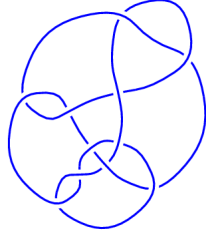
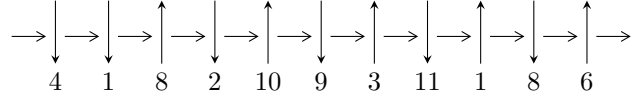


11n₃₉ (K11n₃₉)

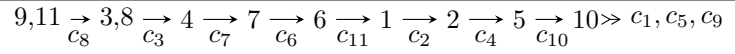


1

Arc Sequences



Solving Sequence



Representation Ideals

$$I = \bigcap_{i=1}^4 I_i^u$$

$$I_1^u = \langle 9a^{12} - 24a^{11} + 2a^{10} + 35a^9 + 14a^8 - 75a^7 + 16a^6 + 43a^5 + 10a^4 - 37a^3 + 6a^2 + 7a + 1, \\ - 716396616a^{11} + 263745113b + \dots - 374049402a - 73369744, \\ - 410540292a^{11} + 263745113u + \dots - 2044126867a - 369175518 \rangle$$

$$I_2^u = \langle u^6 - 6u^5 + 11u^4 - 4u^3 - u^2 - u + 1, -u^5 + 6u^4 - 11u^3 + 4u^2 + a + u + 1, \\ 3u^5 - 13u^4 + 7u^3 + 17u^2 + 13b + 8u - 7 \rangle$$

$$I_3^u = \langle u^6 + 6u^5 + 11u^4 + 4u^3 - u^2 + u + 1, 3u^5 + 13u^4 + 7u^3 - 17u^2 + 13b + 8u + 7, \\ 21u^5 + 117u^4 + 179u^3 - 2u^2 + 13a - 35u + 23 \rangle$$

$$I_4^u = \langle u^{12} + 11u^{11} + 45u^{10} + 132u^9 + 363u^8 + 440u^7 + 892u^6 + 262u^5 + 448u^4 - 241u^3 - 175u^2 + 26u + 17, \\ - 3.24712 \times 10^{14}u^{11} - 3.40329 \times 10^{15}u^{10} + \dots + 4.19367 \times 10^{16}b - 2.43530 \times 10^{16}, \\ 6.08778 \times 10^{16}u^{11} + 6.63150 \times 10^{17}u^{10} + \dots + 7.12924 \times 10^{17}a + 1.91045 \times 10^{18} \rangle$$

There are 4 irreducible components with 36 representations.

¹The knot diagram image is adapter from “C. Livingston and A. H. Moore, KnotInfo: Table of Knot Invariants, <http://www.indiana.edu/~knotinfo>”

I.

$$I_1^u = \langle 9a^{12} - 24a^{11} + \dots + 7a + 1, 2.64 \times 10^8 b - 7.16 \times 10^8 a^{11} + \dots - 3.74 \times 10^8 a - 7.34 \times 10^7, 2.64 \times 10^8 u - 4.11 \times 10^8 a^{11} + \dots - 2.04 \times 10^9 a - 3.69 \times 10^8 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_9 &= \begin{pmatrix} 0 \\ 1.55658a^{11} - 6.67995a^{10} + \dots + 7.75039a + 1.39974 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} a \\ 2.71625a^{11} - 6.26861a^{10} + \dots + 1.41822a + 0.278184 \end{pmatrix} \\ a_3 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -0.467857a^{11} + 1.58935a^{10} + \dots + 1.79411a + 0.281008 \\ 2.73950a^{11} - 7.30187a^{10} + \dots + 8.57417a + 1.63340 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1.94598a^{11} - 4.39757a^{10} + \dots - 3.17158a + 0.700778 \\ 5.76845a^{11} - 16.4903a^{10} + \dots + 0.465582a + 1.71218 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -3.20735a^{11} + 8.89122a^{10} + \dots - 6.78007a - 1.35239 \\ 2.73950a^{11} - 7.30187a^{10} + \dots + 8.57417a + 1.63340 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -3.20735a^{11} + 8.89122a^{10} + \dots - 6.78007a - 1.35239 \\ 2.62673a^{11} - 10.8456a^{10} + \dots + 7.18779a + 2.59583 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -0.489083a^{11} + 0.0896889a^{10} + \dots + 1.16589a + 0.803097 \\ -0.0254170a^{11} - 3.11632a^{10} + \dots + 9.16399a + 1.35611 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -0.482184a^{11} + 2.78223a^{10} + \dots + 0.171244a + 1.19432 \\ 12.0102a^{11} - 28.0103a^{10} + \dots + 14.0214a + 3.58774 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 13.3420a^{11} - 29.8730a^{10} + \dots + 2.95914a + 1.08538 \\ 19.4429a^{11} - 37.3345a^{10} + \dots - 21.0429a - 3.75506 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 2.10036a^{11} - 3.74367a^{10} + \dots - 1.39524a - 0.337983 \\ 5.40924a^{11} - 11.5039a^{10} + \dots - 4.31951a - 0.798845 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 2.10036a^{11} - 3.74367a^{10} + \dots - 1.39524a - 0.337983 \\ 5.40924a^{11} - 11.5039a^{10} + \dots - 4.31951a - 0.798845 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.287706 + 0.831147I$ $a = -0.960631 - 0.671826I$ $b = -0.142924 + 1.159516I$	$2.99789 + 2.65597I$	$1.54637 - 3.55162I$
$u = 0.287706 - 0.831147I$ $a = -0.960631 + 0.671826I$ $b = -0.142924 - 1.159516I$	$2.99789 - 2.65597I$	$1.54637 + 3.55162I$
$u = 0.26437 + 2.03792I$ $a = -0.645041 - 0.612930I$ $b = -0.03547 - 1.77530I$	$13.70954 - 3.42721I$	$0.48765 + 2.36550I$
$u = 0.26437 - 2.03792I$ $a = -0.645041 + 0.612930I$ $b = -0.03547 + 1.77530I$	$13.70954 + 3.42721I$	$0.48765 - 2.36550I$
$u = -0.552079 - 0.783280I$ $a = -0.205082 - 0.070064I$ $b = -0.321608 - 0.359079I$	$-1.90302 - 1.10871I$	$-2.03402 + 2.13465I$
$u = -0.552079 + 0.783280I$ $a = -0.205082 + 0.070064I$ $b = -0.321608 + 0.359079I$	$-1.90302 + 1.10871I$	$-2.03402 - 2.13465I$
$u = 0.26437 + 2.03792I$ $a = 0.718893 - 0.432703I$ $b = -0.03547 - 1.77530I$	$13.70954 - 3.42721I$	$0.48765 + 2.36550I$
$u = 0.26437 - 2.03792I$ $a = 0.718893 + 0.432703I$ $b = -0.03547 + 1.77530I$	$13.70954 + 3.42721I$	$0.48765 - 2.36550I$
$u = -0.552079 - 0.783280I$ $a = 0.987935 - 0.622278I$ $b = -0.321608 - 0.359079I$	$-1.90302 - 1.10871I$	$-2.03402 + 2.13465I$
$u = -0.552079 + 0.783280I$ $a = 0.987935 + 0.622278I$ $b = -0.321608 + 0.359079I$	$-1.90302 + 1.10871I$	$-2.03402 - 2.13465I$

	Solution to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u =$	$0.287706 - 0.831147I$		
$a =$	$1.43726 - 0.44693I$	$2.99789 - 2.65597I$	$1.54637 + 3.55162I$
$b =$	$-0.142924 - 1.159516I$		
$u =$	$0.287706 + 0.831147I$		
$a =$	$1.43726 + 0.44693I$	$2.99789 + 2.65597I$	$1.54637 - 3.55162I$
$b =$	$-0.142924 + 1.159516I$		

$$\text{II. } I_2^u = \langle u^6 - 6u^5 + 11u^4 - 4u^3 - u^2 - u + 1, -u^5 + 6u^4 - 11u^3 + 4u^2 + a + u + 1, 3u^5 - 13u^4 + 7u^3 + 17u^2 + 13b + 8u - 7 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_9 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_{11} &= \begin{pmatrix} u^5 - 6u^4 + 11u^3 - 4u^2 - u - 1 \\ -\frac{3}{13}u^5 + u^4 + \dots - \frac{8}{13}u + \frac{7}{13} \end{pmatrix} \\ a_3 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -u^5 + 6u^4 - 11u^3 + 4u^2 + u + 1 \\ \frac{3}{13}u^5 - u^4 + \dots + \frac{21}{13}u - \frac{7}{13} \end{pmatrix} \\ a_4 &= \begin{pmatrix} -\frac{7}{13}u^5 + 3u^4 + \dots - \frac{10}{13}u - \frac{1}{13} \\ -1.15385u^5 + 6u^4 + \dots + 0.923077u + 0.692308 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -1.23077u^5 + 7u^4 + \dots - 0.615385u + 1.53846 \\ \frac{3}{13}u^5 - u^4 + \dots + \frac{21}{13}u - \frac{7}{13} \end{pmatrix} \\ a_6 &= \begin{pmatrix} -1.23077u^5 + 7u^4 + \dots - 0.615385u + 1.53846 \\ \frac{7}{13}u^5 - 3u^4 + \dots + \frac{10}{13}u - \frac{12}{13} \end{pmatrix} \\ a_1 &= \begin{pmatrix} 0 \\ \frac{19}{13}u^5 - 8u^4 + \dots - \frac{10}{13}u - \frac{27}{13} \end{pmatrix} \\ a_2 &= \begin{pmatrix} 1 \\ \frac{25}{13}u^5 - 10u^4 + \dots - \frac{7}{13}u - \frac{28}{13} \end{pmatrix} \\ a_5 &= \begin{pmatrix} -1.23077u^5 + 7u^4 + \dots - 0.615385u + 1.53846 \\ \frac{3}{13}u^5 - u^4 + \dots + \frac{21}{13}u - \frac{7}{13} \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.346225 - 0.393823I$		
$a = 1.25915 - 1.43225I$	$0.245672 + 0.924305I$	$1.12292 - 1.33143I$
$b = 0.655968 - 0.098281I$		
$u = -0.346225 + 0.393823I$		
$a = 1.25915 + 1.43225I$	$0.245672 - 0.924305I$	$1.12292 + 1.33143I$
$b = 0.655968 + 0.098281I$		
$u = 0.658836 - 0.177500I$		
$a = -1.41511 - 0.38125I$	$-1.64493 - 5.69302I$	$-0.29418 + 2.69056I$
$b = -0.415113 + 0.381252I$		
$u = 0.658836 + 0.177500I$		
$a = -1.41511 + 0.38125I$	$-1.64493 + 5.69302I$	$-0.29418 - 2.69056I$
$b = -0.415113 - 0.381252I$		
$u = 2.68739 - 0.76772I$		
$a = -0.344032 - 0.098281I$	$-3.53554 - 0.92430I$	$-6.82874 + 7.13914I$
$b = 2.25915 - 1.43225I$		
$u = 2.68739 + 0.76772I$		
$a = -0.344032 + 0.098281I$	$-3.53554 + 0.92430I$	$-6.82874 - 7.13914I$
$b = 2.25915 + 1.43225I$		

$$\text{III. } I_3^u = \langle u^6 + 6u^5 + 11u^4 + 4u^3 - u^2 + u + 1, 3u^5 + 13u^4 + 7u^3 - 17u^2 + 13b + 8u + 7, 21u^5 + 117u^4 + \dots + 13a + 23 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_9 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -1.61538u^5 - 9u^4 + \dots + 2.69231u - 1.76923 \\ -\frac{3}{13}u^5 - u^4 + \dots - \frac{8}{13}u - \frac{7}{13} \end{pmatrix} \\ a_3 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -2.07692u^5 - 11u^4 + \dots + 2.46154u - 2.84615 \\ 0 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -2.07692u^5 - 11u^4 + \dots + 2.46154u - 2.84615 \\ 0 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -2.07692u^5 - 11u^4 + \dots + 2.46154u - 2.84615 \\ \frac{10}{13}u^5 + 4u^4 + \dots - \frac{8}{13}u + \frac{19}{13} \end{pmatrix} \\ a_1 &= \begin{pmatrix} -0.538462u^5 - 3u^4 + \dots - 0.769231u + 1.07692 \\ -1 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -0.538462u^5 - 3u^4 + \dots - 0.769231u + 2.07692 \\ -1 \end{pmatrix} \\ a_5 &= \begin{pmatrix} \frac{7}{13}u^5 + 3u^4 + \dots + \frac{10}{13}u - \frac{14}{13} \\ 1 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} \frac{9}{13}u^5 + 3u^4 + \dots + \frac{24}{13}u + \frac{21}{13} \\ -\frac{3}{13}u^5 - u^4 + \dots - \frac{8}{13}u - \frac{7}{13} \end{pmatrix} \\ a_{10} &= \begin{pmatrix} \frac{9}{13}u^5 + 3u^4 + \dots + \frac{24}{13}u + \frac{21}{13} \\ -\frac{3}{13}u^5 - u^4 + \dots - \frac{8}{13}u - \frac{7}{13} \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -2.68739 - 0.76772I$		
$a = 0.315740 - 0.200172I$	$-3.53554 + 0.92430I$	$-6.82874 - 7.13914I$
$b = -2.25915 - 1.43225I$		
$u = -2.68739 + 0.76772I$		
$a = 0.315740 + 0.200172I$	$-3.53554 - 0.92430I$	$-6.82874 + 7.13914I$
$b = -2.25915 + 1.43225I$		
$u = -0.658836 - 0.177500I$		
$a = -1.30674 + 1.20014I$	$-1.64493 + 5.69302I$	$-0.29418 - 2.69056I$
$b = 0.415113 + 0.381252I$		
$u = -0.658836 + 0.177500I$		
$a = -1.30674 - 1.20014I$	$-1.64493 - 5.69302I$	$-0.29418 + 2.69056I$
$b = 0.415113 - 0.381252I$		
$u = 0.346225 - 0.393823I$		
$a = 1.49099 - 0.22339I$	$0.245672 - 0.924305I$	$1.12292 + 1.33143I$
$b = -0.655968 - 0.098281I$		
$u = 0.346225 + 0.393823I$		
$a = 1.49099 + 0.22339I$	$0.245672 + 0.924305I$	$1.12292 - 1.33143I$
$b = -0.655968 + 0.098281I$		

$$\text{IV. } I_4^u = \langle u^{12} + 11u^{11} + \dots + 26u + 17, -3.25 \times 10^{14}u^{11} - 3.40 \times 10^{15}u^{10} + \dots + 4.19 \times 10^{16}b - 2.44 \times 10^{16}, 6.09 \times 10^{16}u^{11} + 6.63 \times 10^{17}u^{10} + \dots + 7.13 \times 10^{17}a + 1.91 \times 10^{18} \rangle$$

(i) Arc colorings

$$\begin{aligned} a_9 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -0.0853917u^{11} - 0.930183u^{10} + \dots + 9.79732u - 2.67973 \\ 0.00774291u^{11} + 0.0811531u^{10} + \dots + 1.12134u + 0.580709 \end{pmatrix} \\ a_3 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -0.0963108u^{11} - 1.04029u^{10} + \dots + 7.60207u - 3.77824 \\ 0.00121114u^{11} + 0.00771332u^{10} + \dots + 2.40248u + 0.338763 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -0.0456746u^{11} - 0.486274u^{10} + \dots + 4.39208u - 2.66422 \\ 0.0194727u^{11} + 0.208795u^{10} + \dots - 1.15800u + 0.240603 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -0.0975219u^{11} - 1.04800u^{10} + \dots + 5.19958u - 4.11700 \\ 0.00121114u^{11} + 0.00771332u^{10} + \dots + 2.40248u + 0.338763 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -0.0975219u^{11} - 1.04800u^{10} + \dots + 5.19958u - 4.11700 \\ 0.0107548u^{11} + 0.110501u^{10} + \dots + 1.38781u + 0.759315 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -0.0199272u^{11} - 0.217988u^{10} + \dots + 0.512481u + 1.88438 \\ -0.0191292u^{11} - 0.199567u^{10} + \dots + 1.27416u - 1.63728 \end{pmatrix} \\ a_2 &= \begin{pmatrix} 0.0456746u^{11} + 0.486274u^{10} + \dots - 4.39208u + 4.66422 \\ -0.0319988u^{11} - 0.338850u^{10} + \dots + 1.41177u - 1.59278 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 0.0381797u^{11} + 0.404025u^{10} + \dots - 1.43158u + 3.01894 \\ -0.0115322u^{11} - 0.123552u^{10} + \dots - 0.459356u - 1.08766 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 0.0141531u^{11} + 0.136211u^{10} + \dots + 4.64120u + 1.52598 \\ 0.0161459u^{11} + 0.179885u^{10} + \dots - 1.47668u + 0.776467 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 0.0141531u^{11} + 0.136211u^{10} + \dots + 4.64120u + 1.52598 \\ 0.0161459u^{11} + 0.179885u^{10} + \dots - 1.47668u + 0.776467 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_4^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -5.15079 - 0.85342I$		
$a = 0.188984 - 0.051071I$	$-3.52730 + 0.57280I$	$-2.7091 + 26.6989I$
$b = -4.57965 - 1.61583I$		
$u = -5.15079 + 0.85342I$		
$a = 0.188984 + 0.051071I$	$-3.52730 - 0.57280I$	$-2.7091 - 26.6989I$
$b = -4.57965 + 1.61583I$		
$u = -0.336025 - 0.091002I$		
$a = -2.47915 + 1.81043I$	$-1.70690 + 6.65526I$	$-0.69156 - 12.28500I$
$b = -0.286636 - 0.460834I$		
$u = -0.336025 + 0.091002I$		
$a = -2.47915 - 1.81043I$	$-1.70690 - 6.65526I$	$-0.69156 + 12.28500I$
$b = -0.286636 + 0.460834I$		
$u = -0.21322 - 1.93092I$		
$a = 0.471977 + 0.723712I$	$12.72394 + 5.46645I$	$-0.22295 - 2.11548I$
$b = 0.01283 + 2.08864I$		
$u = -0.21322 + 1.93092I$		
$a = 0.471977 - 0.723712I$	$12.72394 - 5.46645I$	$-0.22295 + 2.11548I$
$b = 0.01283 - 2.08864I$		
$u = -0.126143 - 1.177030I$		
$a = 0.263148 - 0.455055I$	$-1.61529 - 1.35793I$	$-3.64822 + 4.51645I$
$b = -0.518983 - 0.603778I$		
$u = -0.126143 + 1.177030I$		
$a = 0.263148 + 0.455055I$	$-1.61529 + 1.35793I$	$-3.64822 - 4.51645I$
$b = -0.518983 + 0.603778I$		
$u = -0.08836 - 2.35166I$		
$a = -0.479676 + 0.565939I$	$12.4026 - 12.7511I$	$-0.69002 + 5.94531I$
$b = 0.24682 + 2.17415I$		
$u = -0.08836 + 2.35166I$		
$a = -0.479676 - 0.565939I$	$12.4026 + 12.7511I$	$-0.69002 - 5.94531I$
$b = 0.24682 - 2.17415I$		

	Solution to I_4^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u =$	$0.414535 - 0.062132I$	$1.46216 + 0.16286I$	$7.96188 + 1.03516I$
$a =$	$0.887657 + 0.804181I$		
$b =$	$0.625624 + 0.005267I$		
$u =$	$0.414535 + 0.062132I$	$1.46216 - 0.16286I$	$7.96188 - 1.03516I$
$a =$	$0.887657 - 0.804181I$		
$b =$	$0.625624 - 0.005267I$		

V. u-Polynomials

Crossings	u-Polynomials at each crossings
c_1, c_8	$(u-1)^6(u^6 + u^5 + \dots + u + 1)(u^{12} + 3u^{11} + \dots + 3u + 1)$ $(u^{12} + 5u^{11} + \dots + 2u + 1)$
c_2	$(u+1)^6(u^6 + 3u^5 + 5u^4 + 4u^3 + 2u^2 + u + 1)$ $(u^{12} - 7u^{11} + \dots - 41u + 1)(u^{12} + 7u^{11} + \dots + 10u + 1)$
c_3, c_9	$u^6(u^6 - u^5 + \dots - u + 1)(u^{12} + u^{11} + \dots + 320u + 64)$ $(u^{12} + u^{11} + \dots + 2u + 1)$
c_4, c_{10}	$(u+1)^6(u^6 - u^5 + \dots - u + 1)(u^{12} + 3u^{11} + \dots + 3u + 1)$ $(u^{12} + 5u^{11} + \dots + 2u + 1)$
c_5	$(u^6 - u^5 - u^4 + 2u^3 - u + 1)(u^6 - u^5 + 2u^4 - 4u^3 + 5u^2 - 3u + 1)$ $(u^{12} - 14u^{10} + \dots - 120u + 77)(u^{12} + u^{11} + \dots - 44u + 23)$
c_6	$(u^6 - 3u^5 + \dots - u + 1)(u^6 - u^5 + \dots - 3u + 1)$ $(u^{12} + 2u^{11} + \dots - 144u + 121)(u^{12} + 3u^{11} + \dots + 14u + 4)$
c_7	$u^6(u^6 + u^5 + \dots + u + 1)(u^{12} + u^{11} + \dots + 320u + 64)$ $(u^{12} + u^{11} + \dots + 2u + 1)$
c_{11}	$(u^6 - 3u^5 + 5u^4 - 4u^3 + 2u^2 - u + 1)(u^6 + u^5 + u^4 + 2u^2 + u + 1)^2$ $(u^6 + 3u^5 + 5u^4 + 4u^3 + 2u^2 + u + 1)$ $(u^{12} + u^{11} + u^{10} + 5u^8 - 4u^6 - 8u^5 + 6u^4 + 3u^3 + 3u^2 + 1)$

VI. Riley Polynomials

Crossings	Riley Polynomials at each crossings
c_1, c_4, c_8 c_{10}	$(y-1)^6(y^6 - 3y^5 + 5y^4 - 4y^3 + 2y^2 - y + 1)$ $(y^{12} - 7y^{11} + \dots - 10y + 1)(y^{12} + 7y^{11} + \dots + 41y + 1)$
c_2	$(y-1)^6(y^6 + y^5 + \dots + 3y + 1)(y^{12} + 27y^{11} + \dots - 451y + 1)$ $(y^{12} + 29y^{11} + \dots + 22y + 1)$
c_3, c_7, c_9	$y^6(y^6 - 3y^5 + 5y^4 - 4y^3 + 2y^2 - y + 1)$ $(y^{12} - 27y^{11} + \dots - 12288y + 4096)(y^{12} - 15y^{11} + \dots - 2y + 1)$
c_5	$(y^6 - 3y^5 + 5y^4 - 4y^3 + 2y^2 - y + 1)(y^6 + 3y^5 + 6y^4 + 5y^2 + y + 1)$ $(y^{12} - 28y^{11} + \dots + 53360y + 5929)$ $(y^{12} - 23y^{11} + \dots - 4098y + 529)$
c_6	$(y^6 + y^5 + 5y^4 + 6y^2 + 3y + 1)(y^6 + 3y^5 + 6y^4 + 5y^2 + y + 1)$ $(y^{12} + 5y^{11} + \dots + 68y + 16)(y^{12} + 24y^{11} + \dots + 28148y + 14641)$
c_{11}	$(y^6 + y^5 + 5y^4 + 6y^2 + 3y + 1)^2(y^6 + y^5 + 5y^4 + 4y^3 + 6y^2 + 3y + 1)^2$ $(y^{12} + y^{11} + \dots + 6y + 1)$