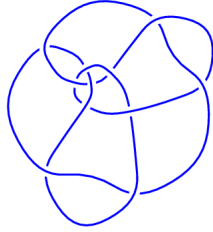
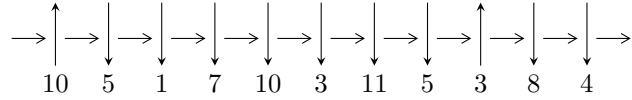


11n₁₆₂ (K11n₁₆₂)

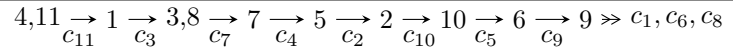


1

Arc Sequences



Solving Sequence



Representation Ideals

$$I = \bigcap_{i=1}^4 I_i^u$$

$$I_1^u = \langle u^6 - 7u^5 + 18u^4 - 22u^3 + 15u^2 - 5u + 1, -2u^5 + 13u^4 - 29u^3 + 27u^2 + a - 12u, -u^5 + 7u^4 - 17u^3 + 18u^2 + b - 10u + 2 \rangle$$

$$I_2^u = \langle b^6 + 2b^5 + 4b^4 + 6b^3 + 6b^2 + 5b + 3, -b^4 - 2b^3 - 3b^2 - 3b + u - 1, -b^5 - 2b^4 - 4b^3 - 5b^2 - 5b + a - 4 \rangle$$

$$I_3^u = \langle u^{13} - 24u^{12} + \dots - 2016u + 480, -219031775u^{12} + 4687623230u^{11} + \dots + 903641744b + 43146415952, -2696650997u^{12} + 58148670678u^{11} + \dots + 27109252320a + 610906263072 \rangle$$

$$I_4^u = \langle b^{26} - 3b^{25} + \dots - 9b + 1, -280010027772943b^{25} + 640188464864309u + \dots - 9045506250176506b + 911334568428454, 1931825958972041b^{25} - 5354645722954962b^{24} + \dots + 1920565394592927a - 4009504723628393 \rangle$$

There are 4 irreducible components with 51 representations.

¹The knot diagram image is adapter from “C. Livingston and A. H. Moore, KnotInfo: Table of Knot Invariants, <http://www.indiana.edu/~knotinfo>”

$$\mathbf{I. } I_1^u = \langle u^6 - 7u^5 + 18u^4 - 22u^3 + 15u^2 - 5u + 1, -2u^5 + 13u^4 - 29u^3 + 27u^2 + a - 12u, -u^5 + 7u^4 - 17u^3 + 18u^2 + b - 10u + 2 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_4 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 2u^5 - 13u^4 + 29u^3 - 27u^2 + 12u \\ u^5 - 7u^4 + 17u^3 - 18u^2 + 10u - 2 \end{pmatrix} \\ a_1 &= \begin{pmatrix} u^5 - 6u^4 + 12u^3 - 9u^2 + 2u + 2 \\ u^5 - 7u^4 + 17u^3 - 18u^2 + 10u - 2 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -2u^5 + 14u^4 - 35u^3 + 39u^2 - 22u + 5 \\ -u^3 + 4u^2 - 4u + 2 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_7 &= \begin{pmatrix} 2u^5 - 14u^4 + 36u^3 - 43u^2 + 26u - 6 \\ u^3 - 4u^2 + 5u - 2 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -3u^5 + 20u^4 - 47u^3 + 48u^2 - 24u + 3 \\ -u^5 + 8u^4 - 22u^3 + 26u^2 - 15u + 3 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -u^4 + 7u^3 - 17u^2 + 17u - 7 \\ u^3 - 4u^2 + 5u - 3 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 2u^5 - 13u^4 + 29u^3 - 27u^2 + 12u \\ u^5 - 6u^4 + 13u^3 - 13u^2 + 7u - 1 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -u^4 + 7u^3 - 17u^2 + 17u - 7 \\ -u^5 + 7u^4 - 17u^3 + 17u^2 - 7u \end{pmatrix} \\ a_9 &= \begin{pmatrix} u^4 - 7u^3 + 17u^2 - 17u + 7 \\ u^5 - 6u^4 + 12u^3 - 9u^2 + 2u + 2 \end{pmatrix} \\ a_9 &= \begin{pmatrix} u^4 - 7u^3 + 17u^2 - 17u + 7 \\ u^5 - 6u^4 + 12u^3 - 9u^2 + 2u + 2 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =unknown

(iv) Complex Volumes and Cusp Shapes

| Solution to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------------------|
| $u = 0.211778 - 0.330391I$ $a = 2.74807 - 0.64577I$ $b = 0.368622 - 1.044697I$ | $9.91965 + 2.91185I$ | $-0.22592 - 3.63955I$ |
| $u = 0.211778 + 0.330391I$ $a = 2.74807 + 0.64577I$ $b = 0.368622 + 1.044697I$ | $9.91965 - 2.91185I$ | $-0.22592 + 3.63955I$ |
| $u = 0.717525 - 0.672354I$ $a = -0.033577 - 0.670495I$ $b = -0.474902 - 0.458521I$ | $-1.33814 - 0.90202I$ | $-11.17385 + 4.13696I$ |
| $u = 0.717525 + 0.672354I$ $a = -0.033577 + 0.670495I$ $b = -0.474902 + 0.458521I$ | $-1.33814 + 0.90202I$ | $-11.17385 - 4.13696I$ |
| $u = 2.57070 - 0.32705I$ $a = -0.214491 + 0.482108I$ $b = -0.393720 + 1.309502I$ | $4.57797 + 6.62522I$ | $-5.60023 - 6.47362I$ |
| $u = 2.57070 + 0.32705I$ $a = -0.214491 - 0.482108I$ $b = -0.393720 - 1.309502I$ | $4.57797 - 6.62522I$ | $-5.60023 + 6.47362I$ |

$$\text{II. } I_2^u = \langle b^6 + 2b^5 + 4b^4 + 6b^3 + 6b^2 + 5b + 3, -b^4 - 2b^3 - 3b^2 - 3b + u - 1, -b^5 - 2b^4 - 4b^3 - 5b^2 - 5b + a - 4 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_4 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} b^5 + 2b^4 + 4b^3 + 5b^2 + 5b + 4 \\ b \end{pmatrix} \\ a_1 &= \begin{pmatrix} b^5 + 2b^4 + 4b^3 + 5b^2 + 4b + 4 \\ b \end{pmatrix} \\ a_3 &= \begin{pmatrix} b^3 + 2b^2 + b + 4 \\ -b^2 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 0 \\ b^4 + 2b^3 + 3b^2 + 3b + 1 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -b^5 - 2b^4 - 4b^3 - 4b^2 - 5b - 2 \\ b^3 + b^2 + b + 1 \end{pmatrix} \\ a_5 &= \begin{pmatrix} b^5 + b^4 + 2b^3 + 3b^2 + b + 2 \\ -b^4 - 2b^3 - 3b^2 - 3b - 2 \end{pmatrix} \\ a_2 &= \begin{pmatrix} b^3 + b^2 + b + 2 \\ b^5 + 2b^4 + 2b^3 + b^2 - 1 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} b^5 + 2b^4 + 4b^3 + 5b^2 + 5b + 4 \\ b^5 + 2b^4 + 2b^3 + 2b^2 + b - 1 \end{pmatrix} \\ a_6 &= \begin{pmatrix} b^5 + 2b^4 + 2b^3 + 4b^2 + 2b + 2 \\ b^5 + 2b^4 + 4b^3 + 5b^2 + 4b + 1 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 2b^5 + 2b^4 + 6b^3 + 6b^2 + 5b + 5 \\ b^4 + b^3 + b^2 + b - 1 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 2b^5 + 2b^4 + 6b^3 + 6b^2 + 5b + 5 \\ b^4 + b^3 + b^2 + b - 1 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

| Solution to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = -0.426050 + 0.368989I$ $a = 1.62708 - 1.36745I$ $b = -1.044140 - 0.390425I$ | $1.07850 + 1.58317I$ | $-4.02349 - 3.48462I$ |
| $u = -0.426050 - 0.368989I$ $a = 1.62708 + 1.36745I$ $b = -1.044140 + 0.390425I$ | $1.07850 - 1.58317I$ | $-4.02349 + 3.48462I$ |
| $u = -0.426050 - 0.368989I$ $a = 0.94687 - 1.73644I$ $b = -0.188646 - 1.182977I$ | $1.07850 - 1.58317I$ | $-4.02349 + 3.48462I$ |
| $u = -0.426050 + 0.368989I$ $a = 0.94687 + 1.73644I$ $b = -0.188646 + 1.182977I$ | $1.07850 + 1.58317I$ | $-4.02349 - 3.48462I$ |
| $u = -3.14790$ $a = -0.073950 - 0.405345I$ $b = 0.232786 - 1.275985I$ | 11.0025 | -0.953017 |
| $u = -3.14790$ $a = -0.073950 + 0.405345I$ $b = 0.232786 + 1.275985I$ | 11.0025 | -0.953017 |

$$\text{III. } I_3^u = \langle u^{13} - 24u^{12} + \dots - 2016u + 480, -2.19 \times 10^8 u^{12} + 4.69 \times 10^9 u^{11} + \dots + 9.04 \times 10^8 b + 4.31 \times 10^{10}, -2.70 \times 10^9 u^{12} + 5.81 \times 10^{10} u^{11} + \dots + 2.71 \times 10^{10} a + 6.11 \times 10^{11} \rangle$$

(i) Arc colorings

$$\begin{aligned} a_4 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0.0994735u^{12} - 2.14498u^{11} + \dots + 88.4038u - 22.5350 \\ 0.242388u^{12} - 5.18748u^{11} + \dots + 178.004u - 47.7473 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -0.142914u^{12} + 3.04250u^{11} + \dots - 89.5997u + 25.2123 \\ 0.242388u^{12} - 5.18748u^{11} + \dots + 178.004u - 47.7473 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -0.0565209u^{12} + 1.24812u^{11} + \dots - 52.9216u + 15.8826 \\ 0.105111u^{12} - 2.30917u^{11} + \dots + 89.5168u - 23.3232 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_7 &= \begin{pmatrix} -0.0485900u^{12} + 1.06105u^{11} + \dots - 36.5952u + 8.44059 \\ -0.105111u^{12} + 2.30917u^{11} + \dots - 88.5168u + 23.3232 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 0.0843754u^{12} - 1.82264u^{11} + \dots + 66.1376u - 17.2594 \\ -0.0111211u^{12} + 0.349662u^{11} + \dots - 36.7390u + 9.95305 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -0.129345u^{12} + 2.74183u^{11} + \dots - 75.8747u + 22.8445 \\ 0.211793u^{12} - 4.54561u^{11} + \dots + 159.148u - 42.2710 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 0.0994735u^{12} - 2.14498u^{11} + \dots + 88.4038u - 22.5350 \\ -0.387441u^{12} + 8.27096u^{11} + \dots - 262.903u + 68.5989 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 0.178070u^{12} - 3.82028u^{11} + \dots + 130.508u - 33.6483 \\ -0.453399u^{12} + 9.71423u^{11} + \dots - 325.341u + 85.4737 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -0.0943531u^{12} + 1.98564u^{11} + \dots - 55.2274u + 15.3443 \\ 0.504250u^{12} - 10.7447u^{11} + \dots + 352.239u - 92.3938 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -0.0943531u^{12} + 1.98564u^{11} + \dots - 55.2274u + 15.3443 \\ 0.504250u^{12} - 10.7447u^{11} + \dots + 352.239u - 92.3938 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

| Solution to I_3^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|-----------------------|
| $u = -0.696637$ $a = 0.314085$ $b = -0.218803$ | -0.973187 | -8.95549 |
| $u = 0.199032 - 0.612878I$ $a = 0.561529 + 1.138335I$ $b = 0.809423 - 0.117584I$ | $5.36911 + 2.95494I$ | $-7.16291 - 2.81901I$ |
| $u = 0.199032 + 0.612878I$ $a = 0.561529 - 1.138335I$ $b = 0.809423 + 0.117584I$ | $5.36911 - 2.95494I$ | $-7.16291 + 2.81901I$ |
| $u = 0.263411 - 0.441744I$ $a = 0.312290 - 1.271242I$ $b = -0.479303 - 0.472811I$ | $-0.52618 - 1.43256I$ | $-3.73519 + 6.28375I$ |
| $u = 0.263411 + 0.441744I$ $a = 0.312290 + 1.271242I$ $b = -0.479303 + 0.472811I$ | $-0.52618 + 1.43256I$ | $-3.73519 - 6.28375I$ |
| $u = 2.34475 - 0.66404I$ $a = 0.204341 - 0.493346I$ $b = 0.151527 - 1.292462I$ | $6.35965 - 0.39707I$ | $-2.26484 + 2.21487I$ |
| $u = 2.34475 + 0.66404I$ $a = 0.204341 + 0.493346I$ $b = 0.151527 + 1.292462I$ | $6.35965 + 0.39707I$ | $-2.26484 - 2.21487I$ |
| $u = 2.53526 - 0.14222I$ $a = -0.127215 - 0.575447I$ $b = -0.40436 - 1.44082I$ | $6.52797 - 5.89125I$ | $-0.30193 + 3.39089I$ |
| $u = 2.53526 + 0.14222I$ $a = -0.127215 + 0.575447I$ $b = -0.40436 + 1.44082I$ | $6.52797 + 5.89125I$ | $-0.30193 - 3.39089I$ |
| $u = 2.93435 - 0.11492I$ $a = 0.185374 - 0.504984I$ $b = 0.48592 - 1.50310I$ | $15.6748 + 13.1069I$ | $-1.18846 - 5.87531I$ |

| Solution to I_3^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 2.93435 + 0.11492I$ | | |
| $a = 0.185374 + 0.504984I$ | $15.6748 - 13.1069I$ | $-1.18846 + 5.87531I$ |
| $b = 0.48592 + 1.50310I$ | | |
| $u = 4.07152 - 1.55549I$ | | |
| $a = -0.093363 + 0.274076I$ | $12.31696 - 2.15873I$ | $3.13107 + 3.07256I$ |
| $b = 0.046196 + 1.261130I$ | | |
| $u = 4.07152 + 1.55549I$ | | |
| $a = -0.093363 - 0.274076I$ | $12.31696 + 2.15873I$ | $3.13107 - 3.07256I$ |
| $b = 0.046196 - 1.261130I$ | | |

IV.

$$I_4^u = \langle b^{26} - 3b^{25} + \dots - 9b + 1, 6.40 \times 10^{14}u - 2.80 \times 10^{14}b^{25} + \dots - 9.05 \times 10^{15}b + 9.11 \times 10^{14}, 1.93 \times 10^{15}b^{25} - 5.35 \times 10^{15}b^{24} + \dots + 1.92 \times 10^{15}a - 4.01 \times 10^{15} \rangle$$

(i) Arc colorings

$$\begin{aligned} a_4 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -1.00586b^{25} + 2.78806b^{24} + \dots - 18.7038b + 2.08767 \\ b \end{pmatrix} \\ a_1 &= \begin{pmatrix} -1.00586b^{25} + 2.78806b^{24} + \dots - 19.7038b + 2.08767 \\ b \end{pmatrix} \\ a_3 &= \begin{pmatrix} 0.229532b^{25} - 0.636550b^{24} + \dots + 6.96510b - 0.00586315 \\ -b^2 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 0 \\ 0.437387b^{25} - 1.02758b^{24} + \dots + 14.1294b - 1.42354 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 0.973498b^{25} - 2.54878b^{24} + \dots + 15.1574b - 3.22989 \\ 0.738314b^{25} - 1.84839b^{24} + \dots + 15.4595b - 1.32528 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -0.353112b^{25} + 1.05017b^{24} + \dots - 8.22868b + 0.546894 \\ 0.624907b^{25} - 2.12314b^{24} + \dots + 25.2114b - 3.59109 \end{pmatrix} \\ a_2 &= \begin{pmatrix} 0.0982585b^{25} - 0.595703b^{24} + \dots + 11.7692b - 2.21440 \\ 0.851882b^{25} - 2.18042b^{24} + \dots + 12.8033b + 1.43267 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -1.00586b^{25} + 2.78806b^{24} + \dots - 18.7038b + 2.08767 \\ 0.0591345b^{25} + 0.0776802b^{24} + \dots + 2.44901b - 1.85007 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -1.39158b^{25} + 3.70478b^{24} + \dots - 30.6015b + 5.15885 \\ -0.682959b^{25} + 1.75673b^{24} + \dots - 14.2343b + 1.11476 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -0.585691b^{25} + 1.68463b^{24} + \dots - 13.7189b + 2.97508 \\ 0.00282387b^{25} + 0.201032b^{24} + \dots + 1.47093b - 1.71634 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -0.585691b^{25} + 1.68463b^{24} + \dots - 13.7189b + 2.97508 \\ 0.00282387b^{25} + 0.201032b^{24} + \dots + 1.47093b - 1.71634 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

| Solution to I_4^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|-----------------------|
| $u = -0.212184 - 0.601220I$ | | |
| $a = 1.78123 + 0.51570I$ | $1.265646 - 0.287296I$ | $-2.88954 - 0.89161I$ |
| $b = -1.207500 - 0.051879I$ | | |
| $u = -0.212184 + 0.601220I$ | | |
| $a = 1.78123 - 0.51570I$ | $1.265646 + 0.287296I$ | $-2.88954 + 0.89161I$ |
| $b = -1.207500 + 0.051879I$ | | |
| $u = -2.55159 - 0.69397I$ | | |
| $a = -0.204696 - 0.440581I$ | $5.76658 - 5.41588I$ | $-0.94009 + 2.54727I$ |
| $b = -0.45644 - 1.36303I$ | | |
| $u = -2.55159 + 0.69397I$ | | |
| $a = -0.204696 + 0.440581I$ | $5.76658 + 5.41588I$ | $-0.94009 - 2.54727I$ |
| $b = -0.45644 + 1.36303I$ | | |
| $u = -1.02005$ | | |
| $a = 0.247472 - 0.411191I$ | -0.889471 | -5.46516 |
| $b = -0.252433 - 0.419434I$ | | |
| $u = -1.02005$ | | |
| $a = 0.247472 + 0.411191I$ | -0.889471 | -5.46516 |
| $b = -0.252433 + 0.419434I$ | | |
| $u = -0.131463 - 0.355843I$ | | |
| $a = -0.308504 + 1.360323I$ | $2.03958 - 2.67289I$ | $-1.48191 + 5.19592I$ |
| $b = -0.247316 - 1.177338I$ | | |
| $u = -0.131463 + 0.355843I$ | | |
| $a = -0.308504 - 1.360323I$ | $2.03958 + 2.67289I$ | $-1.48191 - 5.19592I$ |
| $b = -0.247316 + 1.177338I$ | | |
| $u = -0.212184 - 0.601220I$ | | |
| $a = 0.70704 - 1.75888I$ | $1.265646 - 0.287296I$ | $-2.88954 - 0.89161I$ |
| $b = -0.067900 - 1.180333I$ | | |
| $u = -0.212184 + 0.601220I$ | | |
| $a = 0.70704 + 1.75888I$ | $1.265646 + 0.287296I$ | $-2.88954 + 0.89161I$ |
| $b = -0.067900 + 1.180333I$ | | |

| Solution to I_4^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|-----------------------|
| $u = -2.31351 + 0.01822I$ $a = -0.332532 - 0.674434I$ $b = 0.052461 - 1.357580I$ | $13.70611 - 0.67900I$ | $1.58151 + 0.47574I$ |
| $u = -2.31351 - 0.01822I$ $a = -0.332532 + 0.674434I$ $b = 0.052461 + 1.357580I$ | $13.70611 + 0.67900I$ | $1.58151 - 0.47574I$ |
| $u = 0.726221 - 1.104014I$ $a = -0.623167 + 0.767003I$ $b = 0.160428 - 0.147487I$ | $8.78740 - 1.45996I$ | $-3.65650 + 0.27682I$ |
| $u = 0.726221 + 1.104014I$ $a = -0.623167 - 0.767003I$ $b = 0.160428 + 0.147487I$ | $8.78740 + 1.45996I$ | $-3.65650 - 0.27682I$ |
| $u = -2.55159 + 0.69397I$ $a = 0.301845 - 0.452092I$ $b = 0.216549 - 1.266236I$ | $5.76658 + 5.41588I$ | $-0.94009 - 2.54727I$ |
| $u = -2.55159 - 0.69397I$ $a = 0.301845 + 0.452092I$ $b = 0.216549 + 1.266236I$ | $5.76658 - 5.41588I$ | $-0.94009 + 2.54727I$ |
| $u = 0.492555 + 0.725715I$ $a = 0.55639 - 1.37912I$ $b = 0.326804 - 1.347110I$ | $10.00278 + 7.01304I$ | $-2.38090 - 4.98186I$ |
| $u = 0.492555 - 0.725715I$ $a = 0.55639 + 1.37912I$ $b = 0.326804 + 1.347110I$ | $10.00278 - 7.01304I$ | $-2.38090 + 4.98186I$ |
| $u = 0.726221 + 1.104014I$ $a = 0.159963 - 0.040090I$ $b = 0.394224 - 1.244999I$ | $8.78740 + 1.45996I$ | $-3.65650 - 0.27682I$ |
| $u = 0.726221 - 1.104014I$ $a = 0.159963 + 0.040090I$ $b = 0.394224 + 1.244999I$ | $8.78740 - 1.45996I$ | $-3.65650 + 0.27682I$ |

| Solution to I_4^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|-----------------------|
| $u = -0.131463 - 0.355843I$ $a = 3.13717 + 0.46398I$ $b = 0.524618 - 0.069053I$ | $2.03958 - 2.67289I$ | $-1.48191 + 5.19592I$ |
| $u = -0.131463 + 0.355843I$ $a = 3.13717 - 0.46398I$ $b = 0.524618 + 0.069053I$ | $2.03958 + 2.67289I$ | $-1.48191 - 5.19592I$ |
| $u = -2.31351 - 0.01822I$ $a = -0.027296 - 0.586589I$ $b = 0.78161 - 1.55425I$ | $13.70611 + 0.67900I$ | $1.58151 - 0.47574I$ |
| $u = -2.31351 + 0.01822I$ $a = -0.027296 + 0.586589I$ $b = 0.78161 + 1.55425I$ | $13.70611 - 0.67900I$ | $1.58151 + 0.47574I$ |
| $u = 0.492555 + 0.725715I$ $a = -1.06159 - 1.17084I$ $b = 1.274903 - 0.275508I$ | $10.00278 + 7.01304I$ | $-2.38090 - 4.98186I$ |
| $u = 0.492555 - 0.725715I$ $a = -1.06159 + 1.17084I$ $b = 1.274903 + 0.275508I$ | $10.00278 - 7.01304I$ | $-2.38090 + 4.98186I$ |

V. u-Polynomials

| Crossings | u-Polynomials at each crossings |
|---------------|--|
| c_1 | $(u^3 + u^2 - 2u + 1)^2(u^6 - u^5 + 8u^3 + 3u^2 - u + 3)$ $(1 + 47u - 142u^2 + 100u^3 + 127u^4 - 214u^5 + 26u^6 + 122u^7 - 59u^8 - 26u^9 + 24u^{10} - 4u^{12} +$ $(u^{13} + 16u^{12} + \dots + 384u + 32)$ |
| c_2, c_5 | $(u^6 + 2u^4 + 3u^3 - 2u^2 - 2u + 1)(u^6 + 3u^4 - 3u^3 - u + 3)$ $(u^{13} + 12u^{11} + \dots - 7u^2 - 1)(u^{26} + u^{25} + \dots - 193u + 61)$ |
| c_3, c_{10} | $(u^6 + u^5 + 3u^4 + 2u^3 + 3u^2 + 2u + 1)$ $(u^6 + 2u^5 + \dots + 5u + 3)(u^{13} + u^{12} + \dots + 4u - 1)$ $(u^{26} + 3u^{25} + \dots + 9u + 1)$ |
| c_4 | $(u^3 + u^2 + 1)^2(u^6 - 2u^5 + 3u^4 - 2u^3 + 5u^2 - 7u + 3)$ $(-5 + 8u - 20u^2 + 23u^3 - 26u^4 + 29u^5 - 17u^6 + 25u^7 - 7u^8 + 14u^9 - 2u^{10} + 5u^{11} - u^{12} + u$ $(u^{13} + 11u^{12} + \dots - 40u - 4)$ |
| c_6, c_8 | $(u^6 - 3u^5 + \dots + 2u + 1)(u^6 + u^5 + \dots + u + 1)$ $(u^{13} - u^{12} + \dots - 11u + 3)(u^{26} + 4u^{25} + \dots + 2400u + 1353)$ |
| c_7, c_{11} | $(u^6 - 2u^5 + 4u^4 - 6u^3 + 6u^2 - 5u + 3)$ $(u^6 - u^5 + \dots - 2u + 1)(u^{13} + u^{12} + \dots + 4u - 1)$ $(u^{26} + 3u^{25} + \dots + 9u + 1)$ |
| c_9 | $(u^3 + u^2 + 1)^2(u^6 - 3u^5 + 2u^4 + u^2 - u + 1)$ $(-3 + 2u + 20u^2 - 23u^3 - 32u^4 + 63u^5 - 7u^6 + 7u^7 - 39u^8 + 4u^9 + 20u^{10} - 5u^{11} - 3u^{12} + u$ $(u^{13} + 8u^{12} + \dots + 6u - 12)$ |

VI. Riley Polynomials

| Crossings | Riley Polynomials at each crossings |
|--------------------------------|--|
| c_1 | $(y^3 - 5y^2 + 2y - 1)^2(y^6 - y^5 + 22y^4 - 60y^3 + 25y^2 + 17y + 9)$ $(-1 + 2493y - 1.10 \times 10^4 y^2 + 2.59 \times 10^4 y^3 - 4.00 \times 10^4 y^4 + 4.43 \times 10^4 y^5 - 3.63 \times 10^4 y^6 + \dots)$ $(y^{13} - 12y^{12} + \dots + 59904y - 1024)$ |
| c_2, c_5 | $(y^6 + 4y^5 + \dots - 8y + 1)(y^6 + 6y^5 + \dots - y + 9)$ $(y^{13} + 24y^{12} + \dots - 14y - 1)(y^{26} + 33y^{25} + \dots + 38147y + 3721)$ |
| c_3, c_7, c_{10} c_{11} | $(y^6 + 4y^5 + \dots + 11y + 9)(y^6 + 5y^5 + \dots + 2y + 1)$ $(y^{13} + 13y^{12} + \dots + 20y - 1)(y^{26} + 19y^{25} + \dots - y + 1)$ |
| c_4 | $(y^3 - y^2 - 2y - 1)^2(y^6 + 2y^5 + 11y^4 + 4y^3 + 15y^2 - 19y + 9)$ $(y^{13} - 3y^{12} + \dots + 456y - 16)$ $(-25 - 136y - 292y^2 - 217y^3 + 308y^4 + 1031y^5 + 1431y^6 + 1301y^7 + 867y^8 + 442y^9 + 172y^{10} + \dots)$ |
| c_6 | $(y^6 + y^5 + 11y^4 + 19y^2 - 6y + 1)(y^6 + 3y^5 + 2y^4 + y^2 + y + 1)$ $(y^{13} + 11y^{12} + \dots - 35y - 9)$ $(y^{26} + 20y^{25} + \dots + 9336774y + 1830609)$ |
| c_8 | $(y^6 + y^5 + 11y^4 + 19y^2 - 6y + 1)(y^6 + 3y^5 + 2y^4 + y^2 + y + 1)$ $(y^{13} + 11y^{12} + \dots - 35y - 9)$ $(y^{26} + 20y^{25} + \dots + 9336774y + 1830609)$ |
| c_9 | $(y^3 - y^2 - 2y - 1)^2(y^6 - 5y^5 + 6y^4 + 5y^2 + y + 1)$ $(-9 + 124y - 684y^2 + 2019y^3 - 3848y^4 + 4895y^5 - 2685y^6 + 1641y^7 - 2053y^8 + 1590y^9 - 66y^{10} + \dots)$ $(y^{13} - 14y^{12} + \dots + 732y - 144)$ |