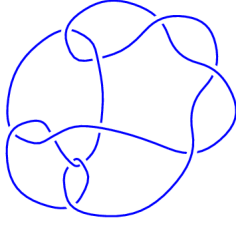
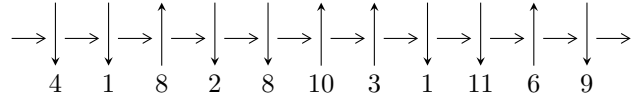


11n₂₈ (K11n₂₈)

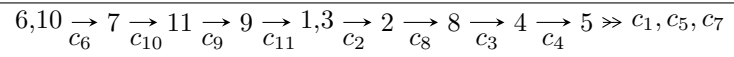


1

Arc Sequences



Solving Sequence



Representation Ideals

$$I = \bigcap_{i=1}^2 I_i^u$$

$$I_1^u = \langle b^4 + b^2 - b + 1, u - 1, -b^3 - b + a + 1 \rangle$$

$$\begin{aligned} I_2^u = & \langle u^{14} + u^{13} + \dots + 5u + 1, \\ & - 271965455479u^{13} - 11438964108u^{12} + \dots + 2446025522016a + 14628820700249, \\ & - 308923491301u^{13} - 413049036210u^{12} + \dots + 4892051044032b - 3107040395155 \rangle \end{aligned}$$

There are 2 irreducible components with 18 representations.

¹The knot diagram image is adapter from “C. Livingston and A. H. Moore, KnotInfo: Table of Knot Invariants, <http://www.indiana.edu/~knotinfo>”

$$\text{I. } I_1^u = \langle b^4 + b^2 - b + 1, u - 1, -b^3 - b + a + 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} b^3 + b - 1 \\ b \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -b^3 - b^2 - b \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} b^3 + b - 1 \\ -b^3 + 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} b^3 + b^2 + 2b \\ -b^3 - b^2 - b \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -b^3 + 2 \\ -1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -b^3 + 3 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -b^3 - b^2 - b \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} b^3 - 2 \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} b^3 - 2 \\ 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

| Solution to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 1.00000$ | | |
| $a = 0.351808 - 0.720342I$ | $-1.85594 - 1.41510I$ | $-5.13523 + 6.85627I$ |
| $b = -0.547424 - 1.120873I$ | | |
| $u = 1.00000$ | | |
| $a = 0.351808 + 0.720342I$ | $-1.85594 + 1.41510I$ | $-5.13523 - 6.85627I$ |
| $b = -0.547424 + 1.120873I$ | | |
| $u = 1.00000$ | | |
| $a = -0.851808 - 0.911292I$ | $5.14581 + 3.16396I$ | $0.63523 - 2.29471I$ |
| $b = 0.547424 - 0.585652I$ | | |
| $u = 1.00000$ | | |
| $a = -0.851808 + 0.911292I$ | $5.14581 - 3.16396I$ | $0.63523 + 2.29471I$ |
| $b = 0.547424 + 0.585652I$ | | |

$$\text{II. } I_2^u = \langle u^{14} + u^{13} + \dots + 5u + 1, -2.72 \times 10^{11} u^{13} - 1.14 \times 10^{10} u^{12} + \dots + 2.45 \times 10^{12} a + 1.46 \times 10^{13}, -3.09 \times 10^{11} u^{13} - 4.13 \times 10^{11} u^{12} + \dots + 4.89 \times 10^{12} b - 3.11 \times 10^{12} \rangle$$

(i) Arc colorings

$$\begin{aligned} a_6 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 0.111187u^{13} + 0.00467655u^{12} + \dots - 5.37669u - 5.98065 \\ 0.0631481u^{13} + 0.0844327u^{12} + \dots + 5.48597u + 0.635120 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 0.837327u^{13} + 0.807911u^{12} + \dots + 35.8519u + 0.145921 \\ -0.0747090u^{13} - 0.0508090u^{12} + \dots + 0.907321u + 0.616101 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0.111187u^{13} + 0.00467655u^{12} + \dots - 5.37669u - 5.98065 \\ 0.0680857u^{13} + 0.0928447u^{12} + \dots + 5.06461u + 0.528610 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 0.501986u^{13} + 0.489429u^{12} + \dots + 22.6456u - 1.10759 \\ -0.0584250u^{13} - 0.0317344u^{12} + \dots + 1.59756u + 0.586684 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -0.155664u^{13} - 0.198576u^{12} + \dots - 7.49944u - 3.10013 \\ u \end{pmatrix} \\ a_3 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_2 &= \begin{pmatrix} 0.0429122u^{13} + 0.0234198u^{12} + \dots + 2.32181u + 0.844336 \\ -u^2 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 0.762618u^{13} + 0.757102u^{12} + \dots + 36.7592u + 0.762022 \\ -0.0747090u^{13} - 0.0508090u^{12} + \dots + 0.907321u + 0.616101 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -0.653072u^{13} - 0.640947u^{12} + \dots - 21.7576u + 1.26505 \\ -0.0251734u^{13} - 0.0694250u^{12} + \dots - 2.74279u - 0.684274 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -0.540734u^{13} - 0.518543u^{12} + \dots - 18.1346u + 1.76849 \\ -0.0121243u^{13} - 0.0580186u^{12} + \dots - 2.53041u - 0.653072 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -0.540734u^{13} - 0.518543u^{12} + \dots - 18.1346u + 1.76849 \\ -0.0121243u^{13} - 0.0580186u^{12} + \dots - 2.53041u - 0.653072 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

| Solution to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------------------|
| $u = -0.841212 - 1.029315I$ $a = -0.025061 - 0.872571I$ $b = 1.268210 - 0.615843I$ | $7.00688 - 0.55948I$ | $2.27714 + 0.75874I$ |
| $u = -0.841212 + 1.029315I$ $a = -0.025061 + 0.872571I$ $b = 1.268210 + 0.615843I$ | $7.00688 + 0.55948I$ | $2.27714 - 0.75874I$ |
| $u = -0.337193 - 1.184656I$ $a = 0.920439 - 0.366491I$ $b = -1.54747 + 0.60627I$ | $6.27413 + 5.41755I$ | $1.11952 - 5.07443I$ |
| $u = -0.337193 + 1.184656I$ $a = 0.920439 + 0.366491I$ $b = -1.54747 - 0.60627I$ | $6.27413 - 5.41755I$ | $1.11952 + 5.07443I$ |
| $u = -0.196229 - 0.341059I$ $a = -1.93607 + 0.51409I$ $b = -0.550908 - 0.305501I$ | $0.65784 + 1.53044I$ | $1.45925 - 4.48215I$ |
| $u = -0.196229 + 0.341059I$ $a = -1.93607 - 0.51409I$ $b = -0.550908 + 0.305501I$ | $0.65784 - 1.53044I$ | $1.45925 + 4.48215I$ |
| $u = -0.17769 - 2.99241I$ $a = 0.294120 + 0.345863I$ $b = -2.42912 + 0.26319I$ | $18.9281 + 1.0022I$ | $1.174737 + 0.209171I$ |
| $u = -0.17769 + 2.99241I$ $a = 0.294120 - 0.345863I$ $b = -2.42912 - 0.26319I$ | $18.9281 - 1.0022I$ | $1.174737 - 0.209171I$ |
| $u = -0.038211 - 0.159690I$ $a = -5.38896 + 0.83379I$ $b = 0.190892 - 0.700537I$ | $-0.35154 + 1.84409I$ | $-0.79789 - 4.83996I$ |
| $u = -0.038211 + 0.159690I$ $a = -5.38896 - 0.83379I$ $b = 0.190892 + 0.700537I$ | $-0.35154 - 1.84409I$ | $-0.79789 + 4.83996I$ |

| Solution to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 0.07654 - 2.96001I$ | $18.7301 + 8.0616I$ | $0.87427 - 4.09385I$ |
| $a = -0.329002 + 0.327325I$ | | |
| $b = 2.94643 + 0.61854I$ | | |
| $u = 0.07654 + 2.96001I$ | $18.7301 - 8.0616I$ | $0.87427 + 4.09385I$ |
| $a = -0.329002 - 0.327325I$ | | |
| $b = 2.94643 - 0.61854I$ | | |
| $u = 1.013993 - 0.325583I$ | $-1.89748 + 0.70166I$ | $-5.60702 + 2.76477I$ |
| $a = -0.035467 - 0.501132I$ | | |
| $b = 0.621959 - 1.014427I$ | | |
| $u = 1.013993 + 0.325583I$ | $-1.89748 - 0.70166I$ | $-5.60702 - 2.76477I$ |
| $a = -0.035467 + 0.501132I$ | | |
| $b = 0.621959 + 1.014427I$ | | |

III. u-Polynomials

| Crossings | u-Polynomials at each crossings |
|------------|--|
| c_1 | $(u - 1)^4(u^{14} + 5u^{13} + \dots + 3u + 1)$ |
| c_2 | $(u + 1)^4(u^{14} + u^{13} + \dots + 5u + 1)$ |
| c_3, c_7 | $u^4(u^{14} + u^{13} + \dots + 72u + 16)$ |
| c_4 | $(u + 1)^4(u^{14} + 5u^{13} + \dots + 3u + 1)$ |
| c_5 | $(u^4 - u^3 + 3u^2 - 2u + 1)(u^{14} + 2u^{13} + \dots - 540u + 200)$ |
| c_6 | $(u^4 - u^3 + u^2 + 1)(u^{14} + 2u^{13} + \dots + u + 1)$ |
| c_8, c_9 | $(u^4 - u^3 + 3u^2 - 2u + 1)(u^{14} + 2u^{13} + \dots + 7u + 1)$ |
| c_{10} | $(u^4 + u^3 + u^2 + 1)(u^{14} + 2u^{13} + \dots + u + 1)$ |
| c_{11} | $(u^4 + u^3 + 3u^2 + 2u + 1)(u^{14} + 2u^{13} + \dots + 7u + 1)$ |

IV. Riley Polynomials

| Crossings | Riley Polynomials at each crossings |
|--------------------|--|
| c_1, c_4 | $(y - 1)^4(y^{14} + y^{13} + \dots + 5y + 1)$ |
| c_2 | $(y - 1)^4(y^{14} + 37y^{13} + \dots + 73y + 1)$ |
| c_3, c_7 | $y^4(y^{14} - 27y^{13} + \dots - 832y + 256)$ |
| c_5 | $(y^4 + 5y^3 + \dots + 2y + 1)(y^{14} + 82y^{13} + \dots + 531600y + 40000)$ |
| c_6, c_{10} | $(y^4 + y^3 + 3y^2 + 2y + 1)(y^{14} + 2y^{13} + \dots + 7y + 1)$ |
| c_8, c_9, c_{11} | $(y^4 + 5y^3 + \dots + 2y + 1)(y^{14} + 22y^{13} + \dots + 7y + 1)$ |