6.44298 + 5.66281I$	$-0.84387 - 2.45088I$
$b = 0.497167 - 0.394085I$		
Solution to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.022545 - 0.827721I$		
$a = -0.316750 - 0.661900I$	$7.32664 - 1.36370I$	$-0.05052 + 1.94758I$
$b = -0.032238 - 0.626280I$		
$u = 1.022545 + 0.827721I$		
$a = -0.316750 + 0.661900I$	$7.32664 + 1.36370I$	$-0.05052 - 1.94758I$
$b = -0.032238 + 0.626280I$		

### V. u-Polynomials

Crossings	u-Polynomials at each crossings
$c_1, c_5$	$(u^2 + 1)^3(u^2 - u + 1)(u^4 + u^3 + \dots + 2u + 1)(u^{22} + u^{21} + \dots - 4u + 1)$
$c_2$	$(u + 1)^6(u^2 + u + 1)(u^4 + 3u^3 + 2u^2 + 1)(u^{22} + 3u^{21} + \dots + 24u + 1)$
$c_3, c_6, c_7$	$(u^2 + 1)^3(u^2 - u + 1)(u^4 + u^3 + \dots + 2u + 1)(u^{22} + u^{21} + \dots - 10u + 1)$
$c_4, c_{10}$	$(u^2 + u + 1)^3(u^6 + u^4 + 2u^2 + 1)(u^{22} - 2u^{21} + \dots - u + 2)$
$c_8, c_9$	$(u^2 + u + 1)^3(1 + 2u + u^2 + u^3)^2(u^{22} + 8u^{21} + \dots + 19u + 4)$
$c_{11}$	$(u^2 + u + 1)^3(-1 + 2u - u^2 + u^3)^2(u^{22} + 8u^{21} + \dots + 19u + 4)$

## VI. Riley Polynomials

Crossings	Riley Polynomials at each crossings
$c_1, c_5$	$(y + 1)^6(y^2 + y + 1)(y^4 + 3y^3 + 2y^2 + 1)(y^{22} + 3y^{21} + \dots + 24y + 1)$
$c_2$	$(y - 1)^6(y^2 + y + 1)(y^4 - 5y^3 + 6y^2 + 4y + 1)$ $(y^{22} + 39y^{21} + \dots + 112y + 1)$
$c_3, c_6, c_7$	$(y + 1)^6(y^2 + y + 1)(y^4 + 3y^3 + 2y^2 + 1)(y^{22} + 31y^{21} + \dots + 56y + 1)$
$c_4, c_{10}$	$(y^2 + y + 1)^3(1 + 2y + y^2 + y^3)^2(y^{22} + 8y^{21} + \dots + 19y + 4)$
$c_8, c_9, c_{11}$	$(y^2 + y + 1)^3(-1 + 2y + 3y^2 + y^3)^2(y^{22} + 12y^{21} + \dots + 623y + 16)$