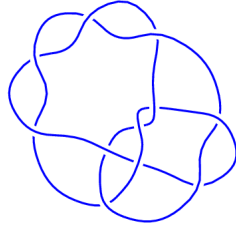
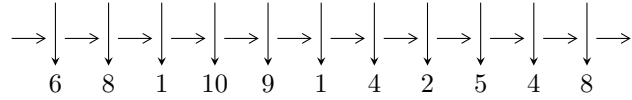


11n₁₈₁ (K11n₁₈₁)

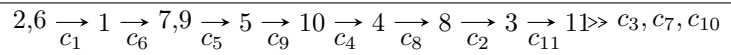


1

Arc Sequences



Solving Sequence



Representation Ideals

$$I = \bigcap_{i=1}^3 I_i^u$$

$$I_1^u = \langle u^7 + 2u^5 + u^4 + u^3 + u^2 - u - 1, b + u, u^6 - u^5 + 3u^4 - u^3 + 2u^2 + a - 1 \rangle$$

$$I_2^u = \langle u^{13} + 5u^{11} - u^{10} + 15u^9 - 3u^8 + 23u^7 - 4u^6 + 22u^5 - 3u^4 + 10u^3 - 2u^2 + 2u - 1, b + u, -57u^{12} - 33u^{11} + \dots + 64a + 47 \rangle$$

$$I_3^u = \langle u^{16} + u^{15} + \dots + 22u + 31, -3020100992u^{15} + 17915450451u^{14} + \dots + 339868204009b + 273458732915, -756017073639u^{15} - 1082850030952u^{14} + \dots + 10535914324279a - 12506104179146 \rangle$$

There are 3 irreducible components with 36 representations.

¹The knot diagram image is adapter from “C. Livingston and A. H. Moore, KnotInfo: Table of Knot Invariants, <http://www.indiana.edu/~knotinfo>”

$$I_1^u = \langle u^7 + 2u^5 + u^4 + u^3 + u^2 - u - 1, b + u, u^6 - u^5 + 3u^4 - u^3 + 2u^2 + a - 1 \rangle \quad \mathbf{I.}$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^6 + u^5 - 3u^4 + u^3 - 2u^2 + 1 \\ -u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^6 - 2u^4 - u^3 - u + 2 \\ u^6 + 2u^4 + u^2 + u - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^6 - u^5 + 3u^4 - u^3 + 2u^2 - 2 \\ -u^6 - 3u^4 - 2u^2 + 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^6 + u^5 - 2u^4 + u^3 - u^2 + 1 \\ u^4 + 2u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^6 + u^5 - 3u^4 + u^3 - 2u^2 - u + 1 \\ -u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^6 + u^5 - 2u^4 + u^3 + 2 \\ u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^6 - u^5 + 3u^4 - 2u^3 + 2u^2 - u - 1 \\ -u^2 - 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^6 - u^5 + 3u^4 - 2u^3 + 2u^2 - u - 1 \\ -u^2 - 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.684504 - 0.212754I$ $a = -0.33756 - 1.93236I$ $b = 0.684504 + 0.212754I$	$0.58425 + 1.95701I$	$-10.82069 - 1.34837I$
$u = -0.684504 + 0.212754I$ $a = -0.33756 + 1.93236I$ $b = 0.684504 - 0.212754I$	$0.58425 - 1.95701I$	$-10.82069 + 1.34837I$
$u = -0.192319 - 1.190842I$ $a = -0.587751 + 0.132804I$ $b = 0.192319 + 1.190842I$	$4.79738 - 0.94912I$	$-1.21872 + 0.82233I$
$u = -0.192319 + 1.190842I$ $a = -0.587751 - 0.132804I$ $b = 0.192319 - 1.190842I$	$4.79738 + 0.94912I$	$-1.21872 - 0.82233I$
$u = 0.511889 - 1.253215I$ $a = 1.161310 - 0.409623I$ $b = -0.511889 + 1.253215I$	$13.16474 + 2.34118I$	$-0.965786 - 0.952471I$
$u = 0.511889 + 1.253215I$ $a = 1.161310 + 0.409623I$ $b = -0.511889 - 1.253215I$	$13.16474 - 2.34118I$	$-0.965786 + 0.952471I$
$u = 0.729869$ $a = -0.471993$ $b = -0.729869$	-4.19405	-9.98962

$$\text{II. } I_2^u = \langle u^{13} + 5u^{11} + \dots + 2u - 1, b + u, -57u^{12} - 33u^{11} + \dots + 64a + 47 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.890625u^{12} + 0.515625u^{11} + \dots + 1.10938u - 0.734375 \\ -u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -0.406250u^{12} + 0.343750u^{11} + \dots + 4.40625u - 1.15625 \\ -0.140625u^{12} + 0.234375u^{11} + \dots + 1.14063u - 0.515625 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -0.531250u^{12} - 0.781250u^{11} + \dots + 1.53125u + 0.718750 \\ 0.0468750u^{12} - 0.0781250u^{11} + \dots - 0.0468750u + 0.171875 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -\frac{3}{4}u^{12} - \frac{3}{4}u^{11} + \dots + \frac{11}{4}u + \frac{1}{4} \\ -0.0156250u^{12} - 0.640625u^{11} + \dots - 0.984375u + 0.609375 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0.890625u^{12} + 0.515625u^{11} + \dots + 0.109375u - 0.734375 \\ -u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -0.515625u^{12} - 0.140625u^{11} + \dots + 2.51563u + 0.109375 \\ u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.296875u^{12} - 1.17188u^{11} + \dots - 1.70313u + 2.57813 \\ -0.234375u^{12} - 0.609375u^{11} + \dots + 0.234375u + 0.140625 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.296875u^{12} - 1.17188u^{11} + \dots - 1.70313u + 2.57813 \\ -0.234375u^{12} - 0.609375u^{11} + \dots + 0.234375u + 0.140625 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.76994 - 1.47811I$ $a = -0.931114 - 0.335072I$ $b = 0.76994 + 1.47811I$	$6.50636 - 11.34500I$	$-6.41522 + 5.59283I$
$u = -0.76994 + 1.47811I$ $a = -0.931114 + 0.335072I$ $b = 0.76994 - 1.47811I$	$6.50636 + 11.34500I$	$-6.41522 - 5.59283I$
$u = -0.454277 - 1.006096I$ $a = -0.093987 + 0.805953I$ $b = 0.454277 + 1.006096I$	$-3.02361 - 2.70878I$	$-9.87229 + 2.50117I$
$u = -0.454277 + 1.006096I$ $a = -0.093987 - 0.805953I$ $b = 0.454277 - 1.006096I$	$-3.02361 + 2.70878I$	$-9.87229 - 2.50117I$
$u = -0.345858 - 0.592455I$ $a = -1.35097 - 0.54415I$ $b = 0.345858 + 0.592455I$	$2.39689 - 1.47210I$	$-6.76905 + 4.68228I$
$u = -0.345858 + 0.592455I$ $a = -1.35097 + 0.54415I$ $b = 0.345858 - 0.592455I$	$2.39689 + 1.47210I$	$-6.76905 - 4.68228I$
$u = 0.150630 - 0.774375I$ $a = -1.54813 + 0.76688I$ $b = -0.150630 + 0.774375I$	$1.92199 - 1.66881I$	$-4.76442 + 0.86409I$
$u = 0.150630 + 0.774375I$ $a = -1.54813 - 0.76688I$ $b = -0.150630 - 0.774375I$	$1.92199 + 1.66881I$	$-4.76442 - 0.86409I$
$u = 0.356605$ $a = 0.881921$ $b = -0.356605$	-0.542082	-18.2828
$u = 0.589560 - 1.048774I$ $a = 1.26834 - 0.65193I$ $b = -0.589560 + 1.048774I$	$12.09747 + 2.52656I$	$-9.24277 - 2.75851I$

Solution to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.589560 + 1.048774I$ $a = 1.26834 + 0.65193I$ $b = -0.589560 - 1.048774I$	$12.09747 - 2.52656I$	$-9.24277 + 2.75851I$
$u = 0.651583 - 1.236761I$ $a = 0.714908 + 0.187738I$ $b = -0.651583 + 1.236761I$	$-1.53379 + 7.84030I$	$-8.79484 - 6.42108I$
$u = 0.651583 + 1.236761I$ $a = 0.714908 - 0.187738I$ $b = -0.651583 - 1.236761I$	$-1.53379 - 7.84030I$	$-8.79484 + 6.42108I$

$$\text{III. } I_3^u = \langle u^{16} + u^{15} + \dots + 22u + 31, -3.02 \times 10^9 u^{15} + 1.79 \times 10^{10} u^{14} + \dots + 3.40 \times 10^{11} b + 2.73 \times 10^{11}, -7.56 \times 10^{11} u^{15} - 1.08 \times 10^{12} u^{14} + \dots + 1.05 \times 10^{13} a - 1.25 \times 10^{13} \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.0717562u^{15} + 0.102777u^{14} + \dots + 2.64959u + 1.18700 \\ 0.00888609u^{15} - 0.0527129u^{14} + \dots - 0.917073u - 0.804602 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -0.0456383u^{15} + 0.00210365u^{14} + \dots + 1.00937u + 1.43837 \\ 0.0466726u^{15} - 0.00819680u^{14} + \dots + 0.200327u - 2.32362 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -0.0311097u^{15} - 0.0880219u^{14} + \dots - 2.05895u - 0.233069 \\ 0.0214961u^{15} + 0.0759945u^{14} + \dots + 1.14894u + 1.31477 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.0372499u^{15} + 0.0153993u^{14} + \dots + 0.787082u - 1.68262 \\ -0.00152993u^{15} - 0.0806813u^{14} + \dots - 0.717701u - 2.17728 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0.0806423u^{15} + 0.0500641u^{14} + \dots + 1.73252u + 0.382395 \\ 0.00888609u^{15} - 0.0527129u^{14} + \dots - 0.917073u - 0.804602 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0.00667175u^{15} - 0.107263u^{14} + \dots - 0.604653u - 3.18254 \\ -0.0682838u^{15} - 0.228891u^{14} + \dots - 3.69147u - 5.03188 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.0372499u^{15} - 0.0153993u^{14} + \dots - 0.787082u + 1.68262 \\ 0.0305782u^{15} + 0.122662u^{14} + \dots + 1.39174u + 1.49991 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.0372499u^{15} - 0.0153993u^{14} + \dots - 0.787082u + 1.68262 \\ 0.0305782u^{15} + 0.122662u^{14} + \dots + 1.39174u + 1.49991 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.55524 - 0.42761I$		
$a = -0.192476 - 0.945314I$	$2.84290 + 3.16396I$	$-6.17326 - 2.56480I$
$b = -0.176984 + 1.046895I$		
$u = -1.55524 + 0.42761I$		
$a = -0.192476 + 0.945314I$	$2.84290 - 3.16396I$	$-6.17326 + 2.56480I$
$b = -0.176984 - 1.046895I$		
$u = -0.589780 - 0.682901I$		
$a = 0.711330 + 0.035736I$	$-4.15885 - 1.41510I$	$-9.82674 + 4.90874I$
$b = -1.159017 + 0.482637I$		
$u = -0.589780 + 0.682901I$		
$a = 0.711330 - 0.035736I$	$-4.15885 + 1.41510I$	$-9.82674 - 4.90874I$
$b = -1.159017 - 0.482637I$		
$u = -0.309677 - 0.918028I$		
$a = 0.626050 - 0.219220I$	$3.73684 - 1.41510I$	$-9.82674 + 4.90874I$
$b = -0.092247 - 1.363224I$		
$u = -0.309677 + 0.918028I$		
$a = 0.626050 + 0.219220I$	$3.73684 + 1.41510I$	$-9.82674 - 4.90874I$
$b = -0.092247 + 1.363224I$		
$u = -0.26048 - 1.62229I$		
$a = 0.943043 + 0.086771I$	$10.73858 - 3.16396I$	$-6.17326 + 2.56480I$
$b = -0.786926 - 1.059081I$		
$u = -0.26048 + 1.62229I$		
$a = 0.943043 - 0.086771I$	$10.73858 + 3.16396I$	$-6.17326 - 2.56480I$
$b = -0.786926 + 1.059081I$		
$u = 0.092247 - 1.363224I$		
$a = -0.389627 - 0.263479I$	$3.73684 + 1.41510I$	$-9.82674 - 4.90874I$
$b = 0.309677 - 0.918028I$		
$u = 0.092247 + 1.363224I$		
$a = -0.389627 + 0.263479I$	$3.73684 - 1.41510I$	$-9.82674 + 4.90874I$
$b = 0.309677 + 0.918028I$		

Solution to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.176984 - 1.046895I$ $a = -1.45821 + 0.14634I$ $b = 1.55524 + 0.42761I$	$2.84290 + 3.16396I$	$-6.17326 - 2.56480I$
$u = 0.176984 + 1.046895I$ $a = -1.45821 - 0.14634I$ $b = 1.55524 - 0.42761I$	$2.84290 - 3.16396I$	$-6.17326 + 2.56480I$
$u = 0.786926 - 1.059081I$ $a = -0.991866 + 0.637958I$ $b = 0.26048 - 1.62229I$	$10.73858 + 3.16396I$	$-6.17326 - 2.56480I$
$u = 0.786926 + 1.059081I$ $a = -0.991866 - 0.637958I$ $b = 0.26048 + 1.62229I$	$10.73858 - 3.16396I$	$-6.17326 + 2.56480I$
$u = 1.159017 - 0.482637I$ $a = -0.135341 - 0.493664I$ $b = 0.589780 + 0.682901I$	$-4.15885 - 1.41510I$	$-9.82674 + 4.90874I$
$u = 1.159017 + 0.482637I$ $a = -0.135341 + 0.493664I$ $b = 0.589780 - 0.682901I$	$-4.15885 + 1.41510I$	$-9.82674 - 4.90874I$

IV. u-Polynomials

Crossings	u-Polynomials at each crossings
c_1, c_8	$(u^7 + 2u^5 + \dots - u - 1)(u^{13} + 5u^{11} + \dots + 2u - 1)$ $(u^{16} + u^{15} + \dots + 22u + 31)$
c_2, c_6	$(u^7 + 2u^5 + \dots - u + 1)(u^{13} + 5u^{11} + \dots + 2u - 1)$ $(u^{16} + u^{15} + \dots + 22u + 31)$
c_3	$(u^2 - u - 1)^8(u^7 + 3u^6 + 3u^5 + 4u^4 + 6u^3 + u^2 - u + 2)$ $(u^{13} + 12u^{12} + \dots - 16u - 16)$
c_4, c_5	$(u^4 - u^3 + 3u^2 - 2u + 1)^4(u^7 + 5u^5 + 7u^3 + 2u - 1)$ $(u^{13} + 5u^{12} + \dots + 30u + 4)$
c_7, c_{11}	$(u^7 - u^6 + \dots + 2u^2 + 1)(u^{13} + u^{12} + \dots + 3u + 1)$ $(u^{16} + u^{15} + \dots - 48u + 19)$
c_9, c_{10}	$(u^4 - u^3 + 3u^2 - 2u + 1)^4(u^7 + 5u^5 + 7u^3 + 2u + 1)$ $(u^{13} + 5u^{12} + \dots + 30u + 4)$

V. Riley Polynomials

Crossings	Riley Polynomials at each crossings
c_1, c_2, c_6 c_8	$(y^7 + 4y^6 + \dots + 3y - 1)(y^{13} + 10y^{12} + \dots + 30y^2 - 1)$ $(y^{16} + 7y^{15} + \dots + 4104y + 961)$
c_3	$(y^2 - 3y + 1)^8(y^7 - 3y^6 - 3y^5 + 12y^4 + 10y^3 - 29y^2 - 3y - 4)$ $(y^{13} - 6y^{12} + \dots + 4480y - 256)$
c_4, c_5, c_9 c_{10}	$(y^4 + 5y^3 + 7y^2 + 2y + 1)^4$ $(y^7 + 10y^6 + 39y^5 + 74y^4 + 69y^3 + 28y^2 + 4y - 1)$ $(y^{13} + 15y^{12} + \dots + 124y - 16)$
c_7, c_{11}	$(y^7 - 3y^6 + \dots - 4y - 1)(y^{13} - 17y^{12} + \dots + 25y - 1)$ $(y^{16} - 9y^{15} + \dots - 4356y + 361)$