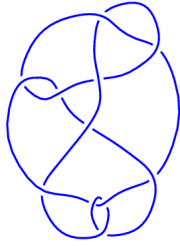
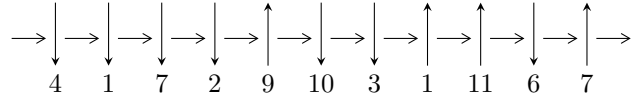


11n<sub>51</sub> (K11n<sub>51</sub>)

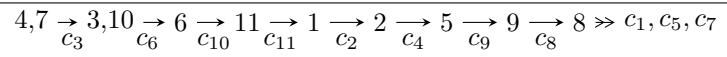


1

**Arc Sequences**



**Solving Sequence**



**Representation Ideals**

$$I = I_1^u \cap I_1^v$$

$$I_1^u = \langle u^{19} + u^{18} + \dots + 32u + 32, 3.89161 \times 10^{18}u^{18} - 1.25291 \times 10^{19}u^{17} + \dots + 1.19579 \times 10^{21}a - 2.43773 \times 10^{20} \\ 4.27694 \times 10^{19}u^{18} + 2.93614 \times 10^{19}u^{17} + \dots + 2.39158 \times 10^{21}b + 7.99100 \times 10^{20} \rangle$$

$$I_1^v = \langle -v^3 + b + 2v, v^5 + v^4 - 2v^3 - v^2 + v - 1, a \rangle$$

There are 2 irreducible components with 24 representations.

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<sup>1</sup>The knot diagram image is adapter from “C. Livingston and A. H. Moore, KnotInfo: Table of Knot Invariants, <http://www.indiana.edu/~knotinfo>”

$$\begin{aligned} & \mathbf{I. } I_1^u = \\ & \langle u^{19} + u^{18} + \dots + 32u + 32, 3.89 \times 10^{18}u^{18} - 1.25 \times 10^{19}u^{17} + \dots + 1.20 \times 10^{21}a - \\ & 2.44 \times 10^{21}, 4.28 \times 10^{19}u^{18} + 2.94 \times 10^{19}u^{17} + \dots + 2.39 \times 10^{21}b + 7.99 \times 10^{20} \rangle \end{aligned}$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -0.00325443u^{18} + 0.0104777u^{17} + \dots + 1.47789u + 2.03859 \\ -0.0178833u^{18} - 0.0122770u^{17} + \dots + 0.528252u - 0.334131 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0.0334283u^{18} + 0.0315554u^{17} + \dots + 2.33117u - 0.293509 \\ -0.00547265u^{18} + 0.00812761u^{17} + \dots + 0.354335u + 0.00511905 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.0126757u^{18} - 0.0158711u^{17} + \dots - 0.965637u + 0.712666 \\ -0.0119895u^{18} - 0.00312216u^{17} + \dots - 0.280593u - 0.182519 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.0126757u^{18} - 0.0158711u^{17} + \dots - 0.965637u + 0.712666 \\ -0.0154120u^{18} - 0.0118073u^{17} + \dots - 0.788470u - 0.284774 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.00273632u^{18} - 0.00406381u^{17} + \dots - 0.177167u + 0.997440 \\ -0.0154120u^{18} - 0.0118073u^{17} + \dots - 0.788470u - 0.284774 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -0.0246651u^{18} - 0.0189933u^{17} + \dots - 1.24623u + 0.530148 \\ 0.0119895u^{18} + 0.00312216u^{17} + \dots + 0.280593u + 0.182519 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -0.00225903u^{18} + 0.00481394u^{17} + \dots + 0.299894u + 0.940474 \\ -0.00680013u^{18} - 0.00393377u^{17} + \dots + 0.909878u - 0.0875624 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.66687 - 1.26708I$ $a = -0.868526 - 0.181292I$ $b = 2.01097 - 0.37234I$	$6.61331 - 2.23643I$	$3.68670 + 1.85634I$
$u = -0.66687 + 1.26708I$ $a = -0.868526 + 0.181292I$ $b = 2.01097 + 0.37234I$	$6.61331 + 2.23643I$	$3.68670 - 1.85634I$
$u = -0.559824$ $a = 0.520700$ $b = -0.696990$	$-1.12234$	$-9.25558$
$u = -0.55184 - 2.12917I$ $a = 0.624151 - 0.075817I$ $b = -3.70077 - 0.64779I$	$17.2204 - 9.5042I$	$1.84766 + 4.86373I$
$u = -0.55184 + 2.12917I$ $a = 0.624151 + 0.075817I$ $b = -3.70077 + 0.64779I$	$17.2204 + 9.5042I$	$1.84766 - 4.86373I$
$u = -0.377279 - 0.570351I$ $a = 0.928450 + 0.852722I$ $b = -1.60892 - 0.88722I$	$-0.904771 + 0.899537I$	$0.47063 + 1.75855I$
$u = -0.377279 + 0.570351I$ $a = 0.928450 - 0.852722I$ $b = -1.60892 + 0.88722I$	$-0.904771 - 0.899537I$	$0.47063 - 1.75855I$
$u = -0.33784 - 2.24339I$ $a = -0.540132 - 0.287132I$ $b = 3.20814 - 0.98987I$	$17.5665 + 0.7457I$	$2.31305 - 0.82283I$
$u = -0.33784 + 2.24339I$ $a = -0.540132 + 0.287132I$ $b = 3.20814 + 0.98987I$	$17.5665 - 0.7457I$	$2.31305 + 0.82283I$
$u = -0.118930 - 1.200608I$ $a = 0.902998 + 0.509171I$ $b = -1.28119 + 1.32428I$	$5.36309 + 6.16703I$	$2.22619 - 6.06641I$

Solution to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.118930 + 1.200608I$ $a = 0.902998 - 0.509171I$ $b = -1.28119 - 1.32428I$	$5.36309 - 6.16703I$	$2.22619 + 6.06641I$
$u = 0.113652 - 0.545215I$ $a = 1.25949 - 1.01771I$ $b = 0.107580 - 0.561696I$	$0.05095 - 1.76235I$	$0.18768 + 4.49049I$
$u = 0.113652 + 0.545215I$ $a = 1.25949 + 1.01771I$ $b = 0.107580 + 0.561696I$	$0.05095 + 1.76235I$	$0.18768 - 4.49049I$
$u = 0.349333 - 1.064248I$ $a = 0.342118 + 0.593985I$ $b = 0.144940 + 0.182376I$	$2.51975 - 1.53406I$	$-0.31883 + 1.85733I$
$u = 0.349333 + 1.064248I$ $a = 0.342118 - 0.593985I$ $b = 0.144940 - 0.182376I$	$2.51975 + 1.53406I$	$-0.31883 - 1.85733I$
$u = 0.42263 - 2.12489I$ $a = -0.069295 - 0.437160I$ $b = 0.299792 + 0.326685I$	$13.37814 + 4.28212I$	$-1.00628 - 2.00074I$
$u = 0.42263 + 2.12489I$ $a = -0.069295 + 0.437160I$ $b = 0.299792 - 0.326685I$	$13.37814 - 4.28212I$	$-1.00628 + 2.00074I$
$u = 0.947060 - 0.059794I$ $a = -0.339607 + 1.065378I$ $b = 0.667953 + 0.197417I$	$1.26128 + 2.36565I$	$1.22099 - 4.76618I$
$u = 0.947060 + 0.059794I$ $a = -0.339607 - 1.065378I$ $b = 0.667953 - 0.197417I$	$1.26128 - 2.36565I$	$1.22099 + 4.76618I$

$$\text{II. } I_1^v = \langle -v^3 + b + 2v, v^5 + v^4 - 2v^3 - v^2 + v - 1, a \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ v^3 - 2v \end{pmatrix}$$

$$a_6 = \begin{pmatrix} v \\ -v^2 + 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} v^4 - v^2 + v - 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} v^4 - 2v^2 + v - 1 \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} v^4 - 2v^2 + v \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -v^4 + 2v^2 - v + 1 \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -v^4 + 2v^2 - v + 1 \\ -v \end{pmatrix}$$

$$a_8 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to $I_1^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = -1.41878 - 0.21917I$ $a = 0$ $b = 0.186078 - 0.874646I$	$4.22763 + 4.40083I$	$1.17182 - 3.02310I$
$v = -1.41878 + 0.21917I$ $a = 0$ $b = 0.186078 + 0.874646I$	$4.22763 - 4.40083I$	$1.17182 + 3.02310I$
$v = 0.309916 - 0.549911I$ $a = 0$ $b = -0.871221 + 1.107662I$	$-1.31583 - 1.53058I$	$-6.99101 + 6.23673I$
$v = 0.309916 + 0.549911I$ $a = 0$ $b = -0.871221 - 1.107662I$	$-1.31583 + 1.53058I$	$-6.99101 - 6.23673I$
$v = 1.21774$ $a = 0$ $b = -0.629714$	$0.756147$	$-2.36161$

### III. u-Polynomials

Crossings	u-Polynomials at each crossings
$c_1$	$(u - 1)^5(u^{19} + 6u^{18} + \dots - 6u - 1)$
$c_2$	$(u + 1)^5(u^{19} + 22u^{17} + \dots + 10u + 1)$
$c_3, c_7$	$u^5(u^{19} + u^{18} + \dots + 32u + 32)$
$c_4$	$(u + 1)^5(u^{19} + 6u^{18} + \dots - 6u - 1)$
$c_5$	$(u^5 - u^4 + \dots + u + 1)(u^{19} + 2u^{18} + \dots + 2u - 1)$
$c_6$	$(u^5 + u^4 + \dots + u + 1)(u^{19} + 2u^{18} + \dots + 4u + 1)$
$c_8$	$(u^5 - u^4 + \dots + u + 1)(u^{19} + 8u^{18} + \dots + 3614u - 53)$
$c_9$	$(u^5 + 3u^4 + \dots - u - 1)(u^{19} + 12u^{18} + \dots + 8u - 1)$
$c_{10}$	$(u^5 - u^4 + \dots + u - 1)(u^{19} + 2u^{18} + \dots + 4u + 1)$
$c_{11}$	$(u^5 + u^4 + \dots + u - 1)(u^{19} + 2u^{18} + \dots + 2u - 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossings
$c_1, c_4$	$(y - 1)^5(y^{19} + 22y^{17} + \dots + 10y - 1)$
$c_2$	$(y - 1)^5(y^{19} + 44y^{18} + \dots - 82y - 1)$
$c_3, c_7$	$y^5(y^{19} + 33y^{18} + \dots - 6656y - 1024)$
$c_5, c_{11}$	$(y^5 - 5y^4 + \dots - y - 1)(y^{19} - 28y^{18} + \dots + 8y - 1)$
$c_6, c_{10}$	$(y^5 + 3y^4 + \dots - y - 1)(y^{19} + 12y^{18} + \dots + 8y - 1)$
$c_8$	$(y^5 - 5y^4 + \dots - y - 1)(y^{19} - 88y^{18} + \dots + 1.13576 \times 10^7 y - 2809)$
$c_9$	$(y^5 - y^4 + \dots + 3y - 1)(y^{19} - 8y^{18} + \dots + 148y - 1)$