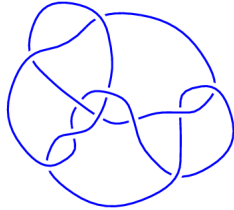
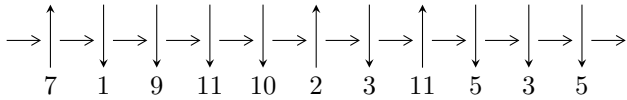


11n₁₃₅ (K11n₁₃₅)

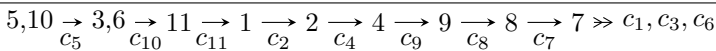


1

Arc Sequences



Solving Sequence



Representation Ideals

$$I = \bigcap_{i=1}^2 I_i^u$$

$$\begin{aligned} I_1^u &= \langle u^8 - 6u^7 + 11u^6 - u^5 - 14u^4 + 4u^3 + 11u^2 - 6u + 1, -u^7 + 6u^6 - 10u^5 - 2u^4 + 14u^3 + u^2 + b - 11u + 3, \\ &\quad -3u^7 + 17u^6 - 27u^5 - 7u^4 + 40u^3 + 2u^2 + a - 32u + 7 \rangle \\ I_2^u &= \langle u^{10} + 3u^9 - 4u^8 - 16u^7 + 6u^6 + 37u^5 + 11u^4 - 21u^3 - 16u^2 - 5u - 1, \\ &\quad 7u^9 + 14u^8 - 40u^7 - 71u^6 + 100u^5 + 158u^4 - 51u^3 - 95u^2 + b - 32u - 9, \\ &\quad 9u^9 + 20u^8 - 50u^7 - 104u^6 + 125u^5 + 233u^4 - 59u^3 - 138u^2 + a - 49u - 13 \rangle \end{aligned}$$

There are 2 irreducible components with 18 representations.

¹The knot diagram image is adapter from “C. Livingston and A. H. Moore, KnotInfo: Table of Knot Invariants, <http://www.indiana.edu/~knotinfo>”

I.

$$I_1^u = \langle u^8 - 6u^7 + \dots - 6u + 1, -u^7 + 6u^6 + \dots + b + 3, -3u^7 + 17u^6 + \dots + a + 7 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_5 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 3u^7 - 17u^6 + 27u^5 + 7u^4 - 40u^3 - 2u^2 + 32u - 7 \\ u^7 - 6u^6 + 10u^5 + 2u^4 - 14u^3 - u^2 + 11u - 3 \end{pmatrix} \\ a_3 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_6 &= \begin{pmatrix} u^6 - 5u^5 + 6u^4 + 5u^3 - 9u^2 - 5u + 6 \\ u^7 - 5u^6 + 6u^5 + 5u^4 - 9u^3 - 5u^2 + 7u \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 2u^7 - 11u^6 + 17u^5 + 5u^4 - 26u^3 - u^2 + 21u - 4 \\ u^7 - 6u^6 + 10u^5 + 2u^4 - 14u^3 - u^2 + 11u - 3 \end{pmatrix} \\ a_1 &= \begin{pmatrix} 2u^7 - 11u^6 + 17u^5 + 5u^4 - 26u^3 - u^2 + 21u - 4 \\ 2u^7 - 10u^6 + 13u^5 + 7u^4 - 19u^3 - 4u^2 + 15u - 4 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -u^7 + 6u^6 - 11u^5 + u^4 + 14u^3 - 4u^2 - 12u + 8 \\ u^7 - 5u^6 + 6u^5 + 5u^4 - 10u^3 - 4u^2 + 8u \end{pmatrix} \\ a_4 &= \begin{pmatrix} u^7 - 6u^6 + 11u^5 - u^4 - 14u^3 + 4u^2 + 11u - 5 \\ u - 1 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 3u^7 - 17u^6 + 27u^5 + 7u^4 - 40u^3 - 2u^2 + 32u - 7 \\ u^7 - 5u^6 + 7u^5 + 2u^4 - 9u^3 - u^2 + 8u - 2 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -2u^7 + 11u^6 - 17u^5 - 5u^4 + 26u^3 + u^2 - 21u + 4 \\ 2u^6 - 8u^5 + 5u^4 + 12u^3 - 7u^2 - 11u + 4 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -2u^7 + 13u^6 - 25u^5 + 38u^3 - 6u^2 - 32u + 8 \\ 2u^6 - 8u^5 + 5u^4 + 12u^3 - 7u^2 - 11u + 4 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -2u^7 + 13u^6 - 25u^5 + 38u^3 - 6u^2 - 32u + 8 \\ 2u^6 - 8u^5 + 5u^4 + 12u^3 - 7u^2 - 11u + 4 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =unknown

(iv) Complex Volumes and Cusp Shapes

| Solution to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|-----------------------|
| $u = -0.880687 - 0.411861I$ | $2.76707 + 1.04226I$ | $-7.14108 + 0.01449I$ |
| $a = 0.384446 + 0.633801I$ | | |
| $b = -0.077538 - 0.716519I$ | | |
| $u = -0.880687 + 0.411861I$ | $2.76707 - 1.04226I$ | $-7.14108 - 0.01449I$ |
| $a = 0.384446 - 0.633801I$ | | |
| $b = -0.077538 + 0.716519I$ | | |
| $u = 0.272591 - 0.146873I$ | $6.36547 - 2.93267I$ | $4.14670 + 1.68828I$ |
| $a = 1.44122 - 3.46089I$ | | |
| $b = -0.115448 - 1.155084I$ | | |
| $u = 0.272591 + 0.146873I$ | $6.36547 + 2.93267I$ | $4.14670 - 1.68828I$ |
| $a = 1.44122 + 3.46089I$ | | |
| $b = -0.115448 + 1.155084I$ | | |
| $u = 1.60890 - 0.18698I$ | $-3.52853 - 0.48963I$ | $-9.23600 - 1.05814I$ |
| $a = -0.746630 - 0.202358I$ | | |
| $b = -1.239094 - 0.185966I$ | | |
| $u = 1.60890 + 0.18698I$ | $-3.52853 + 0.48963I$ | $-9.23600 + 1.05814I$ |
| $a = -0.746630 + 0.202358I$ | | |
| $b = -1.239094 + 0.185966I$ | | |
| $u = 1.99919 - 0.45726I$ | $-5.60402 + 3.77609I$ | $-14.7696 - 2.3802I$ |
| $a = 0.420965 + 0.197898I$ | | |
| $b = 0.932081 + 0.203144I$ | | |
| $u = 1.99919 + 0.45726I$ | $-5.60402 - 3.77609I$ | $-14.7696 + 2.3802I$ |
| $a = 0.420965 - 0.197898I$ | | |
| $b = 0.932081 - 0.203144I$ | | |

II.

$$I_2^u = \langle u^{10} + 3u^9 + \cdots - 5u - 1, 7u^9 + 14u^8 + \cdots + b - 9, 9u^9 + 20u^8 + \cdots + a - 13 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_5 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -9u^9 - 20u^8 + \cdots + 49u + 13 \\ -7u^9 - 14u^8 + \cdots + 32u + 9 \end{pmatrix} \\ a_3 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -2u^9 - 3u^8 + 12u^7 + 14u^6 - 30u^5 - 30u^4 + 17u^3 + 18u^2 + 7u + 1 \\ -3u^9 - 4u^8 + 18u^7 + 18u^6 - 44u^5 - 39u^4 + 24u^3 + 25u^2 + 10u + 2 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -2u^9 - 6u^8 + 10u^7 + 33u^6 - 25u^5 - 75u^4 + 8u^3 + 43u^2 + 17u + 4 \\ -7u^9 - 14u^8 + \cdots + 32u + 9 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -2u^9 - 6u^8 + 10u^7 + 33u^6 - 25u^5 - 75u^4 + 8u^3 + 43u^2 + 17u + 4 \\ -5u^9 - 13u^8 + \cdots + 30u + 9 \end{pmatrix} \\ a_2 &= \begin{pmatrix} u^9 + u^8 - 6u^7 - 4u^6 + 14u^5 + 9u^4 - 7u^3 - 7u^2 - 3u + 1 \\ 3u^9 + 4u^8 - 18u^7 - 18u^6 + 44u^5 + 39u^4 - 25u^3 - 24u^2 - 9u - 2 \end{pmatrix} \\ a_4 &= \begin{pmatrix} u^9 + u^8 - 6u^7 - 4u^6 + 14u^5 + 9u^4 - 7u^3 - 7u^2 - 2u \\ -2u^9 - 2u^8 + 12u^7 + 8u^6 - 28u^5 - 18u^4 + 14u^3 + 14u^2 + 5u + 1 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -9u^9 - 20u^8 + \cdots + 49u + 13 \\ -2u^8 - u^7 + 13u^6 + u^5 - 30u^4 - u^3 + 15u^2 + 6u + 2 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -2u^9 - 6u^8 + 10u^7 + 33u^6 - 25u^5 - 75u^4 + 8u^3 + 43u^2 + 17u + 4 \\ 6u^9 + 17u^8 + \cdots - 37u - 11 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 4u^9 + 11u^8 - 22u^7 - 60u^6 + 60u^5 + 134u^4 - 38u^3 - 75u^2 - 20u - 7 \\ 6u^9 + 17u^8 + \cdots - 37u - 11 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 4u^9 + 11u^8 - 22u^7 - 60u^6 + 60u^5 + 134u^4 - 38u^3 - 75u^2 - 20u - 7 \\ 6u^9 + 17u^8 + \cdots - 37u - 11 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

| Solution to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = -1.91166 - 0.13941I$ $a = -1.71182 - 0.70510I$ $b = -3.17411 - 1.58657I$ | $-17.7391 - 8.0399I$ | $-7.30663 + 2.83159I$ |
| $u = -1.91166 + 0.13941I$ $a = -1.71182 + 0.70510I$ $b = -3.17411 + 1.58657I$ | $-17.7391 + 8.0399I$ | $-7.30663 - 2.83159I$ |
| $u = -1.85920$ $a = 2.10858$ $b = 3.92027$ | -13.1860 | -6.15586 |
| $u = -0.672782 - 0.035203I$ $a = 0.07501 - 1.84158I$ $b = 0.115292 - 1.236343I$ | $5.72141 + 3.10928I$ | $-8.09311 - 4.32692I$ |
| $u = -0.672782 + 0.035203I$ $a = 0.07501 + 1.84158I$ $b = 0.115292 + 1.236343I$ | $5.72141 - 3.10928I$ | $-8.09311 + 4.32692I$ |
| $u = -0.125563 - 0.292930I$ $a = -0.451377 - 1.260813I$ $b = 0.312653 - 0.290533I$ | $-0.422559 + 0.990373I$ | $-6.71540 - 6.78739I$ |
| $u = -0.125563 + 0.292930I$ $a = -0.451377 + 1.260813I$ $b = 0.312653 + 0.290533I$ | $-0.422559 - 0.990373I$ | $-6.71540 + 6.78739I$ |
| $u = 1.07196$ $a = -0.382834$ $b = 0.410385$ | -1.55504 | -5.61011 |
| $u = 1.60362 - 0.62517I$ $a = 0.225319 + 0.092507I$ $b = -0.419159 - 0.007483I$ | $-4.86323 + 4.26845I$ | $-7.00188 - 6.39401I$ |
| $u = 1.60362 + 0.62517I$ $a = 0.225319 - 0.092507I$ $b = -0.419159 + 0.007483I$ | $-4.86323 - 4.26845I$ | $-7.00188 + 6.39401I$ |

III. u-Polynomials

| Crossings | u-Polynomials at each crossings |
|---------------|---|
| c_1 | $(u^8 + 2u^6 + \dots - u + 1)(u^{10} + 6u^9 + \dots + 14u + 4)$ |
| c_2 | $(u^8 + 4u^7 + 10u^6 + 16u^5 + 19u^4 + 15u^3 + 8u^2 + 3u + 1)$ $(u^{10} + 4u^9 + \dots + 36u + 16)$ |
| c_3, c_{11} | $(u^8 + u^6 + u^5 - 2u^4 - u + 1)$ $(u^{10} + u^9 - 10u^8 - 30u^7 + 42u^6 + 25u^5 - 18u^4 - 7u^3 - 10u^2 - 2u - 1)$ |
| c_4 | $(u^8 + u^6 - u^5 - 2u^4 + u + 1)$ $(u^{10} + u^9 - 10u^8 - 30u^7 + 42u^6 + 25u^5 - 18u^4 - 7u^3 - 10u^2 - 2u - 1)$ |
| c_5, c_{10} | $(u^8 - u^7 - 2u^4 + u^3 + u^2 + 1)$ $(u^{10} + 2u^9 - 12u^8 - 41u^7 + 4u^6 - 65u^5 + 12u^4 + 18u^3 - 8u^2 - u + 1)$ |
| c_6 | $(u^8 + 2u^6 + \dots + u + 1)(u^{10} + 6u^9 + \dots + 14u + 4)$ |
| c_7 | $(u^8 + 2u^6 + \dots + 3u + 1)(u^{10} + 6u^9 + \dots + 42u + 180)$ |
| c_8 | $(u^8 + 7u^7 + 17u^6 + 15u^5 + u^4 + 5u^2 + 2u + 1)$ $(u^{10} + 4u^9 - 3u^8 - 29u^7 - 21u^6 + 48u^5 + 80u^4 + 47u^3 + 16u^2 + 5u + 1)$ |
| c_9 | $(u^8 + u^7 - 2u^4 - u^3 + u^2 + 1)$ $(u^{10} + 2u^9 - 12u^8 - 41u^7 + 4u^6 - 65u^5 + 12u^4 + 18u^3 - 8u^2 - u + 1)$ |

IV. Riley Polynomials

| Crossings | Riley Polynomials at each crossings |
|--------------------|--|
| c_1, c_6 | $(y^8 + 4y^7 + 10y^6 + 16y^5 + 19y^4 + 15y^3 + 8y^2 + 3y + 1)$ $(y^{10} + 4y^9 + \dots + 36y + 16)$ |
| c_2 | $(y^8 + 4y^7 + 10y^6 + 20y^5 + 19y^4 + 3y^3 + 12y^2 + 7y + 1)$ $(y^{10} + 4y^9 + \dots - 1648y + 256)$ |
| c_3, c_4, c_{11} | $(y^8 + 2y^7 - 3y^6 - 5y^5 + 6y^4 + 4y^3 - 4y^2 - y + 1)$ $(y^{10} - 21y^9 + \dots + 16y + 1)$ |
| c_5, c_9, c_{10} | $(y^8 - y^7 - 4y^6 + 4y^5 + 6y^4 - 5y^3 - 3y^2 + 2y + 1)$ $(y^{10} - 28y^9 + \dots - 17y + 1)$ |
| c_7 | $(y^8 + 4y^7 + 6y^6 - 11y^5 + 33y^4 + 43y^3 + 21y^2 + y + 1)$ $(y^{10} - 56y^9 + \dots + 244836y + 32400)$ |
| c_8 | $(y^8 - 15y^7 + 81y^6 - 181y^5 + 145y^4 - 16y^3 + 27y^2 + 6y + 1)$ $(y^{10} - 22y^9 + \dots + 7y + 1)$ |