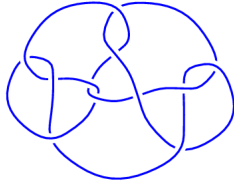
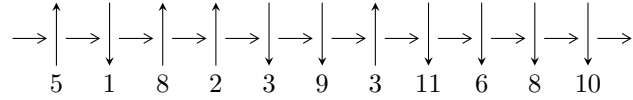


11n<sub>7</sub> (K11n<sub>7</sub>)

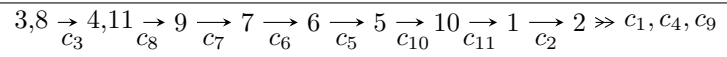


1

**Arc Sequences**



**Solving Sequence**



**Representation Ideals**

$$I = I_1^u \cap I_1^v$$

$$I_1^u = \langle u^{39} - 3u^{38} + \dots + 160u - 64, \\ -1.35871 \times 10^{74}u^{38} + 4.22296 \times 10^{74}u^{37} + \dots + 6.78965 \times 10^{75}b - 7.58203 \times 10^{75}, \\ 1.97322 \times 10^{74}u^{38} - 5.74566 \times 10^{74}u^{37} + \dots + 1.35793 \times 10^{76}a + 2.27616 \times 10^{76} \rangle$$

$$I_1^v = \langle b^6 + 3b^5 + 7b^4 + 4b^3 + b^2 + 2b + 1, -19b^5 - 45b^4 - 105b^3 - 11b^2 - 15b + v - 30, a \rangle$$

There are 2 irreducible components with 45 representations.

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<sup>1</sup>The knot diagram image is adapter from “C. Livingston and A. H. Moore, KnotInfo: Table of Knot Invariants, <http://www.indiana.edu/~knotinfo>”

$$\mathbf{I. } I_1^u = \langle u^{39} - 3u^{38} + \dots + 160u - 64, -1.36 \times 10^{74}u^{38} + 4.22 \times 10^{74}u^{37} + \dots + 6.79 \times 10^{75}b - 7.58 \times 10^{75}, 1.97 \times 10^{74}u^{38} - 5.75 \times 10^{74}u^{37} + \dots + 1.36 \times 10^{76}a + 2.28 \times 10^{76} \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.0145311u^{38} + 0.0423119u^{37} + \dots + 4.20910u - 1.67620 \\ 0.0200115u^{38} - 0.0621970u^{37} + \dots - 9.61102u + 1.11671 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -0.0207767u^{38} + 0.0602462u^{37} + \dots + 2.06543u - 0.671114 \\ 0.0162503u^{38} - 0.0497470u^{37} + \dots - 7.62454u + 0.958859 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0.00471591u^{38} - 0.00996442u^{37} + \dots + 5.08469u - 0.806754 \\ 0.00561330u^{38} - 0.0187349u^{37} + \dots - 2.86181u + 0.381508 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0.0103292u^{38} - 0.0286993u^{37} + \dots + 2.22288u - 0.425246 \\ 0.00561330u^{38} - 0.0187349u^{37} + \dots - 2.86181u + 0.381508 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -0.0145311u^{38} + 0.0423119u^{37} + \dots + 4.20910u - 1.67620 \\ 0.0200871u^{38} - 0.0633748u^{37} + \dots - 8.88605u + 1.19871 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.0103292u^{38} + 0.0286993u^{37} + \dots - 2.22288u + 0.425246 \\ 0.00178031u^{38} - 0.00566997u^{37} + \dots - 2.56686u + 0.527957 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.000822752u^{38} + 0.00351950u^{37} + \dots + 2.47747u + 0.115491 \\ -0.00249633u^{38} + 0.00737375u^{37} + \dots + 1.50215u + 0.140681 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.000822752u^{38} + 0.00351950u^{37} + \dots + 2.47747u + 0.115491 \\ -0.00249633u^{38} + 0.00737375u^{37} + \dots + 1.50215u + 0.140681 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

| Solution to $I_1^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|---|---------------------------------------|-----------------------|
| $u = -1.015771 - 0.563299I$<br>$a = -0.400629 + 0.467419I$<br>$b = -0.589409 - 0.852841I$ | $1.33536 + 1.46808I$                  | $4.04275 - 4.37387I$  |
| $u = -1.015771 + 0.563299I$<br>$a = -0.400629 - 0.467419I$<br>$b = -0.589409 + 0.852841I$ | $1.33536 - 1.46808I$                  | $4.04275 + 4.37387I$  |
| $u = -0.764144 - 0.288695I$<br>$a = 1.26262 - 0.65906I$<br>$b = -0.15031 + 1.56666I$      | $-2.82585 + 1.96097I$                 | $-4.21009 - 0.40138I$ |
| $u = -0.764144 + 0.288695I$<br>$a = 1.26262 + 0.65906I$<br>$b = -0.15031 - 1.56666I$      | $-2.82585 - 1.96097I$                 | $-4.21009 + 0.40138I$ |
| $u = -0.58641 - 1.60233I$<br>$a = 0.021261 + 0.795333I$<br>$b = -0.05289 - 2.62347I$      | $-5.09332 + 8.17367I$                 | $-3.75441 - 5.17214I$ |
| $u = -0.58641 + 1.60233I$<br>$a = 0.021261 - 0.795333I$<br>$b = -0.05289 + 2.62347I$      | $-5.09332 - 8.17367I$                 | $-3.75441 + 5.17214I$ |
| $u = -0.525627 - 0.805732I$<br>$a = -0.429621 + 0.235494I$<br>$b = 0.035751 - 0.891969I$  | $1.15178 + 1.50599I$                  | $2.56109 - 2.72315I$  |
| $u = -0.525627 + 0.805732I$<br>$a = -0.429621 - 0.235494I$<br>$b = 0.035751 + 0.891969I$  | $1.15178 - 1.50599I$                  | $2.56109 + 2.72315I$  |
| $u = -0.391025 - 0.528783I$<br>$a = 0.25451 + 1.68510I$<br>$b = 0.000923 - 0.452010I$     | $2.88333 + 1.52566I$                  | $-2.95623 - 6.42875I$ |
| $u = -0.391025 + 0.528783I$<br>$a = 0.25451 - 1.68510I$<br>$b = 0.000923 + 0.452010I$     | $2.88333 - 1.52566I$                  | $-2.95623 + 6.42875I$ |

| Solution to $I_1^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|--|---------------------------------------|-----------------------|
| $u = -0.362636 - 1.289161I$<br>$a = -0.653617 - 0.135764I$<br>$b = 0.1117599 - 0.0736303I$ | $-1.45248 + 3.13609I$                 | $-0.74981 - 2.49452I$ |
| $u = -0.362636 + 1.289161I$<br>$a = -0.653617 + 0.135764I$<br>$b = 0.1117599 + 0.0736303I$ | $-1.45248 - 3.13609I$                 | $-0.74981 + 2.49452I$ |
| $u = -0.32507 - 1.55745I$<br>$a = -0.191541 - 0.850101I$<br>$b = -0.68404 + 2.14659I$      | $-8.99304 + 6.36082I$                 | $-7.31007 - 4.20770I$ |
| $u = -0.32507 + 1.55745I$<br>$a = -0.191541 + 0.850101I$<br>$b = -0.68404 - 2.14659I$      | $-8.99304 - 6.36082I$                 | $-7.31007 + 4.20770I$ |
| $u = -0.277331 - 0.646400I$<br>$a = -1.58033 + 0.79557I$<br>$b = -0.375450 - 0.246768I$    | $2.42328 - 4.44150I$                  | $-7.41017 + 1.05267I$ |
| $u = -0.277331 + 0.646400I$<br>$a = -1.58033 - 0.79557I$<br>$b = -0.375450 + 0.246768I$    | $2.42328 + 4.44150I$                  | $-7.41017 - 1.05267I$ |
| $u = 0.023739 - 0.376403I$<br>$a = 0.00176 - 2.42806I$<br>$b = 0.45391 + 3.98939I$         | $-1.32570 - 2.15384I$                 | $-38.3073 + 0.3658I$  |
| $u = 0.023739 + 0.376403I$<br>$a = 0.00176 + 2.42806I$<br>$b = 0.45391 - 3.98939I$         | $-1.32570 + 2.15384I$                 | $-38.3073 - 0.3658I$  |
| $u = 0.08279 - 1.46418I$<br>$a = 0.642531 - 0.155659I$<br>$b = 0.115784 - 0.127405I$       | $-5.68977 + 0.80789I$                 | $-5.63151 - 0.39749I$ |
| $u = 0.08279 + 1.46418I$<br>$a = 0.642531 + 0.155659I$<br>$b = 0.115784 + 0.127405I$       | $-5.68977 - 0.80789I$                 | $-5.63151 + 0.39749I$ |

| Solution to $I_1^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|---|---------------------------------------|-----------------------|
| $u = 0.101788 - 1.392135I$<br>$a = 0.258295 - 0.919920I$<br>$b = 0.65375 + 2.18067I$    | $-5.43179 - 1.52389I$                 | $-4.49323 + 0.71316I$ |
| $u = 0.101788 + 1.392135I$<br>$a = 0.258295 + 0.919920I$<br>$b = 0.65375 - 2.18067I$    | $-5.43179 + 1.52389I$                 | $-4.49323 - 0.71316I$ |
| $u = 0.14680 - 1.57664I$<br>$a = -0.340464 - 0.843420I$<br>$b = -0.62348 + 2.12772I$    | $-9.33600 - 3.03011I$                 | $-7.58951 + 2.63816I$ |
| $u = 0.14680 + 1.57664I$<br>$a = -0.340464 + 0.843420I$<br>$b = -0.62348 - 2.12772I$    | $-9.33600 + 3.03011I$                 | $-7.58951 - 2.63816I$ |
| $u = 0.274747$<br>$a = -3.03443$<br>$b = 0.503610$                                      | $-1.20362$                            | $-8.91674$            |
| $u = 0.40659 - 1.39442I$<br>$a = 0.345713 + 0.549146I$<br>$b = -0.00006 - 2.05405I$     | $0.05191 + 4.16636I$                  | $-0.57665 - 9.00427I$ |
| $u = 0.40659 + 1.39442I$<br>$a = 0.345713 - 0.549146I$<br>$b = -0.00006 + 2.05405I$     | $0.05191 - 4.16636I$                  | $-0.57665 + 9.00427I$ |
| $u = 0.45680 - 1.86686I$<br>$a = -0.031347 + 0.713289I$<br>$b = 0.03721 - 2.58839I$     | $-10.41507 - 3.75787I$                | $-8.66055 + 3.06635I$ |
| $u = 0.45680 + 1.86686I$<br>$a = -0.031347 - 0.713289I$<br>$b = 0.03721 + 2.58839I$     | $-10.41507 + 3.75787I$                | $-8.66055 - 3.06635I$ |
| $u = 0.51700 - 1.43416I$<br>$a = 0.666754 - 0.161021I$<br>$b = -0.0860983 + 0.1075653I$ | $-4.49350 - 8.17612I$                 | $-3.77298 + 5.44747I$ |

| Solution to $I_1^u$           | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-------------------------------|---------------------------------------|-----------------------|
| $u = 0.51700 + 1.43416I$      |                                       |                       |
| $a = 0.666754 + 0.161021I$    | $-4.49350 + 8.17612I$                 | $-3.77298 - 5.44747I$ |
| $b = -0.0860983 - 0.1075653I$ |                                       |                       |
| $u = 0.612697 - 0.489080I$    |                                       |                       |
| $a = -1.115050 - 0.268415I$   | $-1.92828 - 0.12066I$                 | $-7.15424 + 0.12690I$ |
| $b = 0.003550 - 0.690228I$    |                                       |                       |
| $u = 0.612697 + 0.489080I$    |                                       |                       |
| $a = -1.115050 + 0.268415I$   | $-1.92828 + 0.12066I$                 | $-7.15424 - 0.12690I$ |
| $b = 0.003550 + 0.690228I$    |                                       |                       |
| $u = 0.77088 - 1.59345I$      |                                       |                       |
| $a = 0.035485 + 0.801642I$    | $-8.1954 - 13.8902I$                  | $-5.93452 + 8.00354I$ |
| $b = 0.02106 - 2.63014I$      |                                       |                       |
| $u = 0.77088 + 1.59345I$      |                                       |                       |
| $a = 0.035485 - 0.801642I$    | $-8.1954 + 13.8902I$                  | $-5.93452 - 8.00354I$ |
| $b = 0.02106 + 2.63014I$      |                                       |                       |
| $u = 0.792668 - 0.169516I$    |                                       |                       |
| $a = -0.128021 + 0.417461I$   | $-0.39510 + 2.82136I$                 | $0.57403 - 4.29661I$  |
| $b = 0.713084 - 0.803498I$    |                                       |                       |
| $u = 0.792668 + 0.169516I$    |                                       |                       |
| $a = -0.128021 - 0.417461I$   | $-0.39510 - 2.82136I$                 | $0.57403 + 4.29661I$  |
| $b = 0.713084 + 0.803498I$    |                                       |                       |
| $u = 1.69889 - 0.01850I$      |                                       |                       |
| $a = 0.648911 + 0.174171I$    | $-3.35360 - 5.46941I$                 | $-6.70822 + 8.69559I$ |
| $b = 1.163139 - 0.325427I$    |                                       |                       |
| $u = 1.69889 + 0.01850I$      |                                       |                       |
| $a = 0.648911 - 0.174171I$    | $-3.35360 + 5.46941I$                 | $-6.70822 - 8.69559I$ |
| $b = 1.163139 + 0.325427I$    |                                       |                       |

$$\text{II. } I_1^v = \langle b^6 + 3b^5 + 7b^4 + 4b^3 + b^2 + 2b + 1, -19b^5 + v + \dots - 15b - 30, a \rangle$$

(i) Arc colorings

$$\begin{aligned}
a_3 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\
a_8 &= \begin{pmatrix} 19b^5 + 45b^4 + 105b^3 + 11b^2 + 15b + 30 \\ 0 \end{pmatrix} \\
a_4 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\
a_{11} &= \begin{pmatrix} 0 \\ b \end{pmatrix} \\
a_9 &= \begin{pmatrix} 19b^5 + 45b^4 + 105b^3 + 11b^2 + 15b + 30 \\ 8b^5 + 19b^4 + 44b^3 + 4b^2 + 5b + 12 \end{pmatrix} \\
a_7 &= \begin{pmatrix} 19b^5 + 45b^4 + 105b^3 + 11b^2 + 15b + 30 \\ 0 \end{pmatrix} \\
a_6 &= \begin{pmatrix} -12b^5 - 27b^4 - 63b^3 + b^2 - 9b - 18 \\ -14b^5 - 33b^4 - 77b^3 - 7b^2 - 11b - 21 \end{pmatrix} \\
a_5 &= \begin{pmatrix} -26b^5 - 60b^4 - 140b^3 - 6b^2 - 20b - 39 \\ -14b^5 - 33b^4 - 77b^3 - 7b^2 - 11b - 21 \end{pmatrix} \\
a_{10} &= \begin{pmatrix} -32b^5 - 75b^4 - 175b^3 - 14b^2 - 25b - 50 \\ b \end{pmatrix} \\
a_1 &= \begin{pmatrix} 12b^5 + 27b^4 + 63b^3 - b^2 + 9b + 18 \\ 14b^5 + 33b^4 + 77b^3 + 7b^2 + 11b + 21 \end{pmatrix} \\
a_2 &= \begin{pmatrix} 42b^5 + 98b^4 + 228b^3 + 14b^2 + 28b + 64 \\ 14b^5 + 33b^4 + 77b^3 + 7b^2 + 11b + 22 \end{pmatrix} \\
a_2 &= \begin{pmatrix} 42b^5 + 98b^4 + 228b^3 + 14b^2 + 28b + 64 \\ 14b^5 + 33b^4 + 77b^3 + 7b^2 + 11b + 22 \end{pmatrix}
\end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =unknown

(iv) Complex Volumes and Cusp Shapes

| Solution to $I_1^v$         | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $v = -0.162359 + 0.281214I$ |                                       |                       |
| $a = 0$                     | $-1.11345 - 2.02988I$                 | $-2.22484 - 4.65789I$ |
| $b = -1.16236 - 2.01326I$   |                                       |                       |
| $v = -0.162359 - 0.281214I$ |                                       |                       |
| $a = 0$                     | $-1.11345 + 2.02988I$                 | $-2.22484 + 4.65789I$ |
| $b = -1.16236 + 2.01326I$   |                                       |                       |
| $v = 1.31813 - 1.15851I$    |                                       |                       |
| $a = 0$                     | $3.02413 + 0.79824I$                  | $-0.92725 + 3.21674I$ |
| $b = -0.655769 - 0.011266I$ |                                       |                       |
| $v = 1.31813 + 1.15851I$    |                                       |                       |
| $a = 0$                     | $3.02413 - 0.79824I$                  | $-0.92725 - 3.21674I$ |
| $b = -0.655769 + 0.011266I$ |                                       |                       |
| $v = 0.34423 - 1.72078I$    |                                       |                       |
| $a = 0$                     | $3.02413 - 4.85801I$                  | $2.65209 + 7.50333I$  |
| $b = 0.318128 - 0.573545I$  |                                       |                       |
| $v = 0.34423 + 1.72078I$    |                                       |                       |
| $a = 0$                     | $3.02413 + 4.85801I$                  | $2.65209 - 7.50333I$  |
| $b = 0.318128 + 0.573545I$  |                                       |                       |



### III. u-Polynomials

| Crossings  | u-Polynomials at each crossings                             |
|------------|---|
| $c_1$      | $(u^2 + u + 1)^3(u^{39} + 4u^{38} + \dots + 10u - 1)$       |
| $c_2$      | $(u^2 + u + 1)^3(u^{39} + 22u^{38} + \dots + 170u - 1)$     |
| $c_3, c_7$ | $u^6(u^{39} + 3u^{38} + \dots + 160u + 64)$                 |
| $c_4$      | $(u^2 - u + 1)^3(u^{39} + 4u^{38} + \dots + 10u - 1)$       |
| $c_5$      | $(u^2 + u + 1)^3(u^{39} + 4u^{38} + \dots + 602u + 49)$     |
| $c_6$      | $(u^3 - u^2 + 2u - 1)^2(u^{39} + 3u^{38} + \dots - 3u - 1)$ |
| $c_8$      | $(u^3 + u^2 - 1)^2(u^{39} + 3u^{38} + \dots - 5u - 1)$      |
| $c_9$      | $(u^3 + u^2 + 2u + 1)^2(u^{39} + 3u^{38} + \dots - 3u - 1)$ |
| $c_{10}$   | $(u^3 - u^2 + 1)^2(u^{39} + 3u^{38} + \dots - 5u - 1)$      |
| $c_{11}$   | $(u^3 + u^2 + 2u + 1)^2(u^{39} + 23u^{38} + \dots + u + 1)$ |

#### IV. Riley Polynomials

| Crossings     | Riley Polynomials at each crossings                             |
|---------------|---|
| $c_1, c_4$    | $(y^2 + y + 1)^3(y^{39} + 22y^{38} + \dots + 170y - 1)$         |
| $c_2$         | $(y^2 + y + 1)^3(y^{39} - 6y^{38} + \dots + 31510y - 1)$        |
| $c_3, c_7$    | $y^6(y^{39} + 35y^{38} + \dots - 23552y - 4096)$                |
| $c_5$         | $(y^2 + y + 1)^3(y^{39} - 34y^{38} + \dots + 391706y - 2401)$   |
| $c_6, c_9$    | $(y^3 + 3y^2 + 2y - 1)^2(y^{39} + 9y^{38} + \dots + y - 1)$     |
| $c_8, c_{10}$ | $(y^3 - y^2 + 2y - 1)^2(y^{39} - 23y^{38} + \dots + y - 1)$     |
| $c_{11}$      | $(y^3 + 3y^2 + 2y - 1)^2(y^{39} - 11y^{38} + \dots + 117y - 1)$ |