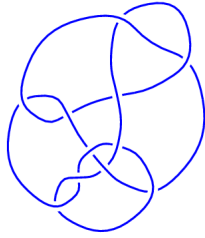
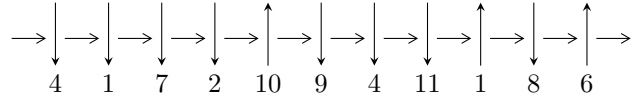


11n₄₁ (K11n₄₁)

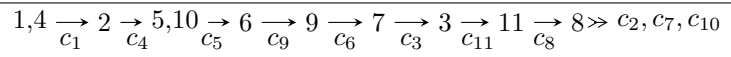


1

Arc Sequences



Solving Sequence



Representation Ideals

$$I = \bigcap_{i=1}^3 I_i^u$$

$$I_1^u = \langle b^6 + b^5 - b^4 - 2b^3 + b + 1, u - 1, -b^4 + 2b^2 + a - 2 \rangle$$

$$I_2^u = \langle u^3 + u^2 - 1, b, -3u^2 + a - 5u - 4 \rangle$$

$$I_3^u = \langle u^{35} + 8u^{34} + \dots + 9u + 1, 5.06381 \times 10^{26}u^{34} + 3.18576 \times 10^{27}u^{33} + \dots + 7.97336 \times 10^{26}b - 1.25386 \times 10^{26} \\ - 4.65925 \times 10^{25}u^{34} + 3.98163 \times 10^{24}u^{33} + \dots + 7.97336 \times 10^{26}a + 6.92161 \times 10^{26} \rangle$$

There are 3 irreducible components with 44 representations.

¹The knot diagram image is adapter from “C. Livingston and A. H. Moore, KnotInfo: Table of Knot Invariants, <http://www.indiana.edu/~knotinfo>”

$$\text{I. } I_1^u = \langle b^6 + b^5 - b^4 - 2b^3 + b + 1, u - 1, -b^4 + 2b^2 + a - 2 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} b^4 - 2b^2 + 2 \\ b \end{pmatrix}$$

$$a_6 = \begin{pmatrix} b^5 - 2b^3 + 2b - 1 \\ b^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} b^4 - 2b^2 - b + 2 \\ b \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ b^4 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} b^4 - 2b^2 + 2 \\ b^4 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ b^4 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ b^4 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$ $a = -0.415113 - 0.381252I$ $b = -1.073950 - 0.558752I$	$-1.64493 + 5.69302I$	$-11.7058 - 8.3306I$
$u = 1.00000$ $a = -0.415113 + 0.381252I$ $b = -1.073950 + 0.558752I$	$-1.64493 - 5.69302I$	$-11.7058 + 8.3306I$
$u = 1.00000$ $a = 2.25915 - 1.43225I$ $b = -0.428243 - 0.664531I$	$-3.53554 - 0.92430I$	$-12.60470 - 5.55069I$
$u = 1.00000$ $a = 2.25915 + 1.43225I$ $b = -0.428243 + 0.664531I$	$-3.53554 + 0.92430I$	$-12.60470 + 5.55069I$
$u = 1.00000$ $a = 0.655968 + 0.098281I$ $b = 1.002193 - 0.295542I$	$0.245672 - 0.924305I$	$-5.68949 + 0.25702I$
$u = 1.00000$ $a = 0.655968 - 0.098281I$ $b = 1.002193 + 0.295542I$	$0.245672 + 0.924305I$	$-5.68949 - 0.25702I$

$$\text{II. } I_2^u = \langle u^3 + u^2 - 1, b, -3u^2 + a - 5u - 4 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u \\ u^2 + u - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 3u^2 + 5u + 4 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 9u^2 + 15u + 12 \\ u^2 + u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 3u^2 + 5u + 4 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u \\ u^2 + u - 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 3u^2 + 6u + 4 \\ -2u^2 - u + 2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u \\ 2u^2 + u - 2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u \\ 2u^2 + u - 2 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.877439 - 0.744862I$ $a = 0.258045 + 0.197115I$ $b = 0$	$1.37919 - 2.82812I$	$-9.0124 + 12.0277I$
$u = -0.877439 + 0.744862I$ $a = 0.258045 - 0.197115I$ $b = 0$	$1.37919 + 2.82812I$	$-9.0124 - 12.0277I$
$u = 0.754878$ $a = 9.48391$ $b = 0$	-2.75839	-102.975

$$\text{III. } I_3^u = \langle u^{35} + 8u^{34} + \dots + 9u + 1, 5.06 \times 10^{26}u^{34} + 3.19 \times 10^{27}u^{33} + \dots + 7.97 \times 10^{26}b - 1.25 \times 10^{26}, -4.66 \times 10^{25}u^{34} + 3.98 \times 10^{24}u^{33} + \dots + 7.97 \times 10^{26}a + 6.92 \times 10^{26} \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.0584352u^{34} - 0.00499367u^{33} + \dots + 87.4344u - 0.868092 \\ -0.635091u^{34} - 3.99551u^{33} + \dots + 1.26311u + 0.157257 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1.72094u^{34} - 17.6948u^{33} + \dots + 67.6060u + 13.1818 \\ -0.291426u^{34} - 1.97724u^{33} + \dots - 9.21351u - 0.566549 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.693526u^{34} + 3.99051u^{33} + \dots + 86.1713u - 1.02535 \\ -0.635091u^{34} - 3.99551u^{33} + \dots + 1.26311u + 0.157257 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.135945u^{34} + 1.32830u^{33} + \dots + 28.8699u - 0.0316372 \\ 0.201606u^{34} + 1.17050u^{33} + \dots + 2.73205u + 0.337551 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.242664u^{34} - 0.573718u^{33} + \dots - 63.3575u - 0.192908 \\ 0.239495u^{34} + 1.52839u^{33} + \dots - 0.429444u - 0.0968115 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0.135945u^{34} + 1.32830u^{33} + \dots + 28.8699u - 0.0316372 \\ -0.239495u^{34} - 1.52839u^{33} + \dots + 0.429444u + 0.0968115 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0.135945u^{34} + 1.32830u^{33} + \dots + 28.8699u - 0.0316372 \\ -0.239495u^{34} - 1.52839u^{33} + \dots + 0.429444u + 0.0968115 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.75068 - 0.06096I$ $a = 0.777922 + 1.044169I$ $b = 1.93922 + 1.67518I$	$-14.4753 - 2.5419I$	$-13.83151 + 2.70823I$
$u = -1.75068 + 0.06096I$ $a = 0.777922 - 1.044169I$ $b = 1.93922 - 1.67518I$	$-14.4753 + 2.5419I$	$-13.83151 - 2.70823I$
$u = -1.72022 - 0.43828I$ $a = 0.296229 + 1.018866I$ $b = -0.61061 + 1.35195I$	$-15.2163 - 5.6356I$	$-10.75742 + 2.79420I$
$u = -1.72022 + 0.43828I$ $a = 0.296229 - 1.018866I$ $b = -0.61061 - 1.35195I$	$-15.2163 + 5.6356I$	$-10.75742 - 2.79420I$
$u = -1.70107 - 0.39786I$ $a = -0.17360 - 1.42986I$ $b = 1.20989 - 1.48650I$	$-15.7071 - 13.7623I$	$-9.89343 + 6.24021I$
$u = -1.70107 + 0.39786I$ $a = -0.17360 + 1.42986I$ $b = 1.20989 + 1.48650I$	$-15.7071 + 13.7623I$	$-9.89343 - 6.24021I$
$u = -1.68600$ $a = 0.808929$ $b = -0.920335$	-11.4779	0.0900530
$u = -1.68299 - 0.18586I$ $a = -0.18783 + 1.58377I$ $b = -1.25568 + 1.90551I$	$-9.90660 - 6.51942I$	$-9.48439 + 5.38265I$
$u = -1.68299 + 0.18586I$ $a = -0.18783 - 1.58377I$ $b = -1.25568 - 1.90551I$	$-9.90660 + 6.51942I$	$-9.48439 - 5.38265I$
$u = -1.63022 - 0.11868I$ $a = -0.279124 - 1.207661I$ $b = 0.397690 - 0.969208I$	$-9.25057 - 1.88240I$	$-8.12432 - 1.64929I$

Solution to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.63022 + 0.11868I$ $a = -0.279124 + 1.207661I$ $b = 0.397690 + 0.969208I$	$-9.25057 + 1.88240I$	$-8.12432 + 1.64929I$
$u = -0.990139 - 0.655507I$ $a = -0.328445 + 0.034132I$ $b = -0.537541 - 0.273251I$	$1.54213 - 2.47872I$	$-0.53499 - 5.93000I$
$u = -0.990139 + 0.655507I$ $a = -0.328445 - 0.034132I$ $b = -0.537541 + 0.273251I$	$1.54213 + 2.47872I$	$-0.53499 + 5.93000I$
$u = -0.686181 - 0.154265I$ $a = 0.838455 + 0.370991I$ $b = 0.977826 + 0.650468I$	$-1.08296 + 5.42643I$	$-0.21975 - 3.30530I$
$u = -0.686181 + 0.154265I$ $a = 0.838455 - 0.370991I$ $b = 0.977826 - 0.650468I$	$-1.08296 - 5.42643I$	$-0.21975 + 3.30530I$
$u = -0.294421 - 0.137620I$ $a = -1.30767 + 1.56416I$ $b = -0.805847 + 0.442462I$	$1.40601 - 1.20005I$	$2.74470 + 1.99044I$
$u = -0.294421 + 0.137620I$ $a = -1.30767 - 1.56416I$ $b = -0.805847 - 0.442462I$	$1.40601 + 1.20005I$	$2.74470 - 1.99044I$
$u = -0.0306219 - 0.0974691I$ $a = -7.02532 - 6.31954I$ $b = 0.458623 - 0.535266I$	$-1.92040 + 0.80331I$	$-4.44102 + 0.15082I$
$u = -0.0306219 + 0.0974691I$ $a = -7.02532 + 6.31954I$ $b = 0.458623 + 0.535266I$	$-1.92040 - 0.80331I$	$-4.44102 - 0.15082I$
$u = 0.605532 - 0.380104I$ $a = -1.43703 - 0.00546I$ $b = -0.043259 + 0.568475I$	$-1.46738 + 0.11420I$	$-8.20214 - 0.34884I$

Solution to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.605532 + 0.380104I$ $a = -1.43703 + 0.00546I$ $b = -0.043259 - 0.568475I$	$-1.46738 - 0.11420I$	$-8.20214 + 0.34884I$
$u = 0.656190 - 1.188229I$ $a = 0.395829 + 0.005674I$ $b = 0.109496 - 1.311600I$	$-7.58070 - 0.56154I$	$-10.57137 + 0.23440I$
$u = 0.656190 + 1.188229I$ $a = 0.395829 - 0.005674I$ $b = 0.109496 + 1.311600I$	$-7.58070 + 0.56154I$	$-10.57137 - 0.23440I$
$u = 0.679243 - 0.583622I$ $a = 0.692444 + 0.020033I$ $b = -0.491434 - 1.250359I$	$-1.63296 + 3.48211I$	$-7.94104 - 7.54592I$
$u = 0.679243 + 0.583622I$ $a = 0.692444 - 0.020033I$ $b = -0.491434 + 1.250359I$	$-1.63296 - 3.48211I$	$-7.94104 + 7.54592I$
$u = 0.704998$ $a = 12.6158$ $b = -0.141812$	-2.72892	194.387
$u = 0.730316 - 1.119096I$ $a = -0.586120 + 0.340107I$ $b = 0.70143 + 1.39478I$	$-7.84770 + 8.00129I$	$-9.44018 - 5.26349I$
$u = 0.730316 + 1.119096I$ $a = -0.586120 - 0.340107I$ $b = 0.70143 - 1.39478I$	$-7.84770 - 8.00129I$	$-9.44018 + 5.26349I$
$u = 0.779230$ $a = -0.816856$ $b = -0.118472$	-1.12597	-9.35809
$u = 0.964380 - 0.326022I$ $a = -1.34533 + 1.00277I$ $b = 1.165204 - 0.364382I$	$-4.47629 + 0.99972I$	$-15.2464 - 0.4133I$

Solution to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.964380 + 0.326022I$ $a = -1.34533 - 1.00277I$ $b = 1.165204 + 0.364382I$	$-4.47629 - 0.99972I$	$-15.2464 + 0.4133I$
$u = 1.204595 - 0.063415I$ $a = -1.45117 + 1.83159I$ $b = -0.035022 + 0.979858I$	$-3.08874 - 1.42303I$	$-6.41632 + 5.79805I$
$u = 1.204595 + 0.063415I$ $a = -1.45117 - 1.83159I$ $b = -0.035022 - 0.979858I$	$-3.08874 + 1.42303I$	$-6.41632 - 5.79805I$
$u = 1.74717 - 0.03675I$ $a = 0.316839 - 1.172532I$ $b = 0.41033 - 1.45360I$	$-10.19429 - 4.27290I$	$-10.69965 + 2.77091I$
$u = 1.74717 + 0.03675I$ $a = 0.316839 + 1.172532I$ $b = 0.41033 + 1.45360I$	$-10.19429 + 4.27290I$	$-10.69965 - 2.77091I$

IV. u-Polynomials

Crossings	u-Polynomials at each crossings
c_1	$(u-1)^6(u^3+u^2-1)(u^{35}+8u^{34}+\dots+9u+1)$
c_2	$(u+1)^6(u^3+u^2+2u+1)(u^{35}+42u^{34}+\dots-129u+1)$
c_3	$u^6(u^3-u^2+2u-1)(u^{35}+2u^{34}+\dots-320u-64)$
c_4	$(u+1)^6(u^3-u^2+1)(u^{35}+8u^{34}+\dots+9u+1)$
c_5	$(u^3+2u^2-3u+1)(u^6-u^5-u^4+2u^3-u+1)$ $(u^{35}+4u^{34}+\dots+1417u-1219)$
c_6	$(u^3+2u^2-3u+1)(u^6-3u^5+5u^4-4u^3+2u^2-u+1)$ $(u^{35}+8u^{34}+\dots+73u-31)$
c_7	$u^6(u^3+u^2+2u+1)(u^{35}+2u^{34}+\dots-320u-64)$
c_8	$(u-1)^3(u^6+u^5+\dots+u+1)(u^{35}+5u^{34}+\dots+67u+1)$
c_9	$u^3(u^6-u^5+\dots-u+1)(u^{35}+6u^{34}+\dots+124u-8)$
c_{10}	$(u+1)^3(u^6-u^5+\dots-u+1)(u^{35}+5u^{34}+\dots+67u+1)$
c_{11}	$(u^3+3u^2+2u-1)(u^6-3u^5+5u^4-4u^3+2u^2-u+1)$ $(u^{35}+3u^{34}+\dots+2u+1)$

V. Riley Polynomials

Crossings	Riley Polynomials at each crossings
c_1, c_4	$(y-1)^6(y^3 - y^2 + 2y - 1)(y^{35} - 42y^{34} + \dots - 129y - 1)$
c_2	$(y-1)^6(y^3 + 3y^2 + 2y - 1)(y^{35} - 90y^{34} + \dots + 6323y - 1)$
c_3, c_7	$y^6(y^3 + 3y^2 + 2y - 1)(y^{35} - 36y^{34} + \dots - 20480y - 4096)$
c_5	$(y^3 - 10y^2 + 5y - 1)(y^6 - 3y^5 + 5y^4 - 4y^3 + 2y^2 - y + 1)$ $(y^{35} - 4y^{34} + \dots + 25178641y - 1485961)$
c_6	$(y^3 - 10y^2 + 5y - 1)(y^6 + y^5 + 5y^4 + 6y^2 + 3y + 1)$ $(y^{35} - 52y^{34} + \dots + 29509y - 961)$
c_8, c_{10}	$(y-1)^3(y^6 - 3y^5 + 5y^4 - 4y^3 + 2y^2 - y + 1)$ $(y^{35} - 33y^{34} + \dots + 5091y - 1)$
c_9	$y^3(y^6 - 3y^5 + \dots - y + 1)(y^{35} + 18y^{34} + \dots + 7312y - 64)$
c_{11}	$(y^3 - 5y^2 + 10y - 1)(y^6 + y^5 + 5y^4 + 6y^2 + 3y + 1)$ $(y^{35} + y^{34} + \dots + 14y - 1)$