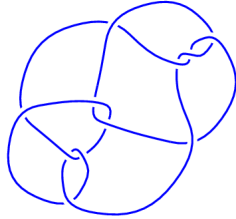
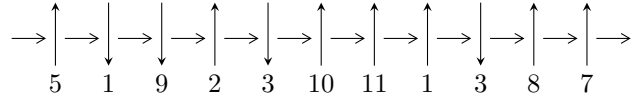


11n₂₀ (K11n₂₀)

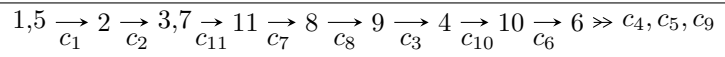


1

Arc Sequences



Solving Sequence



Representation Ideals

$$I = \bigcap_{i=1}^2 I_i^u$$

$$I_1^u = \langle a^6 + 7a^5 + 19a^4 + 26a^3 + 22a^2 + 15a + 7, a^5 + 4a^4 + 7a^3 + 10a^2 + 5b + 12a + 4, 2a^5 + 13a^4 + 29a^3 + 30a^2 + 24a + 5u + 18 \rangle$$

$$I_2^u = \langle u^{17} + 4u^{16} + \dots + 3u + 1, -u^{16} - 3u^{15} - 5u^{14} - 4u^{13} - 7u^{12} - 10u^{11} - 10u^{10} - 7u^8 - 8u^7 - 3u^6 + 3u^5 - 5u^4 + 10u^2 + 4a - 9u + 4, u^{16} + 4u^{15} + \dots + 4b + 1 \rangle$$

There are 2 irreducible components with 23 representations.

¹The knot diagram image is adapter from “C. Livingston and A. H. Moore, KnotInfo: Table of Knot Invariants, <http://www.indiana.edu/~knotinfo>”

$$\mathbf{I. } I_1^u = \langle a^6 + 7a^5 + 19a^4 + 26a^3 + 22a^2 + 15a + 7, a^5 + 4a^4 + 7a^3 + 10a^2 + 5b + 12a + 4, 2a^5 + 13a^4 + 29a^3 + 30a^2 + 24a + 5u + 18 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ -\frac{2}{5}a^5 - \frac{13}{5}a^4 + \dots - \frac{24}{5}a - \frac{18}{5} \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -\frac{2}{5}a^5 - \frac{13}{5}a^4 + \dots - \frac{24}{5}a - \frac{13}{5} \end{pmatrix}$$

$$a_3 = \begin{pmatrix} \frac{2}{5}a^5 + \frac{13}{5}a^4 + \dots + \frac{24}{5}a + \frac{18}{5} \\ -\frac{2}{5}a^5 - \frac{13}{5}a^4 + \dots - \frac{24}{5}a - \frac{13}{5} \end{pmatrix}$$

$$a_7 = \begin{pmatrix} a \\ -\frac{1}{5}a^5 - \frac{4}{5}a^4 + \dots - \frac{12}{5}a - \frac{4}{5} \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} \frac{3}{5}a^5 + \frac{12}{5}a^4 + \dots + \frac{11}{5}a + \frac{12}{5} \\ -\frac{2}{5}a^5 - \frac{8}{5}a^4 + \dots - \frac{9}{5}a - \frac{8}{5} \end{pmatrix}$$

$$a_8 = \begin{pmatrix} a^5 + 5a^4 + 8a^3 + 5a^2 + 3a + 2 \\ -\frac{1}{5}a^5 - \frac{4}{5}a^4 + \dots + \frac{3}{5}a + \frac{1}{5} \end{pmatrix}$$

$$a_9 = \begin{pmatrix} \frac{4}{5}a^5 + \frac{21}{5}a^4 + \dots + \frac{18}{5}a + \frac{11}{5} \\ -\frac{1}{5}a^5 - \frac{4}{5}a^4 + \dots + \frac{3}{5}a + \frac{1}{5} \end{pmatrix}$$

$$a_4 = \begin{pmatrix} \frac{2}{5}a^5 + \frac{13}{5}a^4 + \dots + \frac{24}{5}a + \frac{18}{5} \\ -\frac{2}{5}a^5 - \frac{13}{5}a^4 + \dots - \frac{24}{5}a - \frac{13}{5} \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} \frac{4}{5}a^5 + \frac{21}{5}a^4 + \dots + \frac{18}{5}a + \frac{11}{5} \\ -\frac{1}{5}a^5 - \frac{4}{5}a^4 + \dots + \frac{3}{5}a + \frac{1}{5} \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.500000 - 0.866025I$		
$a = -2.23956 - 0.46731I$	$-3.02413 + 4.85801I$	$-1.45566 - 6.64456I$
$b = 0.215080 + 1.307141I$		
$u = -0.500000 + 0.866025I$		
$a = -2.23956 + 0.46731I$	$-3.02413 - 4.85801I$	$-1.45566 + 6.64456I$
$b = 0.215080 - 1.307141I$		
$u = -0.500000 + 0.866025I$		
$a = -1.284920 - 0.493496I$	$1.11345 - 2.02988I$	$5.85715 + 4.49037I$
$b = 0.569840$		
$u = -0.500000 - 0.866025I$		
$a = -1.284920 + 0.493496I$	$1.11345 + 2.02988I$	$5.85715 - 4.49037I$
$b = 0.569840$		
$u = -0.500000 + 0.866025I$		
$a = 0.024478 - 0.839835I$	$-3.02413 + 0.79824I$	$2.09851 + 0.12339I$
$b = 0.215080 + 1.307141I$		
$u = -0.500000 - 0.866025I$		
$a = 0.024478 + 0.839835I$	$-3.02413 - 0.79824I$	$2.09851 - 0.12339I$
$b = 0.215080 - 1.307141I$		

II.

$$I_2^u = \langle u^{17} + 4u^{16} + \dots + 3u + 1, -u^{16} - 3u^{15} + \dots + 4a + 4, u^{16} + 4u^{15} + \dots + 4b + 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} \frac{1}{4}u^{16} + \frac{3}{4}u^{15} + \dots + \frac{9}{4}u - 1 \\ -\frac{1}{4}u^{16} - u^{15} + \dots - \frac{3}{4}u - \frac{1}{4} \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} \frac{1}{4}u^{16} + \frac{7}{4}u^{15} + \dots + \frac{11}{4}u + \frac{5}{2} \\ \frac{3}{4}u^{16} + \frac{9}{4}u^{15} + \dots + 2u^2 + \frac{5}{4}u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -\frac{11}{4}u^{16} - \frac{39}{4}u^{15} + \dots - \frac{27}{4}u - 4 \\ u^{16} + \frac{15}{4}u^{15} + \dots + 3u + \frac{7}{4} \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -\frac{7}{4}u^{16} - 6u^{15} + \dots - \frac{15}{4}u - \frac{9}{4} \\ u^{16} + \frac{15}{4}u^{15} + \dots + 3u + \frac{7}{4} \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ -u^3 - u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -\frac{13}{4}u^{16} - 10u^{15} + \dots - \frac{25}{4}u - \frac{15}{4} \\ 2u^{16} + \frac{25}{4}u^{15} + \dots + 4u + \frac{9}{4} \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^5 - 2u^3 - u \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^5 - 2u^3 - u \\ u^5 + u^3 + u \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.09163 - 0.95076I$ $a = 0.96960 - 1.67272I$ $b = -0.55805 + 1.32231I$	$11.91545 - 1.84478I$	$3.96952 + 0.75367I$
$u = -1.09163 + 0.95076I$ $a = 0.96960 + 1.67272I$ $b = -0.55805 - 1.32231I$	$11.91545 + 1.84478I$	$3.96952 - 0.75367I$
$u = -1.05476 - 1.04416I$ $a = 2.07888 - 0.43065I$ $b = -1.052716 - 0.047013I$	$15.8539 + 3.8626I$	$6.39661 - 2.12816I$
$u = -1.05476 + 1.04416I$ $a = 2.07888 + 0.43065I$ $b = -1.052716 + 0.047013I$	$15.8539 - 3.8626I$	$6.39661 + 2.12816I$
$u = -0.97902 - 1.09233I$ $a = 2.11700 + 1.07061I$ $b = -0.50759 - 1.37481I$	$11.4057 + 9.4106I$	$3.33658 - 4.76975I$
$u = -0.97902 + 1.09233I$ $a = 2.11700 - 1.07061I$ $b = -0.50759 + 1.37481I$	$11.4057 - 9.4106I$	$3.33658 + 4.76975I$
$u = -0.509232 - 0.371578I$ $a = -2.67025 - 1.66568I$ $b = 0.281522 + 1.323870I$	$-2.51924 + 3.59257I$	$1.69678 - 1.62034I$
$u = -0.509232 + 0.371578I$ $a = -2.67025 + 1.66568I$ $b = 0.281522 - 1.323870I$	$-2.51924 - 3.59257I$	$1.69678 + 1.62034I$
$u = -0.494210$ $a = -2.62173$ $b = 0.710942$	1.69761	6.54343
$u = 0.045204 - 0.831305I$ $a = 0.842729 - 0.566333I$ $b = 0.095288 - 1.269798I$	$-4.44298 - 1.97657I$	$-3.41444 + 3.62302I$

Solution to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.045204 + 0.831305I$ $a = 0.842729 + 0.566333I$ $b = 0.095288 + 1.269798I$	$-4.44298 + 1.97657I$	$-3.41444 - 3.62302I$
$u = 0.559459 - 0.682406I$ $a = 0.584057 + 0.456170I$ $b = -0.122694 - 0.403191I$	$0.106087 - 1.407485I$	$0.91901 + 2.91397I$
$u = 0.559459 + 0.682406I$ $a = 0.584057 - 0.456170I$ $b = -0.122694 + 0.403191I$	$0.106087 + 1.407485I$	$0.91901 - 2.91397I$
$u = 0.591154 - 1.059120I$ $a = 1.71916 - 0.51588I$ $b = -0.219268 + 0.999289I$	$-1.31705 - 3.54605I$	$2.16487 + 2.95335I$
$u = 0.591154 + 1.059120I$ $a = 1.71916 + 0.51588I$ $b = -0.219268 - 0.999289I$	$-1.31705 + 3.54605I$	$2.16487 - 2.95335I$
$u = 0.685929 - 0.418499I$ $a = -0.330311 + 0.852864I$ $b = 0.228042 - 0.683004I$	$0.22550 - 1.43526I$	$4.15937 + 3.64291I$
$u = 0.685929 + 0.418499I$ $a = -0.330311 - 0.852864I$ $b = 0.228042 + 0.683004I$	$0.22550 + 1.43526I$	$4.15937 - 3.64291I$

III. u-Polynomials

Crossings	u-Polynomials at each crossings
c_1	$(u^2 + u + 1)^3(u^{17} + 4u^{16} + \dots + 3u + 1)$
c_2	$(u^2 + u + 1)^3(u^{17} + 2u^{16} + \dots + 3u - 1)$
c_3, c_9	$u^6(u^{17} + u^{16} + \dots - 96u - 64)$
c_4	$(u^2 - u + 1)^3(u^{17} + 4u^{16} + \dots + 3u + 1)$
c_5	$(u^2 + u + 1)^3(u^{17} + 4u^{16} + \dots + 557u - 137)$
c_6, c_8	$(u^3 - u^2 + 1)^2(u^{17} + 3u^{16} + \dots + 2u + 1)$
c_7, c_{10}, c_{11}	$(u^3 - u^2 + 2u - 1)^2(u^{17} + 3u^{16} + \dots - 2u - 1)$

IV. Riley Polynomials

Crossings	Riley Polynomials at each crossings
c_1, c_4	$(y^2 + y + 1)^3(y^{17} + 2y^{16} + \dots + 3y - 1)$
c_2	$(y^2 + y + 1)^3(y^{17} + 30y^{16} + \dots + 3y - 1)$
c_3, c_9	$y^6(y^{17} + 35y^{16} + \dots + 9216y - 4096)$
c_5	$(y^2 + y + 1)^3(y^{17} + 58y^{16} + \dots - 518053y - 18769)$
c_6, c_8	$(y^3 - y^2 + 2y - 1)^2(y^{17} - 31y^{16} + \dots - 14y - 1)$
c_7, c_{10}, c_{11}	$(y^3 + 3y^2 + 2y - 1)^2(y^{17} + 13y^{16} + \dots - 14y - 1)$