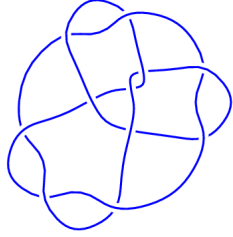
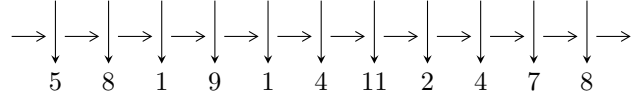


11n₁₆₉ (K11n₁₆₉)

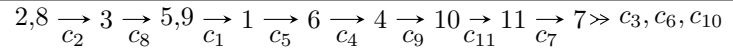


1

Arc Sequences



Solving Sequence



Representation Ideals

$$I = \bigcap_{i=1}^3 I_i^u$$

$$I_1^u = \langle a^{12} + 10a^{10} + 6a^9 + 31a^8 + 12a^7 + 41a^6 - 15a^5 - 2a^4 + 15a^3 + 42a^2 + 21a + 7, \\ - 6317a^{11} + 39893u + \dots - 215502a - 55601, \\ 14803708a^{11} + 104399981b + \dots + 217594097a - 61454022 \rangle$$

$$I_2^u = \langle u^8 + u^7 + 2u^6 - u^5 + u^4 - 3u^3 + u^2 - 2u + 1, u^5 + u^4 + u^3 - u^2 + b - 1, u^7 + u^6 + 3u^5 + u^4 + 3u^3 - 3u^2 -$$

$$I_3^u = \langle u^{13} - 8u^{12} + \dots + 56u - 8, \\ u^{12} - 6u^{11} + 18u^{10} - 38u^9 + 64u^8 - 91u^7 + 111u^6 - 114u^5 + 100u^4 - 77u^3 + 51u^2 + 8a - 28u + 12, \\ - u^{12} + 8u^{11} + \dots + 4b - 12 \rangle$$

There are 3 irreducible components with 33 representations.

¹The knot diagram image is adapter from “C. Livingston and A. H. Moore, KnotInfo: Table of Knot Invariants, <http://www.indiana.edu/~knotinfo>”

$$\mathbf{I. } I_1^u = \langle a^{12} + 10a^{10} + \dots + 21a + 7, -6317a^{11} + 39893u + \dots - 215502a - 55601, 1.04 \times 10^8 b + 1.48 \times 10^7 a^{11} + \dots + 2.18 \times 10^8 a - 6.15 \times 10^7 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} a \\ -0.141798a^{11} + 0.138802a^{10} + \dots - 2.08424a + 0.588640 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0.138802a^{11} - 0.0483084a^{10} + \dots + 3.56640a + 1.99259 \\ 0.199814a^{11} - 0.100324a^{10} + \dots + 3.55063a + 1.75075 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ 0.158349a^{11} - 0.0264207a^{10} + \dots + 5.40200a + 1.39375 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.141798a^{11} - 0.138802a^{10} + \dots + 3.08424a - 0.588640 \\ -0.141798a^{11} + 0.138802a^{10} + \dots - 2.08424a + 0.588640 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ 0.158349a^{11} - 0.0264207a^{10} + \dots + 5.40200a + 2.39375 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.158349a^{11} + 0.0264207a^{10} + \dots - 5.40200a - 1.39375 \\ 0.158349a^{11} - 0.0264207a^{10} + \dots + 5.40200a + 2.39375 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.146210a^{11} + 0.0393344a^{10} + \dots + 6.68400a + 2.97987 \\ 0.0703822a^{11} - 0.0839361a^{10} + \dots + 0.464569a - 0.752853 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -0.0135540a^{11} - 0.0157206a^{10} + \dots - 0.766309a - 0.245528 \\ -0.0448347a^{11} + 0.160873a^{10} + \dots + 1.31433a + 2.06632 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.170487a^{11} + 0.0921758a^{10} + \dots - 4.12000a + 0.192359 \\ 0.00740795a^{11} + 0.0876429a^{10} + \dots + 3.11760a + 0.987279 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.0314412a^{11} + 0.102271a^{10} + \dots + 0.0782103a + 2.18976 \\ 0.241434a^{11} - 0.158751a^{10} + \dots + 5.92854a + 1.42744 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.0314412a^{11} + 0.102271a^{10} + \dots + 0.0782103a + 2.18976 \\ 0.241434a^{11} - 0.158751a^{10} + \dots + 5.92854a + 1.42744 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.500000 + 0.866025I$ $a = -0.86942 - 1.28287I$ $b = 0.231240 - 1.394375I$	$4.22983 + 2.02988I$	$-12.00000 - 3.46410I$
$u = -0.500000 - 0.866025I$ $a = -0.86942 + 1.28287I$ $b = 0.231240 + 1.394375I$	$4.22983 - 2.02988I$	$-12.00000 + 3.46410I$
$u = -0.500000 + 0.866025I$ $a = -0.519247 - 0.520638I$ $b = -1.61068 - 0.71000I$	$-12.68949 + 2.02988I$	$-12.00000 - 3.46410I$
$u = -0.500000 - 0.866025I$ $a = -0.519247 + 0.520638I$ $b = -1.61068 + 0.71000I$	$-12.68949 - 2.02988I$	$-12.00000 + 3.46410I$
$u = -0.500000 - 0.866025I$ $a = -0.281671 - 0.395754I$ $b = 0.763411 + 0.046058I$	$-1.40994 - 2.02988I$	$-12.00000 + 3.46410I$
$u = -0.500000 + 0.866025I$ $a = -0.281671 + 0.395754I$ $b = 0.763411 - 0.046058I$	$-1.40994 + 2.02988I$	$-12.00000 - 3.46410I$
$u = -0.500000 - 0.866025I$ $a = 0.28167 - 1.76408I$ $b = -0.139922 - 1.125974I$	$-1.40994 - 2.02988I$	$-12.00000 + 3.46410I$
$u = -0.500000 + 0.866025I$ $a = 0.28167 + 1.76408I$ $b = -0.139922 + 1.125974I$	$-1.40994 + 2.02988I$	$-12.00000 - 3.46410I$
$u = -0.500000 + 0.866025I$ $a = 0.51925 - 2.60041I$ $b = 0.709707 - 0.850523I$	$-12.68949 + 2.02988I$	$-12.00000 - 3.46410I$
$u = -0.500000 - 0.866025I$ $a = 0.51925 + 2.60041I$ $b = 0.709707 + 0.850523I$	$-12.68949 - 2.02988I$	$-12.00000 + 3.46410I$

Solution to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.500000 - 0.866025I$ $a = 0.869423 - 0.512030I$ $b = -0.453761 - 1.008958I$	$4.22983 - 2.02988I$	$-12.00000 + 3.46410I$
$u = -0.500000 + 0.866025I$ $a = 0.869423 + 0.512030I$ $b = -0.453761 + 1.008958I$	$4.22983 + 2.02988I$	$-12.00000 - 3.46410I$

$$\text{II. } I_2^u = \langle u^8 + u^7 + 2u^6 - u^5 + u^4 - 3u^3 + u^2 - 2u + 1, u^5 + u^4 + u^3 - u^2 + b - 1, u^7 + u^6 + 3u^5 + u^4 + 3u^3 - 3u^2 + a - 3 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_2 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -u^7 - u^6 - 3u^5 - u^4 - 3u^3 + 3u^2 + 3 \\ -u^5 - u^4 - u^3 + u^2 + 1 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -2u^7 - 3u^6 - 5u^5 - u^3 + 5u^2 + u + 3 \\ -u^7 - u^6 - 2u^5 + u^4 - u^3 + 3u^2 - u + 1 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_9 &= \begin{pmatrix} -u^7 - u^6 - 2u^5 - 2u^3 + 2u^2 + 2 \\ -u^5 - u^4 - u^3 + u^2 + 1 \end{pmatrix} \\ a_1 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -u \\ u^3 + u \end{pmatrix} \\ a_4 &= \begin{pmatrix} -u^7 - 2u^6 - 3u^5 - u^4 + 2u^2 + 2u + 1 \\ -u^7 - u^6 - 2u^5 + u^4 - u^3 + 3u^2 + 1 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -2u^7 - 3u^6 - 5u^5 - 2u^3 + 4u^2 + 4 \\ -u^7 - 2u^6 - 3u^5 - u^4 - u^3 + 2u^2 + u + 2 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 3u^7 + 4u^6 + 7u^5 - u^4 + 2u^3 - 7u^2 + u - 4 \\ u^7 + u^6 + 2u^5 - u^4 + u^3 - 3u^2 + u - 2 \end{pmatrix} \\ a_7 &= \begin{pmatrix} u^7 + 2u^6 + 4u^5 + 2u^4 + 2u^3 - 3u^2 - 2u - 4 \\ u^7 + 2u^6 + 3u^5 + u^4 + u^3 - 2u^2 - u - 2 \end{pmatrix} \\ a_7 &= \begin{pmatrix} u^7 + 2u^6 + 4u^5 + 2u^4 + 2u^3 - 3u^2 - 2u - 4 \\ u^7 + 2u^6 + 3u^5 + u^4 + u^3 - 2u^2 - u - 2 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.95744 - 1.12705I$ $a = 0.508528 - 0.793604I$ $b = -0.211625 - 1.217615I$	$1.24083 - 3.75870I$	$-10.69968 + 3.38204I$
$u = -0.95744 + 1.12705I$ $a = 0.508528 + 0.793604I$ $b = -0.211625 + 1.217615I$	$1.24083 + 3.75870I$	$-10.69968 - 3.38204I$
$u = -0.404913 - 1.017878I$ $a = -0.792580 + 1.098412I$ $b = 0.350924 + 1.208539I$	$5.21920 - 1.77211I$	$-2.23409 + 0.85548I$
$u = -0.404913 + 1.017878I$ $a = -0.792580 - 1.098412I$ $b = 0.350924 - 1.208539I$	$5.21920 + 1.77211I$	$-2.23409 - 0.85548I$
$u = 0.163169 - 0.915412I$ $a = 0.48888 - 1.77230I$ $b = -0.511162 - 1.035647I$	$-0.155635 + 0.787051I$	$-8.59786 + 1.33483I$
$u = 0.163169 + 0.915412I$ $a = 0.48888 + 1.77230I$ $b = -0.511162 + 1.035647I$	$-0.155635 - 0.787051I$	$-8.59786 - 1.33483I$
$u = 0.479751$ $a = 3.21196$ $b = 1.04135$	-12.9150	-12.7749
$u = 0.918626$ $a = -0.621620$ $b = -0.297628$	-2.98361	-12.1618

$$\text{III. } I_3^u = \langle u^{13} - 8u^{12} + \dots + 56u - 8, u^{12} - 6u^{11} + \dots + 8a + 12, -u^{12} + 8u^{11} + \dots + 4b - 12 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_2 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -\frac{1}{8}u^{12} + \frac{3}{4}u^{11} + \dots + \frac{7}{2}u - \frac{3}{2} \\ \frac{1}{4}u^{12} - 2u^{11} + \dots - \frac{33}{2}u + 3 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -\frac{1}{4}u^{12} + \frac{3}{2}u^{11} + \dots + \frac{3}{2}u + \frac{1}{2} \\ -\frac{1}{2}u^{11} + 3u^{10} + \dots - \frac{23}{2}u + 2 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_9 &= \begin{pmatrix} -\frac{3}{8}u^{12} + \frac{11}{4}u^{11} + \dots + 20u - \frac{9}{2} \\ \frac{1}{4}u^{12} - 2u^{11} + \dots - \frac{33}{2}u + 3 \end{pmatrix} \\ a_1 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -u \\ u^3 + u \end{pmatrix} \\ a_4 &= \begin{pmatrix} \frac{1}{4}u^{12} - 2u^{11} + \dots - 13u + \frac{5}{2} \\ \frac{1}{2}u^{11} - 3u^{10} + \dots + \frac{25}{2}u - 2 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} \frac{1}{4}u^{12} - \frac{5}{4}u^{11} + \dots + \frac{55}{4}u - 4 \\ -\frac{3}{4}u^{12} + \frac{11}{2}u^{11} + \dots + 29u - 4 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} \frac{1}{4}u^{12} - 2u^{11} + \dots - 14u + \frac{7}{2} \\ \frac{1}{2}u^{12} - \frac{7}{2}u^{11} + \dots - \frac{29}{2}u + 2 \end{pmatrix} \\ a_7 &= \begin{pmatrix} u^{12} - \frac{27}{4}u^{11} + \dots - \frac{73}{4}u + 2 \\ -\frac{3}{4}u^{12} + \frac{11}{2}u^{11} + \dots + 29u - 4 \end{pmatrix} \\ a_7 &= \begin{pmatrix} u^{12} - \frac{27}{4}u^{11} + \dots - \frac{73}{4}u + 2 \\ -\frac{3}{4}u^{12} + \frac{11}{2}u^{11} + \dots + 29u - 4 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.326542 - 1.020095I$ $a = -0.174135 - 1.155087I$ $b = 0.329129 - 0.671341I$	$-1.07131 - 1.81105I$	$-12.48073 + 2.50977I$
$u = -0.326542 + 1.020095I$ $a = -0.174135 + 1.155087I$ $b = 0.329129 + 0.671341I$	$-1.07131 + 1.81105I$	$-12.48073 - 2.50977I$
$u = 0.270743 - 1.206069I$ $a = 0.134462 + 1.126172I$ $b = -0.598666 + 0.794370I$	$2.89440 + 2.21633I$	$-9.35734 - 3.25180I$
$u = 0.270743 + 1.206069I$ $a = 0.134462 - 1.126172I$ $b = -0.598666 - 0.794370I$	$2.89440 - 2.21633I$	$-9.35734 + 3.25180I$
$u = 0.325158$ $a = -0.805865$ $b = 0.388289$	-0.575325	-17.2598
$u = 0.63465 - 1.27236I$ $a = -0.131915 - 1.240229I$ $b = 0.796089 - 1.077434I$	$-0.15730 + 7.29804I$	$-11.37128 - 6.48312I$
$u = 0.63465 + 1.27236I$ $a = -0.131915 + 1.240229I$ $b = 0.796089 + 1.077434I$	$-0.15730 - 7.29804I$	$-11.37128 + 6.48312I$
$u = 0.83155 - 1.23498I$ $a = 0.21318 + 1.40057I$ $b = -0.92331 + 1.41816I$	$-10.0617 + 10.8173I$	$-12.24076 - 5.20880I$
$u = 0.83155 + 1.23498I$ $a = 0.21318 - 1.40057I$ $b = -0.92331 - 1.41816I$	$-10.0617 - 10.8173I$	$-12.24076 + 5.20880I$
$u = 1.161483 - 0.385396I$ $a = -0.259148 - 0.010479I$ $b = -0.475687 - 0.592166I$	$-3.17225 - 0.94602I$	$-12.22572 + 6.14642I$

Solution to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.161483 + 0.385396I$	$-3.17225 + 0.94602I$	$-12.22572 - 6.14642I$
$a = -0.259148 + 0.010479I$		
$b = -0.475687 + 0.592166I$		
$u = 1.26554 - 0.69993I$	$-11.99574 - 3.34885I$	$-12.69425 + 2.28469I$
$a = 0.620492 + 0.189125I$		
$b = 0.678296 + 1.053703I$		
$u = 1.26554 + 0.69993I$	$-11.99574 + 3.34885I$	$-12.69425 - 2.28469I$
$a = 0.620492 - 0.189125I$		
$b = 0.678296 - 1.053703I$		

IV. u-Polynomials

Crossings	u-Polynomials at each crossings
c_1	$(u^2 - u + 1)^6(u^8 + u^7 + 2u^6 - u^5 + u^4 - 3u^3 + u^2 - 2u + 1)$ $(u^{13} + 8u^{12} + \dots + 56u + 8)$
c_2, c_9	$(u^8 + 3u^6 + \dots - 3u - 1)(u^{12} + u^{11} + \dots - 14u + 7)$ $(u^{13} + 3u^{11} + \dots + 2u - 1)$
c_3, c_6	$(u^8 + 2u^7 + \dots - u + 1)(u^{12} + u^{11} + \dots + 56u + 13)$ $(u^{13} + 2u^{12} + \dots - 4u - 1)$
c_4, c_8	$(u^8 + 3u^6 + \dots + 3u - 1)(u^{12} + u^{11} + \dots - 14u + 7)$ $(u^{13} + 3u^{11} + \dots + 2u - 1)$
c_5	$(u^2 - u + 1)^6(u^8 - u^7 + 2u^6 + u^5 + u^4 + 3u^3 + u^2 + 2u + 1)$ $(u^{13} + 8u^{12} + \dots + 56u + 8)$
c_7	$(u^3 - u^2 - 2u + 1)^4(u^8 + u^7 - 5u^6 - 4u^5 + 8u^4 + 5u^3 - 3u^2 - u - 1)$ $(u^{13} + 6u^{12} + \dots + 14u + 4)$
c_{10}, c_{11}	$(u^3 - u^2 - 2u + 1)^4(u^8 - u^7 - 5u^6 + 4u^5 + 8u^4 - 5u^3 - 3u^2 + u - 1)$ $(u^{13} + 6u^{12} + \dots + 14u + 4)$

V. Riley Polynomials

Crossings	Riley Polynomials at each crossings
c_1, c_5	$(y^2 + y + 1)^6(y^8 + 3y^7 + 8y^6 + 11y^5 + 5y^4 - 7y^3 - 9y^2 - 2y + 1)$ $(y^{13} + 4y^{12} + \dots + 480y - 64)$
c_2, c_4, c_8 c_9	$(y^8 + 6y^7 + 15y^6 + 17y^5 + y^4 - 21y^3 - 24y^2 - 9y + 1)$ $(y^{12} + 3y^{11} + \dots - 140y^2 + 49)(y^{13} + 6y^{12} + \dots + 2y - 1)$
c_3, c_6	$(y^8 - 2y^7 - 9y^6 - 7y^5 + 5y^4 + 11y^3 + 8y^2 + 3y + 1)$ $(y^{12} - 13y^{11} + \dots - 432y + 169)(y^{13} - 26y^{12} + \dots + 42y - 1)$
c_7, c_{10}, c_{11}	$(y^3 - 5y^2 + 6y - 1)^4$ $(y^8 - 11y^7 + 49y^6 - 112y^5 + 134y^4 - 71y^3 + 3y^2 + 5y + 1)$ $(y^{13} - 16y^{12} + \dots + 204y - 16)$