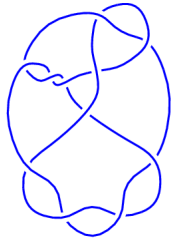
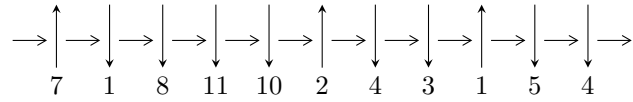


11n₁₃₉ (K11n₁₃₉)

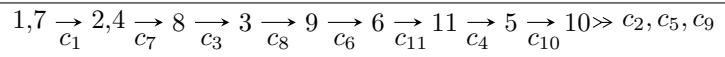


1

Arc Sequences



Solving Sequence



Representation Ideals

$$I = \bigcap_{i=1}^2 I_i^u$$

$$I_1^u = \langle u^4 + 3u^2 + 1, u^2 + a + 2, -u^3 + b - 2u \rangle$$

$$I_2^u = \langle u^8 + u^7 + 8u^6 + 4u^5 + 18u^4 + 11u^2 - 5u + 2, -u^7 - 8u^5 - 18u^3 + 2u^2 + 4b - 9u + 2, -u^7 - 6u^5 + 2u^4 - 8u^3 + 8u^2 + 4a + u + 4 \rangle$$

There are 2 irreducible components with 12 representations.

¹The knot diagram image is adapter from “C. Livingston and A. H. Moore, KnotInfo: Table of Knot Invariants, <http://www.indiana.edu/~knotinfo>”

$$\mathbf{I. } I_1^u = \langle u^4 + 3u^2 + 1, u^2 + a + 2, -u^3 + b - 2u \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^2 - 2 \\ u^3 + 2u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^3 + 3u + 1 \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^2 - 2 \\ u^3 + u^2 + 2u + 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^3 + 3u \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u^2 + 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^3 - 2u \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^2 + 1 \\ u^2 + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^2 + 1 \\ u^2 + 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.618034I$ $a = -1.61803$ $b = -1.00000I$	0.986960	0
$u = 0.618034I$ $a = -1.61803$ $b = 1.00000I$	0.986960	0
$u = -1.61803I$ $a = 0.618034$ $b = 1.00000I$	8.88264	0
$u = 1.61803I$ $a = 0.618034$ $b = -1.00000I$	8.88264	0

$$\text{II. } I_2^u = \langle u^8 + u^7 + 8u^6 + 4u^5 + 18u^4 + 11u^2 - 5u + 2, -u^7 - 8u^5 - 18u^3 + 2u^2 + 4b - 9u + 2, -u^7 - 6u^5 + 2u^4 - 8u^3 + 8u^2 + 4a + u + 4 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} \frac{1}{4}u^7 + \frac{3}{2}u^5 + \dots - \frac{1}{4}u - 1 \\ \frac{1}{4}u^7 + 2u^5 + \dots + \frac{9}{4}u - \frac{1}{2} \end{pmatrix}$$

$$a_2 = \begin{pmatrix} \frac{1}{4}u^7 + \frac{3}{2}u^5 + \dots - u^2 + \frac{11}{4}u \\ -\frac{1}{2}u^6 - \frac{1}{2}u^5 + \dots - \frac{3}{2}u^2 + \frac{3}{2}u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} \frac{1}{4}u^7 + \frac{3}{2}u^5 + \dots - \frac{1}{4}u - 1 \\ \frac{1}{2}u^6 + \frac{1}{2}u^5 + \dots + \frac{5}{2}u^2 + \frac{1}{2}u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} \frac{1}{4}u^7 + \frac{1}{2}u^6 + \dots + \frac{1}{2}u^2 + \frac{5}{4}u \\ -\frac{1}{2}u^6 - \frac{1}{2}u^5 + \dots - \frac{3}{2}u^2 + \frac{3}{2}u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^4 - 3u^2 - 1 \\ u^4 + 2u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^3 - 2u \\ u^5 + 3u^3 + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^2 + 1 \\ -u^4 - 2u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^2 + 1 \\ -u^4 - 2u^2 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.36613 - 1.66771I$ $a = -1.005552 - 0.492957I$ $b = -1.52012 + 0.43970I$	$12.93019 - 1.89326I$	$1.23462 + 1.04722I$
$u = -0.36613 + 1.66771I$ $a = -1.005552 + 0.492957I$ $b = -1.52012 - 0.43970I$	$12.93019 + 1.89326I$	$1.23462 - 1.04722I$
$u = -0.234808 - 1.029494I$ $a = 0.740043 + 0.762517I$ $b = 0.776759 + 0.445071I$	$3.66920 + 1.06491I$	$1.31198 - 1.63429I$
$u = -0.234808 + 1.029494I$ $a = 0.740043 - 0.762517I$ $b = 0.776759 - 0.445071I$	$3.66920 - 1.06491I$	$1.31198 + 1.63429I$
$u = -0.15755 - 1.96154I$ $a = 1.131185 - 0.148871I$ $b = 1.39990 - 1.57125I$	$-12.82706 - 5.56972I$	$0.47783 + 1.89693I$
$u = -0.15755 + 1.96154I$ $a = 1.131185 + 0.148871I$ $b = 1.39990 + 1.57125I$	$-12.82706 + 5.56972I$	$0.47783 - 1.89693I$
$u = 0.258486 - 0.303432I$ $a = -1.115676 + 0.333931I$ $b = -0.156540 - 0.733537I$	$-0.482455 + 0.984921I$	$-7.02443 - 7.03211I$
$u = 0.258486 + 0.303432I$ $a = -1.115676 - 0.333931I$ $b = -0.156540 + 0.733537I$	$-0.482455 - 0.984921I$	$-7.02443 + 7.03211I$

III. u-Polynomials

Crossings	u-Polynomials at each crossings
c_1, c_6	$(u^2 + 1)^2(u^8 + u^7 - u^6 - 8u^5 + 2u^4 + 7u^3 + 5u^2 + 4u + 5)$
c_2	$(u + 1)^4(u^8 + 3u^7 + \dots - 34u + 25)$
c_3, c_7, c_8	$(u^2 + 1)^2(u^8 + u^7 + 9u^6 + 2u^5 + 22u^4 - 5u^3 + 23u^2 + 6u + 5)$
c_4, c_5, c_{10} c_{11}	$(u^4 + 3u^2 + 1)(u^8 + u^7 + 8u^6 + 4u^5 + 18u^4 + 11u^2 - 5u + 2)$
c_9	$(u^2 - u - 1)^2$ $(u^8 + 11u^7 + 44u^6 + 62u^5 + 426u^4 - 1920u^3 + 1693u^2 - 389u + 136)$

IV. Riley Polynomials

Crossings	Riley Polynomials at each crossings
c_1, c_6	$(y + 1)^4(y^8 - 3y^7 + \dots + 34y + 25)$
c_2	$(y - 1)^4(y^8 + 33y^7 + \dots - 1706y + 625)$
c_3, c_7, c_8	$(y + 1)^4$ $(y^8 + 17y^7 + 121y^6 + 448y^5 + 916y^4 + 1053y^3 + 809y^2 + 194y + 25)$
c_4, c_5, c_{10} c_{11}	$(y^2 + 3y + 1)^2$ $(y^8 + 15y^7 + 92y^6 + 294y^5 + 514y^4 + 468y^3 + 193y^2 + 19y + 4)$
c_9	$(y^2 - 3y + 1)^2(y^8 - 33y^7 + \dots + 309175y + 18496)$