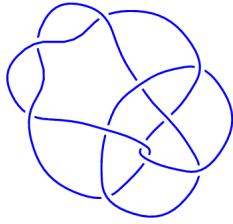
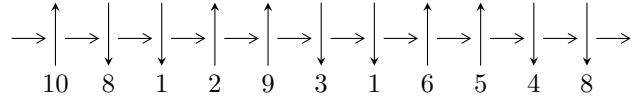


11n₁₅₅ (K11n₁₅₅)

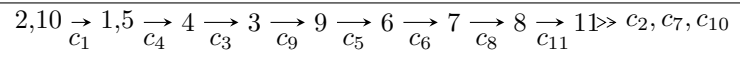


1

Arc Sequences



Solving Sequence



Representation Ideals

$$I = \bigcap_{i=1}^3 I_i^u$$

$$I_1^u = \langle u^9 + u^8 - 3u^6 + 2u^4 + 3u^3 - u^2 - u - 1, b + u, -u^8 + u^6 + 3u^5 - 3u^4 - 2u^3 - u^2 + a + 3u \rangle$$

$$I_2^u = \langle u^{16} - 7u^{15} + \dots - 26u + 7,$$

$$- 5989474225u^{15} + 35317058852u^{14} + \dots + 7635864529b - 29727831515,$$

$$34290455046u^{15} - 193768360261u^{14} + \dots + 53451051703a + 406627298359 \rangle$$

$$I_3^u = \langle u^{18} - u^{17} + \dots + 6u + 1, b + u, 95742u^{17} - 272489u^{16} + \dots + 148175a + 581762 \rangle$$

There are 3 irreducible components with 43 representations.

¹The knot diagram image is adapter from “C. Livingston and A. H. Moore, KnotInfo: Table of Knot Invariants, <http://www.indiana.edu/~knotinfo>”

$$\text{I. } I_1^u = \langle u^9 + u^8 - 3u^6 + 2u^4 + 3u^3 - u^2 - u - 1, b + u, -u^8 + u^6 + 3u^5 - 3u^4 - 2u^3 - u^2 + a + 3u \rangle$$

(i) Arc colorings

$$\begin{aligned} a_2 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} u^8 - u^6 - 3u^5 + 3u^4 + 2u^3 + u^2 - 3u \\ -u \end{pmatrix} \\ a_1 &= \begin{pmatrix} u^8 + u^7 - 3u^5 + 2u^3 + 2u^2 - u \\ u^2 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_4 &= \begin{pmatrix} -u \\ u \end{pmatrix} \\ a_3 &= \begin{pmatrix} u^8 + u^7 - 3u^5 + u^3 + 2u^2 - u + 1 \\ u^3 + u^2 + u \end{pmatrix} \\ a_9 &= \begin{pmatrix} u^8 - u^6 - 3u^5 + 3u^4 + 2u^3 + u^2 - 3u \\ u^3 - u - 1 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -u^7 + u^5 + 3u^4 - 2u^3 - 2u^2 - u + 2 \\ u^8 + u^7 - 2u^5 + u^3 + u^2 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -u^8 - 2u^7 + 3u^5 + u^4 - 6u^3 - 4u^2 + u + 3 \\ -u^7 - 2u^6 - u^5 + 2u^4 + 2u^3 - u^2 - 2u - 1 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -u^7 + u^5 + 2u^4 - 3u^3 - 2u^2 + 2 \\ -u^6 - u^5 + 2u^3 - u - 1 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} u^8 - u^6 - 3u^5 + 3u^4 + 2u^3 + u^2 - 3u + 1 \\ -u - 1 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} u^8 - u^6 - 3u^5 + 3u^4 + 2u^3 + u^2 - 3u + 1 \\ -u - 1 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.93778 - 1.07792I$ $a = -0.869995 - 0.592754I$ $b = 0.93778 + 1.07792I$	$-4.99677 + 5.78819I$	$-2.01216 - 5.60852I$
$u = -0.93778 + 1.07792I$ $a = -0.869995 + 0.592754I$ $b = 0.93778 - 1.07792I$	$-4.99677 - 5.78819I$	$-2.01216 + 5.60852I$
$u = -0.704599 - 0.747798I$ $a = -0.648299 + 0.197800I$ $b = 0.704599 + 0.747798I$	$1.13540 + 3.06246I$	$3.40537 - 6.53342I$
$u = -0.704599 + 0.747798I$ $a = -0.648299 - 0.197800I$ $b = 0.704599 - 0.747798I$	$1.13540 - 3.06246I$	$3.40537 + 6.53342I$
$u = -0.291926 - 0.569978I$ $a = 1.13307 + 1.40877I$ $b = 0.291926 + 0.569978I$	$-0.857058 - 0.898737I$	$-7.48049 - 2.86554I$
$u = -0.291926 + 0.569978I$ $a = 1.13307 - 1.40877I$ $b = 0.291926 - 0.569978I$	$-0.857058 + 0.898737I$	$-7.48049 + 2.86554I$
$u = 0.898266$ $a = -0.341074$ $b = -0.898266$	-6.41317	-5.42199
$u = 0.985174 - 0.537720I$ $a = 0.555759 - 1.205383I$ $b = -0.985174 + 0.537720I$	$-11.81419 + 1.53593I$	$-5.20172 - 0.08744I$
$u = 0.985174 + 0.537720I$ $a = 0.555759 + 1.205383I$ $b = -0.985174 - 0.537720I$	$-11.81419 - 1.53593I$	$-5.20172 + 0.08744I$

II.

$$I_2^u = \langle u^{16} - 7u^{15} + \dots - 26u + 7, -5.99 \times 10^9 u^{15} + 3.53 \times 10^{10} u^{14} + \dots + 7.64 \times 10^9 b - 2.97 \times 10^{10}, 3.43 \times 10^{10} u^{15} - 1.94 \times 10^{11} u^{14} + \dots + 5.35 \times 10^{10} a + 4.07 \times 10^{11} \rangle$$

(i) Arc colorings

$$\begin{aligned} a_2 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -0.641530u^{15} + 3.62516u^{14} + \dots + 13.2090u - 7.60747 \\ 0.784387u^{15} - 4.62516u^{14} + \dots - 1.49472u + 3.89318 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -0.471721u^{15} + 3.74197u^{14} + \dots - 39.9962u + 11.2928 \\ 1.02789u^{15} - 8.41954u^{14} + \dots + 77.8512u - 23.2585 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_4 &= \begin{pmatrix} -u \\ u \end{pmatrix} \\ a_3 &= \begin{pmatrix} -0.403962u^{15} + 3.65834u^{14} + \dots - 57.2020u + 14.7733 \\ 2.15783u^{15} - 16.6386u^{14} + \dots + 119.703u - 31.0972 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -0.641530u^{15} + 3.62516u^{14} + \dots + 13.2090u - 7.60747 \\ 0.615453u^{15} - 3.15412u^{14} + \dots - 19.5084u + 9.95207 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 0.201611u^{15} - 0.883525u^{14} + \dots - 11.2371u + 4.30542 \\ 0.452245u^{15} - 3.25232u^{14} + \dots + 11.3384u - 0.392224 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 0.296286u^{15} - 2.70439u^{14} + \dots + 52.5692u - 12.1830 \\ -0.151449u^{15} + 1.45205u^{14} + \dots - 37.5254u + 1.92491 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -0.501789u^{15} + 3.29201u^{14} + \dots - 13.2595u + 0.897630 \\ 0.335453u^{15} - 2.17614u^{14} + \dots + 15.9763u - 1.31484 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -0.641530u^{15} + 3.62516u^{14} + \dots + 14.2090u - 7.60747 \\ 0.784387u^{15} - 4.62516u^{14} + \dots - 2.49472u + 3.89318 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -0.641530u^{15} + 3.62516u^{14} + \dots + 14.2090u - 7.60747 \\ 0.784387u^{15} - 4.62516u^{14} + \dots - 2.49472u + 3.89318 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.81087 - 1.46236I$		
$a = 0.849619 + 0.334480I$	$-6.57974 + 5.23868I$	$-8.00000 - 3.04258I$
$b = -0.559608 - 0.857499I$		
$u = -0.81087 + 1.46236I$		
$a = 0.849619 - 0.334480I$	$-6.57974 - 5.23868I$	$-8.00000 + 3.04258I$
$b = -0.559608 + 0.857499I$		
$u = -0.530385 - 0.793677I$		
$a = 0.814519 - 0.270987I$	$0.02985 + 2.18536I$	$-4.41681 - 3.14055I$
$b = -0.232467 - 0.600007I$		
$u = -0.530385 + 0.793677I$		
$a = 0.814519 + 0.270987I$	$0.02985 - 2.18536I$	$-4.41681 + 3.14055I$
$b = -0.232467 + 0.600007I$		
$u = 0.028221 - 0.727930I$		
$a = 2.08457 + 0.00686I$	$-13.18932 - 2.18536I$	$-11.58319 + 3.14055I$
$b = -2.13775 - 1.37856I$		
$u = 0.028221 + 0.727930I$		
$a = 2.08457 - 0.00686I$	$-13.18932 + 2.18536I$	$-11.58319 - 3.14055I$
$b = -2.13775 + 1.37856I$		
$u = 0.232467 - 0.600007I$		
$a = -1.091833 - 0.655444I$	$0.02985 - 2.18536I$	$-4.41681 + 3.14055I$
$b = 0.530385 - 0.793677I$		
$u = 0.232467 + 0.600007I$		
$a = -1.091833 + 0.655444I$	$0.02985 + 2.18536I$	$-4.41681 - 3.14055I$
$b = 0.530385 + 0.793677I$		
$u = 0.503866 - 0.651460I$		
$a = 0.636481 - 0.057780I$	$-6.57974 - 1.04600I$	$-8.00000 + 6.68545I$
$b = -1.37934 - 0.90268I$		
$u = 0.503866 + 0.651460I$		
$a = 0.636481 + 0.057780I$	$-6.57974 + 1.04600I$	$-8.00000 - 6.68545I$
$b = -1.37934 + 0.90268I$		

Solution to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.559608 - 0.857499I$ $a = -1.34461 + 0.64449I$ $b = 0.81087 - 1.46236I$	$-6.57974 - 5.23868I$	$-8.00000 + 3.04258I$
$u = 0.559608 + 0.857499I$ $a = -1.34461 - 0.64449I$ $b = 0.81087 + 1.46236I$	$-6.57974 + 5.23868I$	$-8.00000 - 3.04258I$
$u = 1.37934 - 0.90268I$ $a = -0.003729 + 0.319275I$ $b = -0.503866 - 0.651460I$	$-6.57974 + 1.04600I$	$-8.00000 - 6.68545I$
$u = 1.37934 + 0.90268I$ $a = -0.003729 - 0.319275I$ $b = -0.503866 + 0.651460I$	$-6.57974 - 1.04600I$	$-8.00000 + 6.68545I$
$u = 2.13775 - 1.37856I$ $a = -0.302168 + 0.514875I$ $b = -0.028221 - 0.727930I$	$-13.18932 + 2.18536I$	$-11.58319 - 3.14055I$
$u = 2.13775 + 1.37856I$ $a = -0.302168 - 0.514875I$ $b = -0.028221 + 0.727930I$	$-13.18932 - 2.18536I$	$-11.58319 + 3.14055I$

$$\text{III. } I_3^u = \langle u^{18} - u^{17} + \cdots + 6u + 1, b + u, 9.57 \times 10^4 u^{17} - 2.72 \times 10^5 u^{16} + \cdots + 1.48 \times 10^5 a + 5.82 \times 10^5 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_2 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -0.646141u^{17} + 1.83897u^{16} + \cdots - 18.2110u - 3.92618 \\ -u \end{pmatrix} \\ a_1 &= \begin{pmatrix} -1.19283u^{17} + 2.12046u^{16} + \cdots + 0.0493336u + 0.353859 \\ u^2 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_4 &= \begin{pmatrix} -u \\ u \end{pmatrix} \\ a_3 &= \begin{pmatrix} 0.863911u^{17} - 0.546617u^{16} + \cdots + 6.73865u + 1.95620 \\ 0.328915u^{17} - 1.57384u^{16} + \cdots - 7.78799u - 1.31006 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -0.646141u^{17} + 1.83897u^{16} + \cdots - 18.2110u - 3.92618 \\ -0.927633u^{17} - 0.382426u^{16} + \cdots - 7.51081u - 1.19283 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 2.77863u^{17} - 3.65924u^{16} + \cdots + 13.4316u + 6.10807 \\ -0.392637u^{17} + 0.644798u^{16} + \cdots + 10.0158u + 2.07343 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 1.22635u^{17} - 2.06353u^{16} + \cdots + 18.4709u + 6.70072 \\ -0.305969u^{17} + 1.67221u^{16} + \cdots + 15.8621u + 3.25843 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -1.55385u^{17} + 1.56547u^{16} + \cdots - 16.1116u - 4.88383 \\ 0.0511355u^{17} - 0.352853u^{16} + \cdots - 8.53170u - 2.08505 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0.281491u^{17} + 2.22139u^{16} + \cdots - 11.7002u - 2.73336 \\ -0.927633u^{17} - 0.382426u^{16} + \cdots - 7.51081u - 1.19283 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0.281491u^{17} + 2.22139u^{16} + \cdots - 11.7002u - 2.73336 \\ -0.927633u^{17} - 0.382426u^{16} + \cdots - 7.51081u - 1.19283 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.98678 - 1.23806I$		
$a = -0.766575 - 0.547190I$	$-5.88062 + 4.16437I$	$-5.71584 - 1.90881I$
$b = 0.98678 + 1.23806I$		
$u = -0.98678 + 1.23806I$		
$a = -0.766575 + 0.547190I$	$-5.88062 - 4.16437I$	$-5.71584 + 1.90881I$
$b = 0.98678 - 1.23806I$		
$u = -0.739762 - 0.866952I$		
$a = -0.410148 + 0.023946I$	$0.25135 + 2.82287I$	$-6.88072 - 3.05587I$
$b = 0.739762 + 0.866952I$		
$u = -0.739762 + 0.866952I$		
$a = -0.410148 - 0.023946I$	$0.25135 - 2.82287I$	$-6.88072 + 3.05587I$
$b = 0.739762 - 0.866952I$		
$u = -0.302221 - 0.080115I$		
$a = 1.67582 + 2.59626I$	$-0.45845 + 1.47133I$	$-0.00849 - 6.64687I$
$b = 0.302221 + 0.080115I$		
$u = -0.302221 + 0.080115I$		
$a = 1.67582 - 2.59626I$	$-0.45845 - 1.47133I$	$-0.00849 + 6.64687I$
$b = 0.302221 - 0.080115I$		
$u = -0.170673 - 0.568505I$		
$a = 0.774909 + 0.330314I$	$-0.543265 + 1.120071I$	$-3.86919 - 5.32416I$
$b = 0.170673 + 0.568505I$		
$u = -0.170673 + 0.568505I$		
$a = 0.774909 - 0.330314I$	$-0.543265 - 1.120071I$	$-3.86919 + 5.32416I$
$b = 0.170673 - 0.568505I$		
$u = 0.028471 - 1.040199I$		
$a = -1.52237 + 0.37502I$	$-14.5599 + 1.9312I$	$-9.20699 - 1.03940I$
$b = -0.028471 + 1.040199I$		
$u = 0.028471 + 1.040199I$		
$a = -1.52237 - 0.37502I$	$-14.5599 - 1.9312I$	$-9.20699 + 1.03940I$
$b = -0.028471 - 1.040199I$		

Solution to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.464186 - 0.991439I$		
$a = -0.047637 + 0.952184I$	$-7.77265 - 2.85464I$	$-5.54920 + 2.31741I$
$b = -0.464186 + 0.991439I$		
$u = 0.464186 + 0.991439I$		
$a = -0.047637 - 0.952184I$	$-7.77265 + 2.85464I$	$-5.54920 - 2.31741I$
$b = -0.464186 - 0.991439I$		
$u = 0.481449 - 0.953626I$		
$a = 1.250342 - 0.610225I$	$-6.93662 + 0.90661I$	$-5.69894 - 2.68686I$
$b = -0.481449 + 0.953626I$		
$u = 0.481449 + 0.953626I$		
$a = 1.250342 + 0.610225I$	$-6.93662 - 0.90661I$	$-5.69894 + 2.68686I$
$b = -0.481449 - 0.953626I$		
$u = 0.78194 - 1.18447I$		
$a = 0.693826 + 0.210668I$	$-8.36952 - 8.49029I$	$-4.40486 + 6.13776I$
$b = -0.78194 + 1.18447I$		
$u = 0.78194 + 1.18447I$		
$a = 0.693826 - 0.210668I$	$-8.36952 + 8.49029I$	$-4.40486 - 6.13776I$
$b = -0.78194 - 1.18447I$		
$u = 0.94339 - 1.44899I$		
$a = 0.851833 - 0.375849I$	$-15.7704 - 12.3848I$	$-6.66577 + 5.56864I$
$b = -0.94339 + 1.44899I$		
$u = 0.94339 + 1.44899I$		
$a = 0.851833 + 0.375849I$	$-15.7704 + 12.3848I$	$-6.66577 - 5.56864I$
$b = -0.94339 - 1.44899I$		

IV. u-Polynomials

Crossings	u-Polynomials at each crossings
c_1, c_4	$(u^9 - u^8 + \dots - u + 1)(u^{16} + 7u^{15} + \dots + 26u + 7)$ $(u^{18} + u^{17} + \dots - 6u + 1)$
c_2	$(u^9 - 4u^7 + \dots + u^2 + 1)(u^{16} + u^{15} + \dots + 244u + 263)$ $(u^{18} - 10u^{16} + \dots + u + 23)$
c_3	$(u^8 + 7u^7 + 17u^6 + 14u^5 - u^4 + 2u^3 + 6u^2 - 4u + 1)^2$ $(u^9 + 8u^8 + 28u^7 + 59u^6 + 88u^5 + 99u^4 + 83u^3 + 51u^2 + 21u + 5)$ $(u^{18} - 11u^{17} + \dots - 17u + 24)$
c_5	$(u^8 - u^7 + 5u^6 - 4u^5 + 7u^4 - 4u^3 + 2u^2 + 1)^2$ $(u^9 + 2u^8 + 7u^7 + 10u^6 + 16u^5 + 15u^4 + 12u^3 + 5u^2 - 1)$ $(u^{18} + 5u^{17} + \dots + 13u + 2)$
c_6, c_{11}	$(u^9 - u^8 + \dots + 3u^2 + 1)(u^{16} + u^{15} + \dots - 54u + 43)$ $(u^{18} - u^{17} + \dots - u + 1)$
c_7	$(u^9 + u^8 + \dots - 3u^2 - 1)(u^{16} + u^{15} + \dots - 54u + 43)$ $(u^{18} - u^{17} + \dots - u + 1)$
c_8, c_9	$(u^8 - u^7 + 5u^6 - 4u^5 + 7u^4 - 4u^3 + 2u^2 + 1)^2$ $(u^9 - 2u^8 + 7u^7 - 10u^6 + 16u^5 - 15u^4 + 12u^3 - 5u^2 + 1)$ $(u^{18} + 5u^{17} + \dots + 13u + 2)$
c_{10}	$(u + 1)^{16}(u^9 - u^8 + u^7 + 3u^6 - 2u^5 + 3u^3 - u + 1)$ $(u^{18} - 16u^{17} + \dots - 1792u + 256)$

V. Riley Polynomials

Crossings	Riley Polynomials at each crossings
c_1, c_4	$(y^9 - y^8 + 6y^7 - 7y^6 + 12y^5 - 8y^4 + 7y^3 - 3y^2 - y - 1)$ $(y^{16} - y^{15} + \dots + 472y + 49)(y^{18} + 11y^{17} + \dots - 8y + 1)$
c_2	$(y^9 - 8y^8 + 34y^7 - 78y^6 + 81y^5 - 26y^4 - 7y^3 - 5y^2 - 2y - 1)$ $(y^{16} - 17y^{15} + \dots - 326744y + 69169)$ $(y^{18} - 20y^{17} + \dots + 597y + 529)$
c_3	$(y^8 - 15y^7 + 91y^6 - 246y^5 + 207y^4 + 130y^3 + 50y^2 - 4y + 1)^2$ $(y^9 - 8y^8 + 16y^7 + 29y^6 - 64y^5 - 115y^4 - 103y^3 - 105y^2 - 69y - 25)$ $(y^{18} - 23y^{17} + \dots - 433y + 576)$
c_5, c_8, c_9	$(y^8 + 9y^7 + 31y^6 + 50y^5 + 39y^4 + 22y^3 + 18y^2 + 4y + 1)^2$ $(y^9 + 10y^8 + 41y^7 + 88y^6 + 104y^5 + 63y^4 + 14y^3 + 5y^2 + 10y - 1)$ $(y^{18} + 19y^{17} + \dots + 47y + 4)$
c_6, c_7, c_{11}	$(y^9 - 7y^8 + 13y^7 - 2y^5 - 14y^4 - 16y^3 - 13y^2 - 6y - 1)$ $(y^{16} - 21y^{15} + \dots - 8076y + 1849)(y^{18} - 27y^{17} + \dots - 7y + 1)$
c_{10}	$(y - 1)^{16}(y^9 + y^8 + 3y^7 - 7y^6 + 8y^5 - 12y^4 + 7y^3 - 6y^2 + y - 1)$ $(y^{18} + 70y^{16} + \dots + 262144y + 65536)$