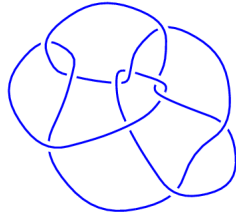
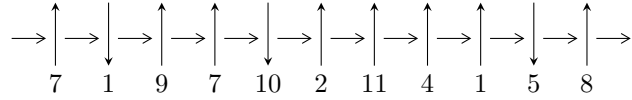


11n<sub>122</sub> (K11n<sub>122</sub>)

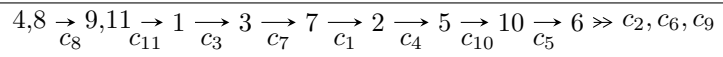


1

**Arc Sequences**



**Solving Sequence**



**Representation Ideals**

$$I = \bigcap_{i=1}^3 I_i^u$$

$$I_1^u = \langle b^6 + 4b^5 + 11b^4 + 10b^3 + 8b^2 + 2b + 1, -7b^5 - 25b^4 - 69b^3 - 54b^2 - 60b + 19u - 10, 12b^5 + 51b^4 + 140b^3 + 136b^2 + 92b + 19a + 28 \rangle$$

$$I_2^u = \langle u^3 + u - 1, -u^2 + b - u, -u^2 + a - 1 \rangle$$

$$I_3^u = \langle u^{16} - u^{15} + \dots + 14u + 5, 3169332u^{15} - 3873553u^{14} + \dots + 78266108b + 42681492, -68965897u^{15} + 83246472u^{14} + \dots + 782661080a - 2333564583 \rangle$$

There are 3 irreducible components with 25 representations.

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<sup>1</sup>The knot diagram image is adapter from “C. Livingston and A. H. Moore, KnotInfo: Table of Knot Invariants, <http://www.indiana.edu/~knotinfo>”

$$\mathbf{I. } I_1^u = \langle b^6 + 4b^5 + 11b^4 + 10b^3 + 8b^2 + 2b + 1, -7b^5 + 19u + \dots - 60b - 10, 12b^5 + 51b^4 + \dots + 19a + 28 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ 0.368421b^5 + 1.31579b^4 + \dots + 3.15789b + 0.526316 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.368421b^5 + 1.31579b^4 + \dots + 3.15789b + 0.526316 \\ 0.368421b^5 + 1.31579b^4 + \dots + 3.15789b + 0.526316 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.631579b^5 - 2.68421b^4 + \dots - 4.84211b - 1.47368 \\ b \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.631579b^5 - 2.68421b^4 + \dots - 4.84211b - 1.47368 \\ -0.631579b^5 - 2.68421b^4 + \dots - 3.84211b - 1.47368 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.473684b^5 + 2.26316b^4 + \dots + 5.63158b + 2.10526 \\ b \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.947368b^5 - 3.52632b^4 + \dots - 3.26316b + 0.789474 \\ -0.789474b^5 - 3.10526b^4 + \dots - 3.05263b - 0.842105 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -0.368421b^5 - 1.31579b^4 + \dots - 1.15789b + 1.47368 \\ -b^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} b \\ -0.210526b^5 - 0.894737b^4 + \dots + 1.05263b - 0.157895 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.526316b^5 - 1.73684b^4 + \dots - 1.36842b + 1.10526 \\ -0.157895b^5 - 0.421053b^4 + \dots - 0.210526b - 0.368421 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.526316b^5 - 1.73684b^4 + \dots - 1.36842b + 1.10526 \\ -0.157895b^5 - 0.421053b^4 + \dots - 0.210526b - 0.368421 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

| Solution to $I_1^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|---|---------------------------------------|----------------------|
| $u = 1.00000I$<br>$a = -0.215080 + 1.307141I$<br>$b = -1.52978 - 2.18458I$    | $3.02413 + 2.82812I$                  | $7.50976 - 2.97945I$ |
| $u = -1.00000I$<br>$a = -0.215080 - 1.307141I$<br>$b = -1.52978 + 2.18458I$   | $3.02413 - 2.82812I$                  | $7.50976 + 2.97945I$ |
| $u = -1.00000I$<br>$a = -0.569840$<br>$b = -0.430160 - 0.754878I$             | $-1.11345$                            | $0.980489$           |
| $u = 1.00000I$<br>$a = -0.569840$<br>$b = -0.430160 + 0.754878I$              | $-1.11345$                            | $0.980489$           |
| $u = -1.00000I$<br>$a = -0.215080 + 1.307141I$<br>$b = -0.040058 - 0.429702I$ | $3.02413 + 2.82812I$                  | $7.50976 - 2.97945I$ |
| $u = 1.00000I$<br>$a = -0.215080 - 1.307141I$<br>$b = -0.040058 + 0.429702I$  | $3.02413 - 2.82812I$                  | $7.50976 + 2.97945I$ |

$$\text{II. } I_2^u = \langle u^3 + u - 1, -u^2 + b - u, -u^2 + a - 1 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^2 + 1 \\ u^2 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^2 - 1 \\ -u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u + 1 \\ u^2 - u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u + 1 \\ 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

| Solution to $I_2^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|------------|
| $u = -0.341164 - 1.161541I$<br>$a = -0.232786 + 0.792552I$<br>$b = -1.57395 - 0.36899I$ | 1.64493                               | 6.00000    |
| $u = -0.341164 + 1.161541I$<br>$a = -0.232786 - 0.792552I$<br>$b = -1.57395 + 0.36899I$ | 1.64493                               | 6.00000    |
| $u = 0.682328$<br>$a = 1.46557$<br>$b = 1.14790$  | 1.64493                               | 6.00000    |

III.

$$I_3^u = \langle u^{16} - u^{15} + \dots + 14u + 5, 3.17 \times 10^6 u^{15} - 3.87 \times 10^6 u^{14} + \dots + 7.83 \times 10^7 b + 4.27 \times 10^7, -6.90 \times 10^7 u^{15} + 8.32 \times 10^7 u^{14} + \dots + 7.83 \times 10^8 a - 2.33 \times 10^9 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.0881172u^{15} - 0.106363u^{14} + \dots - 1.75694u + 2.98158 \\ -0.0404943u^{15} + 0.0494921u^{14} + \dots - 0.475198u - 0.545338 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0.0881172u^{15} - 0.106363u^{14} + \dots - 1.75694u + 2.98158 \\ -0.0666612u^{15} + 0.0867678u^{14} + \dots - 0.290059u - 0.636569 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.146114u^{15} - 0.176168u^{14} + \dots - 3.58050u + 2.67329 \\ -0.142245u^{15} + 0.217246u^{14} + \dots - 0.241323u - 0.898131 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.295676u^{15} - 0.375222u^{14} + \dots + 2.18214u + 4.27038 \\ 0.0731003u^{15} - 0.121686u^{14} + \dots - 0.170342u + 1.48163 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0.539146u^{15} - 0.806823u^{14} + \dots + 5.67472u + 7.01358 \\ 0.318586u^{15} - 0.390881u^{14} + \dots + 0.0487607u + 4.11236 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -0.253272u^{15} + 0.339269u^{14} + \dots + 3.64900u - 3.72169 \\ 0.0631942u^{15} - 0.115526u^{14} + \dots + 1.97305u + 0.421239 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0.136312u^{15} - 0.268499u^{14} + \dots + 3.56108u + 1.69481 \\ 0.203960u^{15} - 0.180133u^{14} + \dots + 0.369678u + 1.93594 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0.136312u^{15} - 0.268499u^{14} + \dots + 3.56108u + 1.69481 \\ 0.203960u^{15} - 0.180133u^{14} + \dots + 0.369678u + 1.93594 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

| Solution to $I_3^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape              |
|---|---------------------------------------|-------------------------|
| $u = -0.501898 - 1.170947I$<br>$a = -0.503764 - 0.361443I$<br>$b = -0.0767367 + 0.0423889I$ | $-4.05827 + 0.49300I$                 | $-0.617664 - 0.214534I$ |
| $u = -0.501898 + 1.170947I$<br>$a = -0.503764 + 0.361443I$<br>$b = -0.0767367 - 0.0423889I$ | $-4.05827 - 0.49300I$                 | $-0.617664 + 0.214534I$ |
| $u = -0.353855 - 0.072083I$<br>$a = 3.59505 - 0.29198I$<br>$b = 1.07980 + 1.11316I$         | $5.01976 + 2.82849I$                  | $13.14002 - 4.04275I$   |
| $u = -0.353855 + 0.072083I$<br>$a = 3.59505 + 0.29198I$<br>$b = 1.07980 - 1.11316I$         | $5.01976 - 2.82849I$                  | $13.14002 + 4.04275I$   |
| $u = -0.21307 - 1.91064I$<br>$a = 0.524290 + 0.017898I$<br>$b = 0.308221 + 0.434571I$       | $-15.2325 + 4.4644I$                  | $1.08918 - 2.21387I$    |
| $u = -0.21307 + 1.91064I$<br>$a = 0.524290 - 0.017898I$<br>$b = 0.308221 - 0.434571I$       | $-15.2325 - 4.4644I$                  | $1.08918 + 2.21387I$    |
| $u = 0.05915 - 1.92604I$<br>$a = 0.262645 - 0.667097I$<br>$b = 0.57327 + 1.88623I$          | $-11.56799 + 1.02407I$                | $3.53875 - 0.89724I$    |
| $u = 0.05915 + 1.92604I$<br>$a = 0.262645 + 0.667097I$<br>$b = 0.57327 - 1.88623I$          | $-11.56799 - 1.02407I$                | $3.53875 + 0.89724I$    |
| $u = 0.191592 - 0.407882I$<br>$a = 0.865782 + 0.145223I$<br>$b = -0.139705 - 0.543596I$     | $0.504151 - 0.997325I$                | $7.27390 + 6.88407I$    |
| $u = 0.191592 + 0.407882I$<br>$a = 0.865782 - 0.145223I$<br>$b = -0.139705 + 0.543596I$     | $0.504151 + 0.997325I$                | $7.27390 - 6.88407I$    |

| Solution to $I_3^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|--|---------------------------------------|----------------------|
| $u = 0.219282 - 1.218529I$<br>$a = -0.005279 + 1.129211I$<br>$b = -0.23172 - 2.01108I$ | $0.90149 + 3.13168I$                  | $3.23299 - 2.68195I$ |
| $u = 0.219282 + 1.218529I$<br>$a = -0.005279 - 1.129211I$<br>$b = -0.23172 + 2.01108I$ | $0.90149 - 3.13168I$                  | $3.23299 + 2.68195I$ |
| $u = 0.31759 - 1.82628I$<br>$a = 0.377606 + 0.685129I$<br>$b = 1.93408 - 2.15013I$     | $-10.6907 - 9.7305I$                  | $4.40505 + 4.74516I$ |
| $u = 0.31759 + 1.82628I$<br>$a = 0.377606 - 0.685129I$<br>$b = 1.93408 + 2.15013I$     | $-10.6907 + 9.7305I$                  | $4.40505 - 4.74516I$ |
| $u = 0.781211 - 0.999484I$<br>$a = -0.816330 - 0.523237I$<br>$b = -1.94720 + 0.86621I$ | $-1.06445 - 4.80370I$                 | $3.93778 + 5.08204I$ |
| $u = 0.781211 + 0.999484I$<br>$a = -0.816330 + 0.523237I$<br>$b = -1.94720 - 0.86621I$ | $-1.06445 + 4.80370I$                 | $3.93778 - 5.08204I$ |



#### IV. u-Polynomials

| Crossings     | u-Polynomials at each crossings  |
|---------------|--|
| $c_1, c_6$    | $u^3(u^6 + u^4 + 2u^2 + 1)(u^{16} + 3u^{15} + \dots - 163u + 62)$  |
| $c_2$         | $u^3(1 + 2u + u^2 + u^3)^2(u^{16} + 29u^{15} + \dots + 16707u + 3844)$                                       |
| $c_3, c_8$    | $(u^2 + 1)^3(u^3 + u + 1)(u^{16} + u^{15} + \dots - 14u + 5)$  |
| $c_4$         | $(u^3 - 2u^2 + u + 1)(u^6 + 4u^5 + 11u^4 + 10u^3 + 8u^2 + 2u + 1)$<br>$(u^{16} + 5u^{15} + \dots - 6u + 67)$ |
| $c_5, c_{10}$ | $(u^2 + 1)^3(u^3 + u + 1)(u^{16} + u^{15} + \dots - 8u + 5)$   |
| $c_7, c_{11}$ | $(u + 1)^3(u^6 - 3u^4 + 2u^2 + 1)(u^{16} - 2u^{15} + \dots + u + 2)$   |
| $c_9$         | $(u^3 + u + 1)(u^6 - 2u^5 - u^4 + 8u^3 + 12u^2 + 6u + 1)$<br>$(u^{16} + u^{15} + \dots + 2824u + 1117)$      |

### V. Riley Polynomials

| Crossings     | Riley Polynomials at each crossings  |
|---------------|--|
| $c_1, c_6$    | $y^3(1 + 2y + y^2 + y^3)^2(y^{16} + 29y^{15} + \dots + 16707y + 3844)$   |
| $c_2$         | $y^3(y^3 + 3y^2 + 2y - 1)^2$<br>$(y^{16} - 75y^{15} + \dots + 939185823y + 14776336)$                                      |
| $c_3, c_8$    | $(y + 1)^6(y^3 + 2y^2 + y - 1)(y^{16} + 27y^{15} + \dots - 96y + 25)$  |
| $c_4$         | $(y^3 - 2y^2 + 5y - 1)(y^6 + 6y^5 + 57y^4 + 62y^3 + 46y^2 + 12y + 1)$<br>$(y^{16} + 19y^{15} + \dots + 15374y + 4489)$     |
| $c_5, c_{10}$ | $(y + 1)^6(y^3 + 2y^2 + y - 1)(y^{16} - y^{15} + \dots - 64y + 25)$  |
| $c_7, c_{11}$ | $(y - 1)^3(1 + 2y - 3y^2 + y^3)^2(y^{16} - 12y^{15} + \dots + 19y + 4)$  |
| $c_9$         | $(y^3 + 2y^2 + y - 1)(y^6 - 6y^5 + 57y^4 - 62y^3 + 46y^2 - 12y + 1)$<br>$(y^{16} + 51y^{15} + \dots - 7186374y + 1247689)$ |