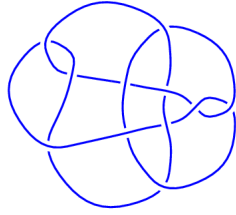
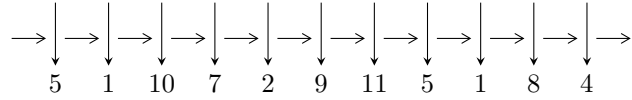


11n₁₂₆ (K11n₁₂₆)

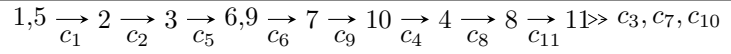


1

Arc Sequences



Solving Sequence



Representation Ideals

$$I = \bigcap_{i=1}^8 I_i^u$$

$$I_1^u = \langle u^2 + 2u + 2, b + u + 1, 2a - u - 2 \rangle$$

$$I_2^u = \langle u^4 + 3u^3 + 2u^2 - 1, a + 1, u^2 + b + u \rangle$$

$$I_3^u = \langle u^5 - 4u^4 + 3u^3 + 2u^2 + u - 1, a - 1, -u^2 + b + u \rangle$$

$$I_4^u = \langle u^6 - 4u^5 + u^4 + 9u^3 - 16u + 10, -8u^5 + 23u^4 + 14u^3 - 33u^2 + 31b - 41u + 47, \\ 27u^5 - 128u^4 + 7u^3 + 433u^2 + 310a + 150u - 612 \rangle$$

$$I_5^u = \langle u^6 + 3u^5 - 3u^3 + 2u^2 + 1, a - 1, -u^5 - 4u^4 - 2u^3 + 3u^2 + 2b - u - 1 \rangle$$

$$I_6^u = \langle b^2 + 1, a + 1, u - 1 \rangle$$

$$I_7^u = \langle b^2 + 1, u - 1, -b + a - 1 \rangle$$

$$I_8^u = \langle u^6 + 3u^5 - 3u^3 + 2u^2 + 1, u^5 + 2u^4 - 2u^3 - u^2 + 2b + 3u - 1, -u^5 - 2u^4 + 4u^3 + 5u^2 + 2a - 7u + 1 \rangle$$

There are 8 irreducible components with 33 representations.

¹The knot diagram image is adapter from “C. Livingston and A. H. Moore, KnotInfo: Table of Knot Invariants, <http://www.indiana.edu/~knotinfo>”

$$\mathbf{I. } I_1^u = \langle u^2 + 2u + 2, b + u + 1, 2a - u - 2 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -2u - 2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 2u + 3 \\ -2u - 2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ -u - 4 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} \frac{1}{2}u + 1 \\ -u - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -\frac{1}{2}u \\ -u - 3 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} \frac{3}{2}u + 2 \\ -u - 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} \frac{1}{2}u + 1 \\ -u - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} \frac{1}{2}u + 1 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} \frac{1}{2}u + 1 \\ 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} \frac{1}{2}u + 1 \\ 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.00000 - 1.00000I$	1.64493	-8.00000
$a = 0.500000 - 0.500000I$		
$b = 1.00000I$		
$u = -1.00000 + 1.00000I$	1.64493	-8.00000
$a = 0.500000 + 0.500000I$		
$b = -1.00000I$		

$$\text{II. } I_2^u = \langle u^4 + 3u^3 + 2u^2 - 1, a + 1, u^2 + b + u \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -1 \\ -u^2 - u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^2 - 2u \\ u^2 + u - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^2 + u - 1 \\ -u^2 - u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^3 - 2u^2 + u + 1 \\ u^3 + 2u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -1 \\ -u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^3 + 3u^2 + u - 1 \\ -u^3 - 3u^2 - u + 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^3 + 3u^2 + u - 1 \\ -u^3 - 3u^2 - u + 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -2.17872$ $a = -1.00000$ $b = -2.56811$	-13.8089	-12.1771
$u = -0.667076 - 0.670769I$ $a = -1.00000$ $b = 0.672017 - 0.224139I$	$3.04056 - 6.31855I$	$-7.20042 + 6.94067I$
$u = -0.667076 + 0.670769I$ $a = -1.00000$ $b = 0.672017 + 0.224139I$	$3.04056 + 6.31855I$	$-7.20042 - 6.94067I$
$u = 0.512876$ $a = -1.00000$ $b = -0.775919$	-2.14179	-18.4220

$$\text{III. } I_3^u = \langle u^5 - 4u^4 + 3u^3 + 2u^2 + u - 1, a - 1, -u^2 + b + u \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ u^2 - u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^2 - 2u \\ u^4 - 3u^3 + u^2 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^2 + u + 1 \\ u^2 - u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^3 - 2u^2 - u + 1 \\ -u^3 + 2u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^3 - 3u^2 + u + 1 \\ -u^4 + 2u^3 + u^2 - u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^3 - 3u^2 + u + 1 \\ -u^4 + 2u^3 + u^2 - u \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.456518 - 0.478939I$ $a = 1.00000$ $b = 0.435545 + 0.916228I$	$4.11394 - 0.50358I$	$-4.17139 + 2.42983I$
$u = -0.456518 + 0.478939I$ $a = 1.00000$ $b = 0.435545 - 0.916228I$	$4.11394 + 0.50358I$	$-4.17139 - 2.42983I$
$u = 0.455088$ $a = 1.00000$ $b = -0.247983$	-0.742760	-13.4344
$u = 2.22897 - 0.22563I$ $a = 1.00000$ $b = 2.68845 - 0.78020I$	$-11.1448 + 10.7639I$	$-11.61144 - 5.00628I$
$u = 2.22897 + 0.22563I$ $a = 1.00000$ $b = 2.68845 + 0.78020I$	$-11.1448 - 10.7639I$	$-11.61144 + 5.00628I$

$$\text{IV. } I_4^u = \langle u^6 - 4u^5 + u^4 + 9u^3 - 16u + 10, -8u^5 + 23u^4 + \dots + 31b + 47, 27u^5 - 128u^4 + \dots + 310a - 612 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -0.0870968u^5 + 0.412903u^4 + \dots - 0.483871u + 1.97419 \\ 0.258065u^5 - 0.741935u^4 + \dots + 1.32258u - 1.51613 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.164516u^5 + 0.335484u^4 + \dots - 1.58065u + 0.729032 \\ -0.290323u^5 + 0.709677u^4 + \dots - 0.612903u + 1.58065 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -0.345161u^5 + 1.15484u^4 + \dots - 1.80645u + 3.49032 \\ 0.258065u^5 - 0.741935u^4 + \dots + 1.32258u - 1.51613 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.0935484u^5 - 0.406452u^4 + \dots + 0.741935u - 0.787097 \\ 0.322581u^5 - 0.677419u^4 + \dots + 1.90323u - 1.64516 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -0.0870968u^5 + 0.412903u^4 + \dots - 0.483871u + 1.97419 \\ -0.0645161u^5 - 0.0645161u^4 + \dots - 0.580645u - 0.870968 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -\frac{1}{10}u^5 + \frac{2}{5}u^4 + \dots - \frac{9}{10}u^2 + \frac{8}{5} \\ 0.0322581u^5 + 0.0322581u^4 + \dots - 0.709677u + 0.935484 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -\frac{1}{10}u^5 + \frac{2}{5}u^4 + \dots - \frac{9}{10}u^2 + \frac{8}{5} \\ 0.0322581u^5 + 0.0322581u^4 + \dots - 0.709677u + 0.935484 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_4^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.221244 - 0.712792I$		
$a = -0.093681 - 0.373158I$	$2.26485 - 4.47692I$	$-9.60193 + 3.00061I$
$b = 0.709117 - 1.052541I$		
$u = -1.221244 + 0.712792I$		
$a = -0.093681 + 0.373158I$	$2.26485 + 4.47692I$	$-9.60193 - 3.00061I$
$b = 0.709117 + 1.052541I$		
$u = 0.912842 - 0.311096I$		
$a = 0.588546 + 0.687760I$	$-0.389538 + 0.233200I$	$-13.01274 - 1.15455I$
$b = 0.072877 - 0.272459I$		
$u = 0.912842 + 0.311096I$		
$a = 0.588546 - 0.687760I$	$-0.389538 - 0.233200I$	$-13.01274 + 1.15455I$
$b = 0.072877 + 0.272459I$		
$u = 2.30840 - 0.22043I$		
$a = -0.894865 - 0.153901I$	$-13.38985 - 2.37783I$	$-11.38532 + 2.96944I$
$b = -2.78199 + 0.25607I$		
$u = 2.30840 + 0.22043I$		
$a = -0.894865 + 0.153901I$	$-13.38985 + 2.37783I$	$-11.38532 - 2.96944I$
$b = -2.78199 - 0.25607I$		

V.

$$I_5^u = \langle u^6 + 3u^5 - 3u^3 + 2u^2 + 1, a - 1, -u^5 - 4u^4 - 2u^3 + 3u^2 + 2b - u - 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ \frac{1}{2}u^5 + 2u^4 + \cdots + \frac{1}{2}u + \frac{1}{2} \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -\frac{1}{2}u^5 - u^4 + \cdots - \frac{5}{2}u + \frac{1}{2} \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -\frac{1}{2}u^5 - 2u^4 + \cdots - \frac{1}{2}u + \frac{1}{2} \\ \frac{1}{2}u^5 + 2u^4 + \cdots + \frac{1}{2}u + \frac{1}{2} \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^4 + 2u^3 - u^2 - u + 1 \\ \frac{1}{2}u^5 + u^4 + \cdots + \frac{3}{2}u + \frac{1}{2} \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ \frac{1}{2}u^5 + 2u^4 + \cdots + \frac{1}{2}u + \frac{1}{2} \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^5 - 3u^4 + 3u^2 - 2u \\ u^3 + u^2 - 2u + 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^5 - 3u^4 + 3u^2 - 2u \\ u^3 + u^2 - 2u + 1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_5^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -2.09963 - 0.15801I$ $a = 1.00000$ $b = 2.07508 + 0.88397I$	$-13.38985 - 2.37783I$	$-11.38532 + 2.96944I$
$u = -2.09963 + 0.15801I$ $a = 1.00000$ $b = 2.07508 - 0.88397I$	$-13.38985 + 2.37783I$	$-11.38532 - 2.96944I$
$u = -0.151576 - 0.522493I$ $a = 1.00000$ $b = 0.971221 - 0.554396I$	$2.26485 + 4.47692I$	$-9.60193 - 3.00061I$
$u = -0.151576 + 0.522493I$ $a = 1.00000$ $b = 0.971221 + 0.554396I$	$2.26485 - 4.47692I$	$-9.60193 + 3.00061I$
$u = 0.751209 - 0.444722I$ $a = 1.00000$ $b = -0.546305 - 0.979253I$	$-0.389538 - 0.233200I$	$-13.01274 + 1.15455I$
$u = 0.751209 + 0.444722I$ $a = 1.00000$ $b = -0.546305 + 0.979253I$	$-0.389538 + 0.233200I$	$-13.01274 - 1.15455I$

$$\text{VI. } I_6^u = \langle b^2 + 1, a + 1, u - 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -1 \\ b \end{pmatrix}$$

$$a_7 = \begin{pmatrix} b - 1 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -b - 1 \\ b \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -2b \\ b \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -1 \\ b + 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_6^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$ $a = -1.00000$ $b = -1.00000I$	1.64493	-8.00000
$u = 1.00000$ $a = -1.00000$ $b = 1.00000I$	1.64493	-8.00000

$$\text{VII. } I_7^u = \langle b^2 + 1, u - 1, -b + a - 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} b+1 \\ b \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -b \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ b \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -1 \\ -b+1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} b+1 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -b+2 \\ 2b \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -b+2 \\ 2b \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_7^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$		
$a = 1.00000 - 1.00000I$	1.64493	-8.00000
$b = -1.00000I$		
$u = 1.00000$		
$a = 1.00000 + 1.00000I$	1.64493	-8.00000
$b = 1.00000I$		

$$\text{VIII. } I_8^u = \langle u^6 + 3u^5 - 3u^3 + 2u^2 + 1, u^5 + 2u^4 - 2u^3 - u^2 + 2b + 3u - 1, -u^5 - 2u^4 + 4u^3 + 5u^2 + 2a - 7u + 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} \frac{1}{2}u^5 + u^4 + \cdots + \frac{7}{2}u - \frac{1}{2} \\ -\frac{1}{2}u^5 - u^4 + \cdots - \frac{3}{2}u + \frac{1}{2} \end{pmatrix}$$

$$a_7 = \begin{pmatrix} \frac{1}{2}u^5 + u^4 + \cdots + \frac{5}{2}u - \frac{3}{2} \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^5 + 2u^4 - 3u^3 - 3u^2 + 5u - 1 \\ -\frac{1}{2}u^5 - u^4 + \cdots - \frac{3}{2}u + \frac{1}{2} \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^5 + 3u^4 - 4u^2 + u + 2 \\ -\frac{1}{2}u^5 - u^4 + \cdots - \frac{1}{2}u - \frac{1}{2} \end{pmatrix}$$

$$a_8 = \begin{pmatrix} \frac{1}{2}u^5 + u^4 + \cdots + \frac{7}{2}u - \frac{1}{2} \\ -u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} \frac{3}{2}u^5 + 4u^4 + \cdots + \frac{7}{2}u + \frac{3}{2} \\ -u^5 - 2u^4 + u^3 + u^2 - u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} \frac{3}{2}u^5 + 4u^4 + \cdots + \frac{7}{2}u + \frac{3}{2} \\ -u^5 - 2u^4 + u^3 + u^2 - u \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_8^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -2.09963 - 0.15801I$		
$a = -1.085384 + 0.186667I$	$-13.38985 - 2.37783I$	$-11.38532 + 2.96944I$
$b = -2.78199 + 0.25607I$		
$u = -2.09963 + 0.15801I$		
$a = -1.085384 - 0.186667I$	$-13.38985 + 2.37783I$	$-11.38532 - 2.96944I$
$b = -2.78199 - 0.25607I$		
$u = -0.151576 - 0.522493I$		
$a = -0.63288 - 2.52094I$	$2.26485 + 4.47692I$	$-9.60193 - 3.00061I$
$b = 0.709117 + 1.052541I$		
$u = -0.151576 + 0.522493I$		
$a = -0.63288 + 2.52094I$	$2.26485 - 4.47692I$	$-9.60193 + 3.00061I$
$b = 0.709117 - 1.052541I$		
$u = 0.751209 - 0.444722I$		
$a = 0.718265 + 0.839346I$	$-0.389538 - 0.233200I$	$-13.01274 + 1.15455I$
$b = 0.072877 + 0.272459I$		
$u = 0.751209 + 0.444722I$		
$a = 0.718265 - 0.839346I$	$-0.389538 + 0.233200I$	$-13.01274 - 1.15455I$
$b = 0.072877 - 0.272459I$		

IX. u-Polynomials

Crossings	u-Polynomials at each crossings
c_1	$(u-1)^4(u^2+2u+2)(u^4+3u^3+2u^2-1)(u^5+4u^4+\dots+u+1)$ $(u^6-3u^5+3u^3+2u^2+1)^2(u^6+4u^5+u^4-9u^3+16u+10)$
c_2	$(u+1)^4(u^2+4)(u^4+5u^3+2u^2+4u+1)$ $(u^5+10u^4+27u^3+6u^2+5u+1)$ $(u^6+9u^5+22u^4+7u^3+4u^2-4u+1)^2$ $(u^6+14u^5+73u^4+189u^3+308u^2+256u+100)$
c_3, c_5, c_8	$(u+1)^4(u^2-2u+2)(u^4-3u^3+2u^2-1)(u^5+4u^4+\dots+u+1)$ $(u^6-3u^5+3u^3+2u^2+1)^2(u^6+4u^5+u^4-9u^3+16u+10)$
c_4, c_7, c_{11}	$(u^2+1)^2(u^2-2u+2)(u^4-u^3+u^2+u-1)$ $(u^5+2u^4+4u^3+2u^2+2u-1)(u^6-u^5+2u^4-u^3+2u^2-2u+1)^2$ $(u^6+4u^5+7u^4+7u^3+6u^2+4u+2)$
c_6, c_9	$(u^2+1)^3(u^4-2u^3-2u^2+u+1)(u^5+6u^4+12u^3+9u^2+5u-2)$ $(u^6-4u^5+u^4+2u^3+13u^2+2u+1)^2$ $(u^6+5u^5+9u^4+7u^3+8u^2+12u+8)$
c_{10}	$(u^2+1)^2(u^2+2u+2)(u^4+u^3+u^2-u-1)$ $(u^5+2u^4+4u^3+2u^2+2u-1)(u^6-u^5+2u^4-u^3+2u^2-2u+1)^2$ $(u^6+4u^5+7u^4+7u^3+6u^2+4u+2)$

X. Riley Polynomials

Crossings	Riley Polynomials at each crossings
c_1, c_3, c_5 c_8	$(y - 1)^4(y^2 + 4)(y^4 - 5y^3 + 2y^2 - 4y + 1)$ $(y^5 - 10y^4 + 27y^3 - 6y^2 + 5y - 1)$ $(y^6 - 14y^5 + 73y^4 - 189y^3 + 308y^2 - 256y + 100)$ $(y^6 - 9y^5 + 22y^4 - 7y^3 + 4y^2 + 4y + 1)^2$
c_2	$(y - 1)^4(y + 4)^2(y^4 - 21y^3 - 34y^2 - 12y + 1)$ $(y^5 - 46y^4 + 619y^3 + 214y^2 + 13y - 1)$ $(y^6 - 50y^5 + 653y^4 + 2279y^3 + 12696y^2 - 3936y + 10000)$ $(y^6 - 37y^5 + 366y^4 + 201y^3 + 116y^2 - 8y + 1)^2$
c_4, c_7, c_{10} c_{11}	$(y + 1)^4(y^2 + 4)(y^4 + y^3 + \dots - 3y + 1)(y^5 + 4y^4 + \dots + 8y - 1)$ $(y^6 - 2y^5 + \dots + 8y + 4)(1 + 4y^2 + 5y^3 + 6y^4 + 3y^5 + y^6)^2$
c_6, c_9	$(y + 1)^6(y^4 - 8y^3 + \dots - 5y + 1)(y^5 - 12y^4 + \dots + 61y - 4)$ $(y^6 - 14y^5 + 43y^4 + 40y^3 + 163y^2 + 22y + 1)^2$ $(y^6 - 7y^5 + 27y^4 - 9y^3 + 40y^2 - 16y + 64)$