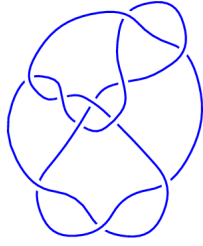
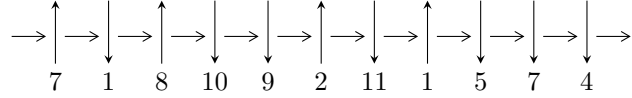


11n<sub>117</sub> (K11n<sub>117</sub>)

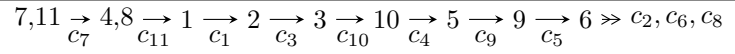


1

**Arc Sequences**



**Solving Sequence**



**Representation Ideals**

$$I = \bigcap_{i=1}^3 I_i^u$$

$$I_1^u = \langle u^8 + u^7 - u^6 - u^5 + u^4 - 2u^3 - u^2 + 2u + 1, a + 1, 5u^7 + 2u^6 - 6u^5 - u^4 + 6u^3 - 13u^2 + b + 3u + 8 \rangle$$

$$I_2^u = \langle u^{12} + 3u^{11} + 2u^{10} - 7u^9 - 20u^8 - u^7 + 57u^6 + 27u^5 - 70u^4 - 40u^3 + 42u^2 + 36u + 7, \\ 72072u^{11} + 189790u^{10} + \dots + 888545b + 231518, \\ 6556604u^{11} + 16709340u^{10} + \dots + 888545a + 103019776 \rangle$$

$$I_3^u = \langle u^{13} + u^{12} - 7u^{11} - 7u^{10} + 22u^9 + 18u^8 - 37u^7 - 18u^6 + 31u^5 + 5u^4 - u^3 + 9u^2 - u + 1, a - 1, \\ 94u^{12} - 167u^{11} + \dots + 1561b + 2486 \rangle$$

There are 3 irreducible components with 33 representations.

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<sup>1</sup>The knot diagram image is adapter from “C. Livingston and A. H. Moore, KnotInfo: Table of Knot Invariants, <http://www.indiana.edu/~knotinfo>”

$$I_1^u = \langle u^8 + u^7 - u^6 - u^5 + u^4 - 2u^3 - u^2 + 2u + 1, a + 1, 5u^7 + 2u^6 + \dots + b + 8 \rangle \quad \mathbf{I.}$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -1 \\ -5u^7 - 2u^6 + 6u^5 + u^4 - 6u^3 + 13u^2 - 3u - 8 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u \\ 3u^7 + u^6 - 4u^5 - u^4 + 3u^3 - 8u^2 + 3u + 5 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 5u^7 + 2u^6 - 6u^5 - u^4 + 6u^3 - 13u^2 + 3u + 7 \\ -5u^7 - 2u^6 + 6u^5 + u^4 - 6u^3 + 13u^2 - 3u - 8 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 5u^7 + 2u^6 - 6u^5 - u^4 + 6u^3 - 13u^2 + 3u + 7 \\ -7u^7 - 3u^6 + 8u^5 + u^4 - 8u^3 + 19u^2 - 4u - 11 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 2u^7 + u^6 - 2u^5 + 2u^3 - 6u^2 + u + 4 \\ -2u^7 - u^6 + 2u^5 - 2u^3 + 6u^2 - u - 4 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1 \\ -5u^7 - 2u^6 + 6u^5 + u^4 - 6u^3 + 14u^2 - 3u - 8 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 5u^7 + 2u^6 - 6u^5 - u^4 + 6u^3 - 14u^2 + 3u + 9 \\ -u^7 - u^6 + u^5 + u^4 - u^3 + 2u^2 + u - 3 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -4u^7 - u^6 + 5u^5 - 5u^3 + 12u^2 - 4u - 6 \\ 8u^7 + 3u^6 - 10u^5 - 2u^4 + 9u^3 - 22u^2 + 6u + 13 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -4u^7 - 2u^6 + 5u^5 + 2u^4 - 4u^3 + 10u^2 - 2u - 7 \\ 2u^7 + u^6 - 3u^5 - u^4 + 3u^3 - 5u^2 + 4 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -4u^7 - 2u^6 + 5u^5 + 2u^4 - 4u^3 + 10u^2 - 2u - 7 \\ 2u^7 + u^6 - 3u^5 - u^4 + 3u^3 - 5u^2 + 4 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.25100 - 0.69398I$ $a = -1.00000$ $b = -0.950543 - 0.460045I$	$1.36880 - 3.95256I$	$-4.43548 + 5.62596I$
$u = -1.25100 + 0.69398I$ $a = -1.00000$ $b = -0.950543 + 0.460045I$	$1.36880 + 3.95256I$	$-4.43548 - 5.62596I$
$u = -0.611947 - 0.066347I$ $a = -1.00000$ $b = -0.31597 + 1.53684I$	$5.52534 + 1.23864I$	$-6.14816 - 0.14411I$
$u = -0.611947 + 0.066347I$ $a = -1.00000$ $b = -0.31597 - 1.53684I$	$5.52534 - 1.23864I$	$-6.14816 + 0.14411I$
$u = 0.341560 - 1.033288I$ $a = -1.00000$ $b = 0.495908 - 0.252645I$	$-5.09351 - 1.73790I$	$-1.280471 + 0.424799I$
$u = 0.341560 + 1.033288I$ $a = -1.00000$ $b = 0.495908 + 0.252645I$	$-5.09351 + 1.73790I$	$-1.280471 - 0.424799I$
$u = 1.021384 - 0.213700I$ $a = -1.00000$ $b = -0.729400 + 0.802470I$	$-1.80062 + 2.46434I$	$-3.13589 - 4.70044I$
$u = 1.021384 + 0.213700I$ $a = -1.00000$ $b = -0.729400 - 0.802470I$	$-1.80062 - 2.46434I$	$-3.13589 + 4.70044I$

**II.**

$$I_2^u = \langle u^{12} + 3u^{11} + \dots + 36u + 7, 7.21 \times 10^4 u^{11} + 1.90 \times 10^5 u^{10} + \dots + 8.89 \times 10^5 b + 2.32 \times 10^5, 6.56 \times 10^6 u^{11} + 1.67 \times 10^7 u^{10} + \dots + 8.89 \times 10^5 a + 1.03 \times 10^8 \rangle$$

**(i) Arc colorings**

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -7.37903u^{11} - 18.8053u^{10} + \dots - 335.903u - 115.942 \\ -0.0811124u^{11} - 0.213596u^{10} + \dots - 3.97130u - 0.260559 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -10.2405u^{11} - 26.9108u^{10} + \dots - 484.537u - 184.723 \\ -2.29311u^{11} - 5.89495u^{10} + \dots - 104.039u - 36.9707 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -7.29792u^{11} - 18.5917u^{10} + \dots - 331.931u - 115.682 \\ -0.0811124u^{11} - 0.213596u^{10} + \dots - 3.97130u - 0.260559 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -7.29792u^{11} - 18.5917u^{10} + \dots - 331.931u - 115.682 \\ 1.48146u^{11} + 3.67868u^{10} + \dots + 63.8181u + 22.8540 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 16.7580u^{11} + 42.6418u^{10} + \dots + 759.709u + 254.261 \\ -0.416600u^{11} - 1.11739u^{10} + \dots - 20.2427u - 10.1023 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -7.37903u^{11} - 18.8053u^{10} + \dots - 335.903u - 115.942 \\ 1.45698u^{11} + 3.67361u^{10} + \dots + 64.3210u + 23.0622 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -1.47078u^{11} - 3.43428u^{10} + \dots - 59.7071u - 12.4125 \\ 1.45698u^{11} + 3.67361u^{10} + \dots + 64.3210u + 22.0622 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -0.0138012u^{11} + 0.239329u^{10} + \dots + 4.61383u + 9.64967 \\ 1.45698u^{11} + 3.67361u^{10} + \dots + 64.3210u + 22.0622 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 5.89445u^{11} + 15.6103u^{10} + \dots + 280.809u + 112.179 \\ 1.45698u^{11} + 3.67361u^{10} + \dots + 64.3210u + 21.0622 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 5.89445u^{11} + 15.6103u^{10} + \dots + 280.809u + 112.179 \\ 1.45698u^{11} + 3.67361u^{10} + \dots + 64.3210u + 21.0622 \end{pmatrix}$$

**(ii) Obstruction class = -1**

**(iii) Cusp Shapes = unknown**

(iv) Complex Volumes and Cusp Shapes

Solution to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.68307 - 0.58734I$		
$a = -0.654754 - 0.127174I$	$-1.91067 - 4.85801I$	$-4.49024 + 6.44355I$
$b = -0.877439 - 0.744862I$		
$u = -1.68307 + 0.58734I$		
$a = -0.654754 + 0.127174I$	$-1.91067 + 4.85801I$	$-4.49024 - 6.44355I$
$b = -0.877439 + 0.744862I$		
$u = -0.993753 - 0.194653I$		
$a = -1.199426 + 0.616214I$	$-1.91067 - 0.79824I$	$-4.49024 - 0.48465I$
$b = -0.877439 - 0.744862I$		
$u = -0.993753 + 0.194653I$		
$a = -1.199426 - 0.616214I$	$-1.91067 + 0.79824I$	$-4.49024 + 0.48465I$
$b = -0.877439 + 0.744862I$		
$u = -0.73677 - 1.98368I$		
$a = 0.083130 - 0.183668I$	$-6.04826 + 2.02988I$	$-11.01951 - 3.46410I$
$b = 0.754878$		
$u = -0.73677 + 1.98368I$		
$a = 0.083130 + 0.183668I$	$-6.04826 - 2.02988I$	$-11.01951 + 3.46410I$
$b = 0.754878$		
$u = -0.425587 - 0.029583I$		
$a = 2.04530 + 4.51888I$	$-6.04826 + 2.02988I$	$-11.01951 - 3.46410I$
$b = 0.754878$		
$u = -0.425587 + 0.029583I$		
$a = 2.04530 - 4.51888I$	$-6.04826 - 2.02988I$	$-11.01951 + 3.46410I$
$b = 0.754878$		
$u = 1.027305 - 0.598610I$		
$a = -1.47177 - 0.28586I$	$-1.91067 + 4.85801I$	$-4.49024 - 6.44355I$
$b = -0.877439 + 0.744862I$		
$u = 1.027305 + 0.598610I$		
$a = -1.47177 + 0.28586I$	$-1.91067 - 4.85801I$	$-4.49024 + 6.44355I$
$b = -0.877439 - 0.744862I$		

Solution to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.311881 - 0.378892I$		
$a = -0.659626 - 0.338888I$	$-1.91067 - 0.79824I$	$-4.49024 - 0.48465I$
$b = -0.877439 - 0.744862I$		
$u = 1.311881 + 0.378892I$		
$a = -0.659626 + 0.338888I$	$-1.91067 + 0.79824I$	$-4.49024 + 0.48465I$
$b = -0.877439 + 0.744862I$		

III.  $I_3^u = \langle u^{13} + u^{12} + \dots - u + 1, a - 1, 94u^{12} - 167u^{11} + \dots + 1561b + 2486 \rangle$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -0.0602178u^{12} + 0.106983u^{11} + \dots + 1.43434u - 1.59257 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u \\ -0.167201u^{12} + 0.477899u^{11} + \dots + 2.65279u - 0.0602178 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0.0602178u^{12} - 0.106983u^{11} + \dots - 1.43434u + 2.59257 \\ -0.0602178u^{12} + 0.106983u^{11} + \dots + 1.43434u - 1.59257 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.0602178u^{12} - 0.106983u^{11} + \dots - 1.43434u + 2.59257 \\ -0.705317u^{12} + 0.199872u^{11} + \dots + 1.66176u - 1.75977 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -0.645099u^{12} + 0.0928892u^{11} + \dots + 0.227418u + 0.832799 \\ 0.476618u^{12} + 0.131967u^{11} + \dots + 0.392056u - 0.437540 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -0.0602178u^{12} + 0.106983u^{11} + \dots + 1.43434u - 1.59257 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -0.0602178u^{12} + 0.106983u^{11} + \dots + 1.43434u - 0.592569 \\ 1.21525u^{12} + 0.511211u^{11} + \dots + 0.596413u + 0.479821 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1.15503u^{12} + 0.618193u^{11} + \dots + 2.03075u - 0.112748 \\ -0.717489u^{12} + 0.295964u^{11} + \dots + 2.34529u + 0.0672646 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0.437540u^{12} + 0.914158u^{11} + \dots + 4.37604u - 0.0454837 \\ -0.260090u^{12} - 0.367713u^{11} + \dots - 2.76233u + 0.461883 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0.437540u^{12} + 0.914158u^{11} + \dots + 4.37604u - 0.0454837 \\ -0.260090u^{12} - 0.367713u^{11} + \dots - 2.76233u + 0.461883 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.59018 - 0.77503I$ $a = 1.00000$ $b = 1.23597 + 1.03056I$	$-10.3151 - 11.3952I$	$-4.67074 + 5.46785I$
$u = -1.59018 + 0.77503I$ $a = 1.00000$ $b = 1.23597 - 1.03056I$	$-10.3151 + 11.3952I$	$-4.67074 - 5.46785I$
$u = -1.342403 - 0.094615I$ $a = 1.00000$ $b = 1.13016 - 1.29050I$	$-9.55616 - 2.72200I$	$-5.53329 + 1.17863I$
$u = -1.342403 + 0.094615I$ $a = 1.00000$ $b = 1.13016 + 1.29050I$	$-9.55616 + 2.72200I$	$-5.53329 - 1.17863I$
$u = -1.12298$ $a = 1.00000$ $b = 0.594830$	$-1.85194$	$-5.42917$
$u = 0.019709 - 0.363243I$ $a = 1.00000$ $b = -0.405732 - 0.430962I$	$-0.133748 - 1.066328I$	$-2.25480 + 6.30909I$
$u = 0.019709 + 0.363243I$ $a = 1.00000$ $b = -0.405732 + 0.430962I$	$-0.133748 + 1.066328I$	$-2.25480 - 6.30909I$
$u = 0.196581 - 0.458453I$ $a = 1.00000$ $b = -0.134806 + 1.341745I$	$6.25855 + 1.58741I$	$3.86210 - 4.96482I$
$u = 0.196581 + 0.458453I$ $a = 1.00000$ $b = -0.134806 - 1.341745I$	$6.25855 - 1.58741I$	$3.86210 + 4.96482I$
$u = 1.156155 - 0.636682I$ $a = 1.00000$ $b = 0.679884 - 0.210052I$	$2.05464 + 3.32300I$	$2.35472 - 0.87537I$



Solution to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.156155 + 0.636682I$ $a = 1.00000$ $b = 0.679884 + 0.210052I$	$2.05464 - 3.32300I$	$2.35472 + 0.87537I$
$u = 1.62163 - 0.33100I$ $a = 1.00000$ $b = 1.19711 - 1.14120I$	$-14.5236 + 4.3483I$	$-7.04341 - 2.19507I$
$u = 1.62163 + 0.33100I$ $a = 1.00000$ $b = 1.19711 + 1.14120I$	$-14.5236 - 4.3483I$	$-7.04341 + 2.19507I$

#### IV. u-Polynomials

Crossings	u-Polynomials at each crossings
$c_1$	$(u^8 + 4u^6 + \dots - u + 1)(u^{12} + u^{11} + \dots - 28u + 19)$ $(u^{13} + 10u^{11} + \dots - 2u + 1)$
$c_2$	$(u^8 + 8u^7 + 26u^6 + 45u^5 + 49u^4 + 35u^3 + 17u^2 + 5u + 1)$ $(u^{12} + 15u^{11} + \dots + 1116u + 361)(u^{13} + 20u^{12} + \dots + 4u - 1)$
$c_3, c_6$	$(u^8 + 4u^6 + \dots + u + 1)(u^{12} + u^{11} + \dots - 28u + 19)$ $(u^{13} + 10u^{11} + \dots - 2u + 1)$
$c_4, c_5, c_9$	$(u^2 - u + 1)^6(u^8 + 5u^6 + 8u^4 - u^3 + 5u^2 - 2u + 1)$ $(u^{13} + 7u^{12} + \dots + 52u + 8)$
$c_7, c_{10}$	$(u^8 - u^7 + \dots - 2u + 1)(u^{12} + 3u^{11} + \dots + 36u + 7)$ $(u^{13} + u^{12} + \dots - u + 1)$
$c_8$	$(u^8 + u^7 + 4u^6 + 5u^5 + 3u^4 + 7u^3 + 7u^2 + 2u + 1)$ $(u^{12} + u^{11} + \dots + 72u + 61)(u^{13} - u^{12} + \dots - 25u + 61)$
$c_{11}$	$(u^3 - u^2 + 1)^4(u^8 - 3u^7 + 6u^6 - 7u^5 + 4u^4 + u^3 - 2u^2 + 1)$ $(u^{13} + 8u^{12} + \dots + 18u + 4)$

## V. Riley Polynomials

Crossings	Riley Polynomials at each crossings
$c_1, c_3, c_6$	$(y^8 + 8y^7 + 26y^6 + 45y^5 + 49y^4 + 35y^3 + 17y^2 + 5y + 1)$ $(y^{12} + 15y^{11} + \dots + 1116y + 361)(y^{13} + 20y^{12} + \dots + 4y - 1)$
$c_2$	$(y^8 - 12y^7 + 54y^6 - 3y^5 + 57y^4 + 43y^3 + 37y^2 + 9y + 1)$ $(y^{12} - 29y^{11} + \dots + 1501032y + 130321)$ $(y^{13} - 56y^{12} + \dots + 56y - 1)$
$c_4, c_5, c_9$	$(y^2 + y + 1)^6$ $(y^8 + 10y^7 + 41y^6 + 90y^5 + 116y^4 + 89y^3 + 37y^2 + 6y + 1)$ $(y^{13} + 11y^{12} + \dots - 176y - 64)$
$c_7, c_{10}$	$(y^8 - 3y^7 + 5y^6 - y^5 - 3y^4 - 4y^3 + 11y^2 - 6y + 1)$ $(y^{12} - 5y^{11} + \dots - 708y + 49)(y^{13} - 15y^{12} + \dots - 17y - 1)$
$c_8$	$(y^8 + 7y^7 + 12y^6 - y^5 - 7y^4 - 19y^3 + 27y^2 + 10y + 1)$ $(y^{12} + 23y^{11} + \dots - 3964y + 3721)$ $(y^{13} + 31y^{12} + \dots + 4407y - 3721)$
$c_{11}$	$(y^3 - y^2 + 2y - 1)^4(y^8 + 3y^7 + \dots - 4y + 1)$ $(y^{13} + 2y^{12} + \dots + 76y - 16)$