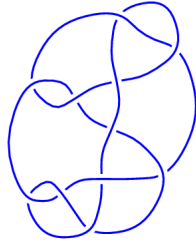
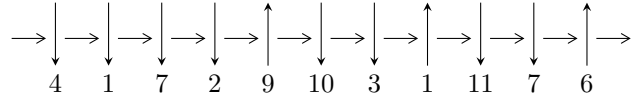


11n₅₄ (K11n₅₄)

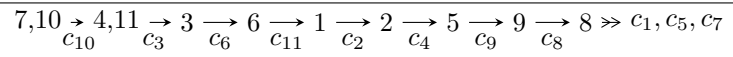


1

Arc Sequences



Solving Sequence



Representation Ideals

$$I = I_1^u \cap I_1^v$$

$$I_1^u = \langle u^{27} + u^{26} + \dots + 128u + 64, 2.25883 \times 10^{34}u^{26} + 6.71521 \times 10^{34}u^{25} + \dots + 4.81127 \times 10^{36}b - 1.68358 \times 10^{37} - 3.23949 \times 10^{35}u^{26} - 1.41213 \times 10^{35}u^{25} + \dots + 9.62254 \times 10^{36}a + 1.69205 \times 10^{37} \rangle$$

$$I_1^v = \langle v^4 - v^2 + b + 1, v^6 + v^5 - v^4 - 2v^3 + v + 1, a \rangle$$

There are 2 irreducible components with 33 representations.

¹The knot diagram image is adapter from “C. Livingston and A. H. Moore, KnotInfo: Table of Knot Invariants, <http://www.indiana.edu/~knotinfo>”

$$\langle u^{27} + u^{26} + \dots + 128u + 64, 2.26 \times 10^{34} u^{26} + 6.72 \times 10^{34} u^{25} + \dots + 4.81 \times 10^{36} b - 1.68 \times 10^{36}, -3.24 \times 10^{35} u^{26} - 1.41 \times 10^{35} u^{25} + \dots + 9.62 \times 10^{36} a + 1.69 \times 10^{37} \rangle$$

I. $I_1^u =$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.0336657u^{26} + 0.0146752u^{25} + \dots + 0.158474u - 1.75842 \\ -0.00469488u^{26} - 0.0139573u^{25} + \dots + 4.87475u + 0.349924 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.0336657u^{26} + 0.0146752u^{25} + \dots + 0.158474u - 1.75842 \\ -0.0142207u^{26} - 0.0154764u^{25} + \dots + 5.15092u + 1.56531 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.0371213u^{26} - 0.0414337u^{25} + \dots - 10.4975u - 2.60349 \\ -0.0413740u^{26} - 0.0246607u^{25} + \dots + 2.44720u + 2.28218 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0.0118157u^{26} + 0.0162794u^{25} + \dots + 4.26934u + 2.02994 \\ -0.00887124u^{26} + 0.00394903u^{25} + \dots + 5.49294u + 2.17103 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.0206870u^{26} + 0.0123303u^{25} + \dots - 1.22360u - 0.141092 \\ -0.00887124u^{26} + 0.00394903u^{25} + \dots + 5.49294u + 2.17103 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -0.00426849u^{26} + 0.0131278u^{25} + \dots + 8.43473u + 3.91529 \\ 0.0160842u^{26} + 0.00315151u^{25} + \dots - 4.16539u - 1.88536 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.00661984u^{26} - 0.00830158u^{25} + \dots - 2.05650u - 1.94409 \\ -0.00835665u^{26} - 0.0259380u^{25} + \dots - 2.78903u - 1.32397 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.916936 - 0.740217I$ $a = -0.978245 + 0.140900I$ $b = 1.94712 + 0.16829I$	$1.53114 - 4.74698I$	$-2.05877 + 5.37624I$
$u = -0.916936 + 0.740217I$ $a = -0.978245 - 0.140900I$ $b = 1.94712 - 0.16829I$	$1.53114 + 4.74698I$	$-2.05877 - 5.37624I$
$u = -0.756621 - 0.053719I$ $a = 0.947761 + 0.339256I$ $b = -1.280090 - 0.221628I$	$-1.077413 - 0.093546I$	$-6.21440 - 0.06252I$
$u = -0.756621 + 0.053719I$ $a = 0.947761 - 0.339256I$ $b = -1.280090 + 0.221628I$	$-1.077413 + 0.093546I$	$-6.21440 + 0.06252I$
$u = -0.591296$ $a = 0.672828$ $b = -0.867515$	-1.09734	-8.57437
$u = -0.52916 - 1.90711I$ $a = 0.462320 - 0.451922I$ $b = -2.81680 - 2.09025I$	$9.8976 - 11.4401I$	$-3.60368 + 6.65783I$
$u = -0.52916 + 1.90711I$ $a = 0.462320 + 0.451922I$ $b = -2.81680 + 2.09025I$	$9.8976 + 11.4401I$	$-3.60368 - 6.65783I$
$u = -0.31974 - 1.83076I$ $a = -0.087922 + 0.626844I$ $b = 0.92863 + 2.70225I$	$5.98407 - 3.79755I$	$-6.46791 + 2.18250I$
$u = -0.31974 + 1.83076I$ $a = -0.087922 - 0.626844I$ $b = 0.92863 - 2.70225I$	$5.98407 + 3.79755I$	$-6.46791 - 2.18250I$
$u = -0.14157 - 2.04029I$ $a = -0.286400 - 0.546539I$ $b = 1.41202 - 2.19032I$	$10.52734 + 3.36992I$	$-2.71394 - 2.50695I$

Solution to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.14157 + 2.04029I$ $a = -0.286400 + 0.546539I$ $b = 1.41202 + 2.19032I$	$10.52734 - 3.36992I$	$-2.71394 + 2.50695I$
$u = -0.099608 - 0.648052I$ $a = 0.67781 - 1.53140I$ $b = 0.014762 - 1.397672I$	$-2.30226 - 0.55935I$	$-5.41913 - 0.15707I$
$u = -0.099608 + 0.648052I$ $a = 0.67781 + 1.53140I$ $b = 0.014762 + 1.397672I$	$-2.30226 + 0.55935I$	$-5.41913 + 0.15707I$
$u = -0.065099 - 0.869686I$ $a = 0.521552 + 1.307380I$ $b = -0.62639 + 1.84157I$	$-0.58075 + 6.65503I$	$-3.43691 - 7.46005I$
$u = -0.065099 + 0.869686I$ $a = 0.521552 - 1.307380I$ $b = -0.62639 - 1.84157I$	$-0.58075 - 6.65503I$	$-3.43691 + 7.46005I$
$u = 0.210916 - 0.867503I$ $a = 0.837971 + 0.172931I$ $b = 0.285706 - 0.077541I$	$1.66847 - 1.93992I$	$0.12713 + 2.72762I$
$u = 0.210916 + 0.867503I$ $a = 0.837971 - 0.172931I$ $b = 0.285706 + 0.077541I$	$1.66847 + 1.93992I$	$0.12713 - 2.72762I$
$u = 0.24190 - 2.02768I$ $a = -0.434808 - 0.207968I$ $b = 0.506970 - 0.092441I$	$12.17430 + 2.19817I$	$-0.63423 - 2.08830I$
$u = 0.24190 + 2.02768I$ $a = -0.434808 + 0.207968I$ $b = 0.506970 + 0.092441I$	$12.17430 - 2.19817I$	$-0.63423 + 2.08830I$
$u = 0.247086 - 0.712064I$ $a = 0.909883 + 0.972277I$ $b = -1.87921 - 0.63112I$	$-2.84916 + 1.60658I$	$-4.88146 - 5.04321I$

Solution to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.247086 + 0.712064I$ $a = 0.909883 - 0.972277I$ $b = -1.87921 + 0.63112I$	$-2.84916 - 1.60658I$	$-4.88146 + 5.04321I$
$u = 0.45786 - 1.94824I$ $a = 0.356806 - 0.323757I$ $b = -0.086723 + 0.461433I$	$11.82207 + 5.91141I$	$-1.03607 - 2.33228I$
$u = 0.45786 + 1.94824I$ $a = 0.356806 + 0.323757I$ $b = -0.086723 - 0.461433I$	$11.82207 - 5.91141I$	$-1.03607 + 2.33228I$
$u = 0.682025 - 0.833060I$ $a = -0.129773 + 0.803497I$ $b = 0.052629 + 0.131638I$	$2.76848 - 0.13713I$	$0.773547 + 0.780119I$
$u = 0.682025 + 0.833060I$ $a = -0.129773 - 0.803497I$ $b = 0.052629 - 0.131638I$	$2.76848 + 0.13713I$	$0.773547 - 0.780119I$
$u = 0.784593 - 0.468587I$ $a = -0.633364 - 1.013310I$ $b = 1.47514 + 0.10710I$	$-2.13464 - 3.70052I$	$-7.14700 + 4.32876I$
$u = 0.784593 + 0.468587I$ $a = -0.633364 + 1.013310I$ $b = 1.47514 - 0.10710I$	$-2.13464 + 3.70052I$	$-7.14700 - 4.32876I$

$$\text{II. } I_1^v = \langle v^4 - v^2 + b + 1, v^6 + v^5 - v^4 - 2v^3 + v + 1, a \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ -v^4 + v^2 - 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -v^5 + 2v^3 + v^2 - v - 1 \\ -v^4 + v^2 - 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} v \\ -v^2 + 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -v^5 + v^3 + v^2 - v - 1 \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -v^5 + v^3 + v^2 - v \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} v^5 - v^3 - v^2 + v + 1 \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} v^5 - v^3 - v^2 + v + 1 \\ -v \end{pmatrix}$$

$$a_8 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_1^v	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = -1.073950 - 0.558752I$		
$a = 0$	$-1.64493 + 5.69302I$	$-6.76721 - 4.86918I$
$b = 0.573950 - 0.818891I$		
$v = -1.073950 + 0.558752I$		
$a = 0$	$-1.64493 - 5.69302I$	$-6.76721 + 4.86918I$
$b = 0.573950 + 0.818891I$		
$v = -0.428243 - 0.664531I$		
$a = 0$	$-3.53554 - 0.92430I$	$-12.63596 - 0.09369I$
$b = -1.000936 + 0.863088I$		
$v = -0.428243 + 0.664531I$		
$a = 0$	$-3.53554 + 0.92430I$	$-12.63596 + 0.09369I$
$b = -1.000936 - 0.863088I$		
$v = 1.002193 - 0.295542I$		
$a = 0$	$0.245672 - 0.924305I$	$-2.59683 + 0.69886I$
$b = -0.573013 + 0.494098I$		
$v = 1.002193 + 0.295542I$		
$a = 0$	$0.245672 + 0.924305I$	$-2.59683 - 0.69886I$
$b = -0.573013 - 0.494098I$		

III. u-Polynomials

Crossings	u-Polynomials at each crossings
c_1	$(u - 1)^6(u^{27} + 7u^{26} + \dots - 5u - 1)$
c_2	$(u + 1)^6(u^{27} + 3u^{26} + \dots + 5u + 1)$
c_3, c_7	$u^6(u^{27} + u^{26} + \dots + 128u + 64)$
c_4	$(u + 1)^6(u^{27} + 7u^{26} + \dots - 5u - 1)$
c_5	$(u^6 - u^5 + \dots - u + 1)(u^{27} + 2u^{26} + \dots + 2u - 1)$
c_6	$(u^6 + u^5 + \dots + u + 1)(u^{27} + 2u^{26} + \dots + 4u + 1)$
c_8	$(u^6 - u^5 + \dots - u + 1)(u^{27} + 8u^{26} + \dots + 16990u + 565)$
c_9	$(u^6 - 3u^5 + \dots - u + 1)(u^{27} + 12u^{26} + \dots + 12u + 1)$
c_{10}	$(u^6 - u^5 + \dots - u + 1)(u^{27} + 2u^{26} + \dots + 4u + 1)$
c_{11}	$(u^6 - 3u^5 + \dots - u + 1)(u^{27} + 6u^{26} + \dots + 48u + 5)$

IV. Riley Polynomials

Crossings	Riley Polynomials at each crossings
c_1, c_4	$(y - 1)^6(y^{27} - 3y^{26} + \dots + 5y - 1)$
c_2	$(y - 1)^6(y^{27} + 49y^{26} + \dots - 23y - 1)$
c_3, c_7	$y^6(y^{27} + 39y^{26} + \dots - 28672y - 4096)$
c_5	$(y^6 - 3y^5 + \dots - y + 1)(y^{27} - 36y^{26} + \dots + 12y - 1)$
c_6, c_{10}	$(y^6 - 3y^5 + \dots - y + 1)(y^{27} - 12y^{26} + \dots + 12y - 1)$
c_8	$(y^6 - 3y^5 + 5y^4 - 4y^3 + 2y^2 - y + 1)$ $(y^{27} - 72y^{26} + \dots + 171458760y - 319225)$
c_9	$(y^6 + y^5 + \dots + 3y + 1)(y^{27} + 8y^{26} + \dots + 32y - 1)$
c_{11}	$(y^6 + y^5 + \dots + 3y + 1)(y^{27} - 4y^{26} + \dots + 504y - 25)$