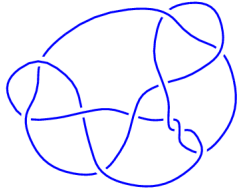
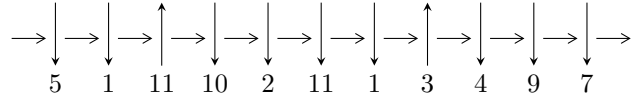


11n<sub>105</sub> (K11n<sub>105</sub>)

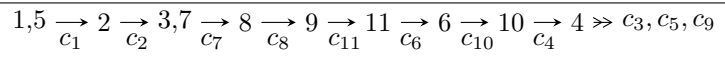


1

**Arc Sequences**



**Solving Sequence**



**Representation Ideals**

$$I = \bigcap_{i=1}^4 I_i^u$$

$$I_1^u = \langle a^4 - 4a^3 + 8a^2 - 8a + 5, u + 1, b - 1 \rangle$$

$$I_2^u = \langle u^{19} - u^{18} + \dots + 2u - 1, b - u, u^{17} - u^{16} + \dots + 8a + 1 \rangle$$

$$I_3^u = \langle u^{22} - u^{21} + \dots - 2u + 5, -u^{21} + u^{20} + \dots + 5a + 2, \\ 2918667u^{21} - 1662902u^{20} + \dots + 11494529b - 1518911 \rangle$$

$$I_4^u = \langle u - 1, a + 1, b + 1 \rangle$$

There are 4 irreducible components with 46 representations.

---

<sup>1</sup>The knot diagram image is adapter from “C. Livingston and A. H. Moore, KnotInfo: Table of Knot Invariants, <http://www.indiana.edu/~knotinfo>”

$$\mathbf{I. } I_1^u = \langle a^4 - 4a^3 + 8a^2 - 8a + 5, u + 1, b - 1 \rangle$$

**(i) Arc colorings**

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} a \\ 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} a - 1 \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} a - 1 \\ -a + 2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -a + 1 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -a^3 + 3a^2 - 4a + 2 \\ a^3 - 4a^2 + 5a - 3 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} a^2 - 2a + 1 \\ a \end{pmatrix}$$

$$a_4 = \begin{pmatrix} a^2 - 2a + 1 \\ a \end{pmatrix}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes =unknown**

(iv) Complex Volumes and Cusp Shapes

Solution to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.00000$ $a = 0.544910 - 1.098684I$ $b = 1.00000$	$-5.75727 + 3.66386I$	$-16.0000 - 4.0000I$
$u = -1.00000$ $a = 0.544910 + 1.098684I$ $b = 1.00000$	$-5.75727 - 3.66386I$	$-16.0000 + 4.0000I$
$u = -1.00000$ $a = 1.45509 - 1.09868I$ $b = 1.00000$	$-5.75727 - 3.66386I$	$-16.0000 + 4.0000I$
$u = -1.00000$ $a = 1.45509 + 1.09868I$ $b = 1.00000$	$-5.75727 + 3.66386I$	$-16.0000 - 4.0000I$

$$\text{II. } I_2^u = \langle u^{19} - u^{18} + \dots + 2u - 1, b - u, u^{17} - u^{16} + \dots + 8a + 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -\frac{1}{8}u^{17} + \frac{1}{8}u^{16} + \dots - \frac{7}{4}u - \frac{1}{8} \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -\frac{1}{8}u^{17} + \frac{1}{8}u^{16} + \dots - \frac{11}{4}u - \frac{1}{8} \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -\frac{1}{8}u^{17} + \frac{1}{8}u^{16} + \dots - \frac{7}{4}u - \frac{1}{8} \\ \frac{1}{8}u^{17} - \frac{1}{8}u^{16} + \dots + \frac{3}{4}u + \frac{1}{8} \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} \frac{1}{8}u^{18} - \frac{1}{8}u^{17} + \dots + \frac{1}{8}u + 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} \frac{11}{8}u^{18} - \frac{7}{4}u^{17} + \dots + \frac{33}{8}u + \frac{3}{8} \\ -\frac{5}{8}u^{18} + \frac{7}{8}u^{17} + \dots - \frac{23}{8}u + \frac{1}{2} \end{pmatrix}$$

$$a_4 = \begin{pmatrix} \frac{7}{8}u^{18} - u^{17} + \dots + \frac{11}{8}u + \frac{7}{8} \\ -\frac{1}{8}u^{18} + \frac{1}{8}u^{17} + \dots + \frac{5}{4}u^2 - \frac{1}{8}u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} \frac{7}{8}u^{18} - u^{17} + \dots + \frac{11}{8}u + \frac{7}{8} \\ -\frac{1}{8}u^{18} + \frac{1}{8}u^{17} + \dots + \frac{5}{4}u^2 - \frac{1}{8}u \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.107494 - 0.812678I$ $a = -0.57304 + 1.36863I$ $b = -1.107494 - 0.812678I$	$4.47255 - 8.26447I$	$-5.93446 + 4.83162I$
$u = -1.107494 + 0.812678I$ $a = -0.57304 - 1.36863I$ $b = -1.107494 + 0.812678I$	$4.47255 + 8.26447I$	$-5.93446 - 4.83162I$
$u = -0.968832 - 0.893275I$ $a = -0.382196 + 1.309221I$ $b = -0.968832 - 0.893275I$	$5.51436 - 5.01792I$	$-4.62542 + 4.88249I$
$u = -0.968832 + 0.893275I$ $a = -0.382196 - 1.309221I$ $b = -0.968832 + 0.893275I$	$5.51436 + 5.01792I$	$-4.62542 - 4.88249I$
$u = -0.777977 - 0.409956I$ $a = 0.48742 + 2.00922I$ $b = -0.777977 - 0.409956I$	$-4.54946 - 5.47873I$	$-11.07465 + 8.55667I$
$u = -0.777977 + 0.409956I$ $a = 0.48742 - 2.00922I$ $b = -0.777977 + 0.409956I$	$-4.54946 + 5.47873I$	$-11.07465 - 8.55667I$
$u = -0.697477 - 0.278835I$ $a = 1.21360 + 1.74151I$ $b = -0.697477 - 0.278835I$	$-4.36768 + 2.62850I$	$-9.97134 + 1.16882I$
$u = -0.697477 + 0.278835I$ $a = 1.21360 - 1.74151I$ $b = -0.697477 + 0.278835I$	$-4.36768 - 2.62850I$	$-9.97134 - 1.16882I$
$u = 0.133918 - 0.761043I$ $a = -0.043527 + 0.980596I$ $b = 0.133918 - 0.761043I$	$1.53985 + 2.22177I$	$-2.53368 - 4.26379I$
$u = 0.133918 + 0.761043I$ $a = -0.043527 - 0.980596I$ $b = 0.133918 + 0.761043I$	$1.53985 - 2.22177I$	$-2.53368 + 4.26379I$

Solution to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.395222$ $a = -0.936768$ $b = 0.395222$	$-0.957690$	$-10.9546$
$u = 0.647319 - 0.397441I$ $a = -0.67547 + 1.54605I$ $b = 0.647319 - 0.397441I$	$-1.23847 + 1.46671I$	$-6.68531 - 4.74531I$
$u = 0.647319 + 0.397441I$ $a = -0.67547 - 1.54605I$ $b = 0.647319 + 0.397441I$	$-1.23847 - 1.46671I$	$-6.68531 + 4.74531I$
$u = 0.887480 - 0.926590I$ $a = 0.297770 + 1.273124I$ $b = 0.887480 - 0.926590I$	$4.22972 - 0.35072I$	$-6.13837 + 0.22490I$
$u = 0.887480 + 0.926590I$ $a = 0.297770 - 1.273124I$ $b = 0.887480 + 0.926590I$	$4.22972 + 0.35072I$	$-6.13837 - 0.22490I$
$u = 1.033803 - 0.730109I$ $a = 0.49884 + 1.52309I$ $b = 1.033803 - 0.730109I$	$-0.86154 + 5.74817I$	$-11.63360 - 4.50327I$
$u = 1.033803 + 0.730109I$ $a = 0.49884 - 1.52309I$ $b = 1.033803 + 0.730109I$	$-0.86154 - 5.74817I$	$-11.63360 + 4.50327I$
$u = 1.151649 - 0.788448I$ $a = 0.64498 + 1.37321I$ $b = 1.151649 - 0.788448I$	$2.31925 + 13.64210I$	$-8.92588 - 8.81475I$
$u = 1.151649 + 0.788448I$ $a = 0.64498 - 1.37321I$ $b = 1.151649 + 0.788448I$	$2.31925 - 13.64210I$	$-8.92588 + 8.81475I$

$$\text{III. } I_3^u = \langle u^{22} - u^{21} + \dots - 2u + 5, -u^{21} + u^{20} + \dots + 5a + 2, 2.92 \times 10^6 u^{21} - 1.66 \times 10^6 u^{20} + \dots + 1.15 \times 10^7 b - 1.52 \times 10^6 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} \frac{1}{5}u^{21} - \frac{1}{5}u^{20} + \dots - \frac{22}{5}u - \frac{2}{5} \\ -0.253918u^{21} + 0.144669u^{20} + \dots - 2.56818u + 0.132142 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0.453918u^{21} - 0.344669u^{20} + \dots - 1.83182u - 0.532142 \\ -0.253918u^{21} + 0.144669u^{20} + \dots - 2.56818u + 0.132142 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.531094u^{21} - 0.655649u^{20} + \dots - 4.45109u - 0.946245 \\ -0.585012u^{21} + 0.600318u^{20} + \dots - 1.51708u + 0.678387 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.0264284u^{21} - 0.227490u^{20} + \dots - 0.137095u - 1.51532 \\ -0.109249u^{21} - 0.221845u^{20} + \dots - 0.375694u + 0.269590 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.136175u^{21} + 0.0168155u^{20} + \dots + 2.42666u - 0.867149 \\ 0.278577u^{21} - 0.861057u^{20} + \dots - 2.18135u - 2.39173 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.207376u^{21} - 0.422121u^{20} + \dots + 0.122656u - 0.129439 \\ -0.0945157u^{21} - 0.235897u^{20} + \dots - 1.35042u - 1.58175 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.207376u^{21} - 0.422121u^{20} + \dots + 0.122656u - 0.129439 \\ -0.0945157u^{21} - 0.235897u^{20} + \dots - 1.35042u - 1.58175 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.282542 - 0.010543I$		
$a = 0.779649 - 0.006409I$	$-3.66655 - 4.75030I$	$-9.35891 + 6.77690I$
$b = 0.620308 + 0.489049I$		
$u = -1.282542 + 0.010543I$		
$a = 0.779649 + 0.006409I$	$-3.66655 + 4.75030I$	$-9.35891 - 6.77690I$
$b = 0.620308 - 0.489049I$		
$u = -1.195773 - 0.178364I$		
$a = 0.818078 - 0.122026I$	$-4.92613 - 1.27541I$	$-13.47945 + 0.80097I$
$b = 0.968725 - 0.342171I$		
$u = -1.195773 + 0.178364I$		
$a = 0.818078 + 0.122026I$	$-4.92613 + 1.27541I$	$-13.47945 - 0.80097I$
$b = 0.968725 + 0.342171I$		
$u = -0.892154 - 0.917804I$		
$a = 0.544560 - 0.560216I$	$5.74879 - 1.64593I$	$-3.95012 + 0.24481I$
$b = -0.703026 + 0.993334I$		
$u = -0.892154 + 0.917804I$		
$a = 0.544560 + 0.560216I$	$5.74879 + 1.64593I$	$-3.95012 - 0.24481I$
$b = -0.703026 - 0.993334I$		
$u = -0.703026 - 0.993334I$		
$a = 0.474710 - 0.670738I$	$5.74879 + 1.64593I$	$-3.95012 - 0.24481I$
$b = -0.892154 + 0.917804I$		
$u = -0.703026 + 0.993334I$		
$a = 0.474710 + 0.670738I$	$5.74879 - 1.64593I$	$-3.95012 + 0.24481I$
$b = -0.892154 - 0.917804I$		
$u = -0.520797 - 0.242115I$		
$a = 1.57889 - 0.73402I$	$-1.99990 - 0.45477I$	$-4.80492 + 1.36957I$
$b = 1.182923 + 0.018546I$		
$u = -0.520797 + 0.242115I$		
$a = 1.57889 + 0.73402I$	$-1.99990 + 0.45477I$	$-4.80492 - 1.36957I$
$b = 1.182923 - 0.018546I$		



Solution to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.620308 - 0.489049I$ $a = -0.994161 - 0.783795I$ $b = -1.282542 + 0.010543I$	$-3.66655 + 4.75030I$	$-9.35891 - 6.77690I$
$u = 0.620308 + 0.489049I$ $a = -0.994161 + 0.783795I$ $b = -1.282542 - 0.010543I$	$-3.66655 - 4.75030I$	$-9.35891 + 6.77690I$
$u = 0.624756 - 1.026888I$ $a = -0.432411 - 0.710738I$ $b = 0.967997 + 0.889244I$	$3.97498 - 7.02220I$	$-6.49946 + 4.88619I$
$u = 0.624756 + 1.026888I$ $a = -0.432411 + 0.710738I$ $b = 0.967997 - 0.889244I$	$3.97498 + 7.02220I$	$-6.49946 - 4.88619I$
$u = 0.729583 - 0.772577I$ $a = -0.646125 - 0.684201I$ $b = 0.729583 + 0.772577I$	$0.0927065$	$-9.81428$
$u = 0.729583 + 0.772577I$ $a = -0.646125 + 0.684201I$ $b = 0.729583 - 0.772577I$	$0.0927065$	$-9.81428$
$u = 0.967997 - 0.889244I$ $a = -0.560257 - 0.514676I$ $b = 0.624756 + 1.026888I$	$3.97498 + 7.02220I$	$-6.49946 - 4.88619I$
$u = 0.967997 + 0.889244I$ $a = -0.560257 + 0.514676I$ $b = 0.624756 - 1.026888I$	$3.97498 - 7.02220I$	$-6.49946 + 4.88619I$
$u = 0.968725 - 0.342171I$ $a = -0.917780 - 0.324176I$ $b = -1.195773 - 0.178364I$	$-4.92613 - 1.27541I$	$-13.47945 + 0.80097I$
$u = 0.968725 + 0.342171I$ $a = -0.917780 + 0.324176I$ $b = -1.195773 + 0.178364I$	$-4.92613 + 1.27541I$	$-13.47945 - 0.80097I$
Solution to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.182923 - 0.018546I$ $a = -0.845156 - 0.013250I$ $b = -0.520797 + 0.242115I$	$-1.99990 + 0.45477I$	$-4.80492 - 1.36957I$
$u = 1.182923 + 0.018546I$ $a = -0.845156 + 0.013250I$ $b = -0.520797 - 0.242115I$	$-1.99990 - 0.45477I$	$-4.80492 + 1.36957I$

$$\text{IV. } I_4^u = \langle u - 1, a + 1, b + 1 \rangle$$

**(i) Arc colorings**

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

**(ii) Obstruction class = -1**

**(iii) Cusp Shapes =unknown**

(iv) Complex Volumes and Cusp Shapes

Solution to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$		
$a = -1.00000$	-3.28987	-12.0000
$b = -1.00000$		

## V. u-Polynomials

Crossings	u-Polynomials at each crossings
$c_1$	$(u+1)^5(u^{19} + u^{18} + \dots + 2u + 1)(u^{22} + u^{21} + \dots + 2u + 5)$
$c_2$	$(u+1)^5(u^{19} + 5u^{18} + \dots + 10u + 1)(u^{22} + 9u^{21} + \dots + 224u + 25)$
$c_3$	$u(u^4 + 2u^2 + 2)$ $(u^{11} - 3u^{10} + 4u^9 - u^8 + 2u^7 - 8u^6 + 8u^5 + 5u^4 - 3u^3 - u^2 + 4u - 1)^2$ $(u^{19} + 9u^{18} + \dots + 106u + 14)$
$c_4, c_9$	$(u)(u^4 - 2u^2 + 2)(1 - u^2 - u^3 + 3u^4 - 4u^6 + 2u^7 + 3u^8 - 2u^9 - u^{10} + u^{11})^2$ $(u^{19} + 3u^{18} + \dots + 6u + 2)$
$c_5$	$(u-1)^4(u+1)(u^{19} + u^{18} + \dots + 2u + 1)(u^{22} + u^{21} + \dots + 2u + 5)$
$c_6, c_7$	$(u-1)(u+1)^4(u^{19} + u^{18} + \dots + 2u + 1)(u^{22} + u^{21} + \dots + 2u + 5)$
$c_8$	$u(u^4 + 2u^2 + 2)$ $(u^{11} - u^{10} - 6u^9 + 5u^8 + 12u^7 - 6u^6 - 10u^5 - u^4 + 5u^3 + u^2 - 1)^2$ $(u^{19} + 3u^{18} + \dots - 70u - 26)$
$c_{10}$	$u(u^2 + 2u + 2)^2$ $(1 + 2u + 7u^2 + 15u^3 + 23u^4 + 28u^5 + 32u^6 + 32u^7 + 25u^8 + 14u^9 + 5u^{10} + u^{11})^2$ $(u^{19} + 9u^{18} + \dots + 4u + 4)$
$c_{11}$	$(u-1)^5(u^{19} + u^{18} + \dots + 2u + 1)(u^{22} + u^{21} + \dots + 2u + 5)$

## VI. Riley Polynomials

Crossings	Riley Polynomials at each crossings
$c_1, c_5, c_6$ $c_7, c_{11}$	$(y - 1)^5(y^{19} - 5y^{18} + \dots + 10y - 1)(y^{22} - 9y^{21} + \dots - 224y + 25)$
$c_2$	$(y - 1)^5(y^{19} + 27y^{18} + \dots + 38y - 1)(y^{22} + 7y^{21} + \dots + 5624y + 625)$
$c_3$	$y(y^2 + 2y + 2)^2$ $(-1 + 14y - 15y^2 + 67y^3 - 75y^4 + 156y^5 - 44y^6 + 76y^7 - 17y^8 + 14y^9 - y^{10} + y^{11})^2$ $(y^{19} + 3y^{18} + \dots + 1044y - 196)$
$c_4, c_9$	$y(y^2 - 2y + 2)^2$ $(-1 + 2y - 7y^2 + 15y^3 - 23y^4 + 28y^5 - 32y^6 + 32y^7 - 25y^8 + 14y^9 - 5y^{10} + y^{11})^2$ $(y^{19} - 9y^{18} + \dots + 4y - 4)$
$c_8$	$y(y^2 + 2y + 2)^2$ $(-1 + 2y - 3y^2 + 15y^3 - 79y^4 + 196y^5 - 324y^6 + 332y^7 - 201y^8 + 70y^9 - 13y^{10} + y^{11})^2$ $(y^{19} - 9y^{18} + \dots - 14444y - 676)$
$c_{10}$	$y(y^2 + 4)^2$ $(-1 - 10y - 35y^2 - 49y^3 - 59y^4 - 32y^5 - 28y^6 + 8y^7 + 7y^8 + 10y^9 + 3y^{10} + y^{11})^2$ $(y^{19} + 3y^{18} + \dots + 144y - 16)$