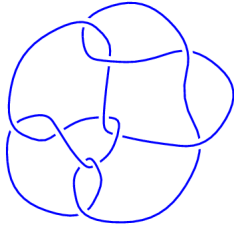
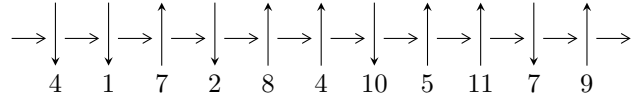


11n<sub>32</sub> (K11n<sub>32</sub>)

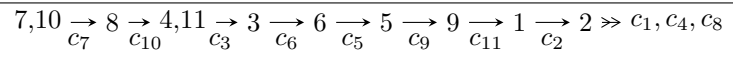


1

**Arc Sequences**



**Solving Sequence**



**Representation Ideals**

$$I = I_1^u \cap I_1^v$$

$$\begin{aligned} I_1^u = \langle & u^{38} + 5u^{37} + \dots + 104u + 16, \\ & -4.56249 \times 10^{53}u^{37} - 1.98366 \times 10^{54}u^{36} + \dots + 3.00630 \times 10^{54}b - 1.18639 \times 10^{55}, \\ & 1.39340 \times 10^{54}u^{37} + 6.28549 \times 10^{54}u^{36} + \dots + 1.50315 \times 10^{54}a + 4.25205 \times 10^{55} \rangle \end{aligned}$$

$$I_1^v = \langle b + v + 2, v^4 + 5v^3 + 7v^2 + 2v + 1, a \rangle$$

There are 2 irreducible components with 42 representations.

---

<sup>1</sup>The knot diagram image is adapter from “C. Livingston and A. H. Moore, KnotInfo: Table of Knot Invariants, <http://www.indiana.edu/~knotinfo>”

$$\mathbf{I. } I_1^u = \langle u^{38} + 5u^{37} + \dots + 104u + 16, -4.56 \times 10^{53} u^{37} - 1.98 \times 10^{54} u^{36} + \dots + 3.01 \times 10^{54} b - 1.19 \times 10^{55}, 1.39 \times 10^{54} u^{37} + 6.29 \times 10^{54} u^{36} + \dots + 1.50 \times 10^{54} a + 4.25 \times 10^{55} \rangle$$

(i) Arc colorings

$$\begin{aligned} a_7 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -0.926987u^{37} - 4.18155u^{36} + \dots - 135.593u - 28.2876 \\ 0.151764u^{37} + 0.659836u^{36} + \dots + 18.5840u + 3.94634 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 1.22438u^{37} + 5.44528u^{36} + \dots + 159.909u + 34.0751 \\ 0.0453851u^{37} + 0.197052u^{36} + \dots + 8.02644u + 1.84760 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -0.926987u^{37} - 4.18155u^{36} + \dots - 135.593u - 28.2876 \\ -0.0784391u^{37} - 0.360238u^{36} + \dots - 13.7357u - 3.30772 \end{pmatrix} \\ a_3 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -u \\ u \end{pmatrix} \\ a_5 &= \begin{pmatrix} -0.471885u^{37} - 2.14728u^{36} + \dots - 70.9792u - 17.1177 \\ -0.0642746u^{37} - 0.280900u^{36} + \dots - 9.18787u - 2.15226 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -1.78274u^{37} - 7.95424u^{36} + \dots - 250.772u - 53.4037 \\ -0.431125u^{37} - 1.91026u^{36} + \dots - 56.0313u - 11.8301 \end{pmatrix} \\ a_1 &= \begin{pmatrix} 0.536159u^{37} + 2.42818u^{36} + \dots + 80.1670u + 19.2700 \\ 0.0631382u^{37} + 0.279519u^{36} + \dots + 8.50618u + 1.88968 \end{pmatrix} \\ a_2 &= \begin{pmatrix} 0.473021u^{37} + 2.14866u^{36} + \dots + 71.6609u + 17.3803 \\ 0.0631382u^{37} + 0.279519u^{36} + \dots + 8.50618u + 1.88968 \end{pmatrix} \\ a_2 &= \begin{pmatrix} 0.473021u^{37} + 2.14866u^{36} + \dots + 71.6609u + 17.3803 \\ 0.0631382u^{37} + 0.279519u^{36} + \dots + 8.50618u + 1.88968 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.52004 - 0.19492I$ $a = -0.483337 - 0.494284I$ $b = -0.12654 + 1.78294I$	$-4.60338 - 2.49292I$	$-7.66096 + 3.58742I$
$u = -1.52004 + 0.19492I$ $a = -0.483337 + 0.494284I$ $b = -0.12654 - 1.78294I$	$-4.60338 + 2.49292I$	$-7.66096 - 3.58742I$
$u = -1.45402 - 0.43836I$ $a = -0.183345 - 0.763715I$ $b = -0.51595 + 2.64583I$	$6.16601 + 6.56194I$	$4.09697 - 5.13849I$
$u = -1.45402 + 0.43836I$ $a = -0.183345 + 0.763715I$ $b = -0.51595 - 2.64583I$	$6.16601 - 6.56194I$	$4.09697 + 5.13849I$
$u = -1.43940 - 0.79817I$ $a = -0.050059 + 0.782526I$ $b = -0.16177 - 2.72225I$	$1.10073 + 13.93897I$	$-0.18114 - 8.68220I$
$u = -1.43940 + 0.79817I$ $a = -0.050059 - 0.782526I$ $b = -0.16177 + 2.72225I$	$1.10073 - 13.93897I$	$-0.18114 + 8.68220I$
$u = -1.32611 - 0.72615I$ $a = -0.689407 - 0.049253I$ $b = 0.149271 - 0.003685I$	$-0.48850 + 8.10053I$	$-2.17285 - 4.60397I$
$u = -1.32611 + 0.72615I$ $a = -0.689407 + 0.049253I$ $b = 0.149271 + 0.003685I$	$-0.48850 - 8.10053I$	$-2.17285 + 4.60397I$
$u = -1.233006 - 0.050062I$ $a = 0.516758 + 0.875767I$ $b = 0.79276 - 1.84419I$	$2.77951 - 1.18659I$	$2.30827 - 0.46017I$
$u = -1.233006 + 0.050062I$ $a = 0.516758 - 0.875767I$ $b = 0.79276 + 1.84419I$	$2.77951 + 1.18659I$	$2.30827 + 0.46017I$

Solution to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.156071 - 0.287792I$	$0.57801 + 4.07433I$	$-1.00107 - 5.21688I$
$a = 0.609116 - 0.482021I$		
$b = -0.088892 + 0.144996I$		
$u = -1.156071 + 0.287792I$	$0.57801 - 4.07433I$	$-1.00107 + 5.21688I$
$a = 0.609116 + 0.482021I$		
$b = -0.088892 - 0.144996I$		
$u = -0.55366 - 1.35876I$	$-3.24288 - 0.91080I$	$-5.85440 + 2.87226I$
$a = 0.289945 + 0.580664I$		
$b = 0.34598 - 1.37942I$		
$u = -0.55366 + 1.35876I$	$-3.24288 + 0.91080I$	$-5.85440 - 2.87226I$
$a = 0.289945 - 0.580664I$		
$b = 0.34598 + 1.37942I$		
$u = -0.533786 - 0.030166I$	$-8.01967 + 3.23855I$	$7.49106 - 4.17157I$
$a = -1.54034 + 1.80642I$		
$b = -0.289563 - 0.253759I$		
$u = -0.533786 + 0.030166I$	$-8.01967 - 3.23855I$	$7.49106 + 4.17157I$
$a = -1.54034 - 1.80642I$		
$b = -0.289563 + 0.253759I$		
$u = -0.391833 - 0.533554I$	$-1.88768 - 0.79705I$	$-5.20475 - 0.93842I$
$a = 0.481578 - 0.104361I$		
$b = -1.014341 - 0.314495I$		
$u = -0.391833 + 0.533554I$	$-1.88768 + 0.79705I$	$-5.20475 + 0.93842I$
$a = 0.481578 + 0.104361I$		
$b = -1.014341 + 0.314495I$		
$u = -0.26079 - 1.59013I$	$-2.54932 - 5.85938I$	$-3.38157 + 9.01726I$
$a = -0.641426 + 0.289977I$		
$b = -1.099622 - 0.719781I$		
$u = -0.26079 + 1.59013I$	$-2.54932 + 5.85938I$	$-3.38157 - 9.01726I$
$a = -0.641426 - 0.289977I$		
$b = -1.099622 + 0.719781I$		

Solution to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.230395 - 0.298664I$ $a = 2.30144 + 0.56503I$ $b = -0.108722 - 0.621711I$	$0.31225 - 1.54508I$	$2.23777 + 4.87383I$
$u = -0.230395 + 0.298664I$ $a = 2.30144 - 0.56503I$ $b = -0.108722 + 0.621711I$	$0.31225 + 1.54508I$	$2.23777 - 4.87383I$
$u = 0.162866 - 0.630461I$ $a = -1.58426 - 0.48425I$ $b = 0.86678 + 1.49705I$	$-1.35379 + 2.75023I$	$-1.67570 + 2.67847I$
$u = 0.162866 + 0.630461I$ $a = -1.58426 + 0.48425I$ $b = 0.86678 - 1.49705I$	$-1.35379 - 2.75023I$	$-1.67570 - 2.67847I$
$u = 0.275945 - 0.814062I$ $a = 0.852519 - 0.312379I$ $b = 0.698335 - 0.334641I$	$0.77944 - 1.52604I$	$4.36193 + 4.60900I$
$u = 0.275945 + 0.814062I$ $a = 0.852519 + 0.312379I$ $b = 0.698335 + 0.334641I$	$0.77944 + 1.52604I$	$4.36193 - 4.60900I$
$u = 0.278602 - 0.363866I$ $a = 0.68703 - 1.96808I$ $b = -1.48828 + 2.95029I$	$-1.79987 - 1.63683I$	$0.6342 + 22.3814I$
$u = 0.278602 + 0.363866I$ $a = 0.68703 + 1.96808I$ $b = -1.48828 - 2.95029I$	$-1.79987 + 1.63683I$	$0.6342 - 22.3814I$
$u = 1.139293 - 0.198092I$ $a = -0.800512 + 0.400559I$ $b = 0.008420 + 0.191321I$	$0.789901 - 0.872417I$	$0.203682 + 1.029460I$
$u = 1.139293 + 0.198092I$ $a = -0.800512 - 0.400559I$ $b = 0.008420 - 0.191321I$	$0.789901 + 0.872417I$	$0.203682 - 1.029460I$

Solution to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.259828 - 0.356568I$ $a = -0.295658 - 0.923203I$ $b = -0.84185 + 1.97914I$	$2.13442 - 6.62776I$	$1.31703 + 5.48212I$
$u = 1.259828 + 0.356568I$ $a = -0.295658 + 0.923203I$ $b = -0.84185 - 1.97914I$	$2.13442 + 6.62776I$	$1.31703 - 5.48212I$
$u = 1.32367 - 0.54173I$ $a = 0.590584 - 0.104768I$ $b = 0.168421 + 0.170029I$	$1.89024 - 2.00477I$	$0.55164 + 1.57531I$
$u = 1.32367 + 0.54173I$ $a = 0.590584 + 0.104768I$ $b = 0.168421 - 0.170029I$	$1.89024 + 2.00477I$	$0.55164 - 1.57531I$
$u = 1.53818 - 0.08244I$ $a = 0.078634 - 0.734504I$ $b = 0.51262 + 2.63453I$	$7.11789 - 0.13853I$	$5.96603 - 0.12241I$
$u = 1.53818 + 0.08244I$ $a = 0.078634 + 0.734504I$ $b = 0.51262 - 2.63453I$	$7.11789 + 0.13853I$	$5.96603 + 0.12241I$
$u = 1.62072 - 0.63223I$ $a = 0.110732 + 0.695721I$ $b = 0.19294 - 2.63595I$	$3.58657 - 7.12992I$	$2.46388 + 6.33493I$
$u = 1.62072 + 0.63223I$ $a = 0.110732 - 0.695721I$ $b = 0.19294 + 2.63595I$	$3.58657 + 7.12992I$	$2.46388 - 6.33493I$

$$\text{II. } I_1^v = \langle b + v + 2, v^4 + 5v^3 + 7v^2 + 2v + 1, a \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ -v - 2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} v \\ v^3 + 4v^2 + 4v \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} v^3 + 2v^2 \\ -v - 2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 2v^3 + 5v^2 + 2v + 1 \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 2v^3 + 6v^2 + 2v + 1 \\ v^2 + 2v - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -2v^3 - 5v^2 - 2v - 1 \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -2v^3 - 5v^2 - 2v \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -2v^3 - 5v^2 - 2v \\ -1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to $I_1^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = -2.39923 - 0.32564I$ $a = 0$ $b = 0.399232 + 0.325640I$	$-8.43568 - 3.16396I$	$-11.64142 + 1.04769I$
$v = -2.39923 + 0.32564I$ $a = 0$ $b = 0.399232 - 0.325640I$	$-8.43568 + 3.16396I$	$-11.64142 - 1.04769I$
$v = -0.100768 - 0.400532I$ $a = 0$ $b = -1.89923 + 0.40053I$	$-1.43393 - 1.41510I$	$3.14142 + 7.60220I$
$v = -0.100768 + 0.400532I$ $a = 0$ $b = -1.89923 - 0.40053I$	$-1.43393 + 1.41510I$	$3.14142 - 7.60220I$



### III. u-Polynomials

Crossings	u-Polynomials at each crossings
$c_1$	$(u - 1)^4(u^{38} + 5u^{37} + \dots - u + 1)$
$c_2$	$(u + 1)^4(u^{38} + 15u^{37} + \dots - 81u + 1)$
$c_3, c_6$	$u^4(u^{38} + 5u^{37} + \dots + 104u + 16)$
$c_4$	$(u + 1)^4(u^{38} + 5u^{37} + \dots - u + 1)$
$c_5$	$(u^4 + u^3 + 3u^2 + 2u + 1)(u^{38} + 2u^{37} + \dots + u + 1)$
$c_7$	$(u^4 + u^3 + u^2 + 1)(u^{38} + 2u^{37} + \dots - 3u + 1)$
$c_8$	$(u^4 - u^3 + 3u^2 - 2u + 1)(u^{38} + 2u^{37} + \dots + u + 1)$
$c_9$	$(u^4 + u^3 + 3u^2 + 2u + 1)(u^{38} + 14u^{37} + \dots + 7u + 1)$
$c_{10}$	$(u^4 - u^3 + u^2 + 1)(u^{38} + 2u^{37} + \dots - 3u + 1)$
$c_{11}$	$(u^4 - u^3 + 3u^2 - 2u + 1)(u^{38} + 14u^{37} + \dots + 7u + 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossings
$c_1, c_4$	$(y - 1)^4(y^{38} - 15y^{37} + \dots + 81y + 1)$
$c_2$	$(y - 1)^4(y^{38} + 21y^{37} + \dots - 2859y + 1)$
$c_3, c_6$	$y^4(y^{38} - 27y^{37} + \dots - 320y + 256)$
$c_5, c_8$	$(y^4 + 5y^3 + \dots + 2y + 1)(y^{38} + 10y^{37} + \dots + 7y + 1)$
$c_7, c_{10}$	$(y^4 + y^3 + 3y^2 + 2y + 1)(y^{38} + 14y^{37} + \dots + 7y + 1)$
$c_9, c_{11}$	$(y^4 + 5y^3 + \dots + 2y + 1)(y^{38} + 22y^{37} + \dots + 179y + 1)$