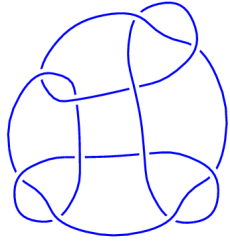
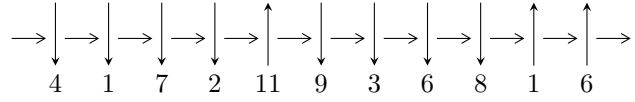


11n₇₁ (K11n₇₁)

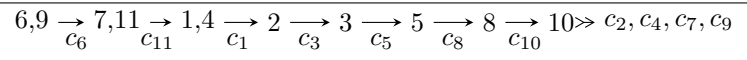


1

Arc Sequences



Solving Sequence



Representation Ideals

$$I = \bigcap_{i=1}^6 I_i^u \bigcap_{j=1}^3 I_j^v$$

¹The knot diagram image is adapter from “C. Livingston and A. H. Moore, KnotInfo: Table of Knot Invariants, <http://www.indiana.edu/~knotinfo>”

$$\begin{aligned}
I_1^u &= \langle b + u, c - a, d - b - 1, ba - 1 \rangle \\
I_2^u &= \langle c, u - 1, a + 1, d + 1, b + 1 \rangle \\
I_3^u &= \langle b - 1, c - 1, d - 1, u + 1, a - 1 \rangle \\
I_4^u &= \langle -u^3 - 3u^2 + 8b + u - 5, -u^3 - 3u^2 + 8d + u - 5, -u^5 - 6u^4 + 38u^2 + 176a + 89u + 168, \\
&\quad -u^5 - 6u^4 + 38u^2 + 176c + 89u + 168, u^6 + 6u^5 + 11u^4 + 28u^3 - u^2 + 30u - 11 \rangle \\
I_5^u &= \langle u^{10} + 10u^8 - 12u^7 + 42u^6 - 68u^5 + 164u^4 - 116u^3 + 301u^2 - 188u + 122, \\
&\quad -273u^9 + 61u^8 + \cdots + 15616a + 24606, \\
&\quad 3u^9 + 3u^8 + 21u^7 + u^6 + 27u^5 + 31u^4 + 79u^3 + 323u^2 + 128b - 2u + 154, \\
&\quad 167u^9 + 61u^8 + 1365u^7 - 845u^6 + 3415u^5 - 2511u^4 + 10247u^3 + 8993u^2 + 15616c + 9702u + 4350, \\
&\quad -3u^9 + 7u^8 - 25u^7 + 73u^6 - 115u^5 + 195u^4 - 307u^3 + 211u^2 + 256d + 2u + 90 \rangle \\
I_6^u &= \langle u^{13} + 3u^{12} + \cdots + 79u - 11, 397u^{12} + 1268u^{11} + \cdots + 5632a + 25599, \\
&\quad u^{12} + u^{11} + 9u^{10} - 17u^9 - 34u^8 - 260u^7 - 406u^6 - 880u^5 - 843u^4 - 965u^3 - 611u^2 + 128b - 439u - 36, \\
&\quad 47u^{12} + 174u^{11} + \cdots + 1408c + 4791, -3u^{12} - 4u^{11} + \cdots + 512d - 265 \rangle
\end{aligned}$$

$$\begin{aligned}
I_1^v &= \langle b, c, v - 1, d + 1, a - 1 \rangle \\
I_2^v &= \langle a, v - 1, d - b, c - a, b^3 + b^2 - 1 \rangle \\
I_3^v &= \langle a, v - 1, b^3 + b^2 - 1, 2db - da + cb + 2d - 1, 2d^2 + da - cb + 2b^2 - 2d - 1, \\
&\quad a^2d - cba + b^2a + a^2b - 4dc - 2da - c^2 - ca + 2b^2 - 3ba + 2c + 3b + a - 3, \\
&\quad 3a^2d + 2b^2c - 3cba + 4a^2b - 12dc - 6da - 4c^2 + 4cb - 4ca + 8b^2 - 12ba + 8c + 10b + 3a - 8, \\
&\quad -dca - 18dc + \cdots + 7a - 14, 2c^2d - dca + \cdots - 12a + 21, -10c^2d - 6dca + \cdots + 12a - 27, \\
&\quad -14c^2d - 10dca + \cdots + 24a - 49, 2c^3d + 4c^2da + \cdots - 57a + 115, c^6 + 3c^5a + \cdots + 27a - 11 \rangle
\end{aligned}$$

There are 9 irreducible components with 41 representations.

There are 1 irreducible components of $\dim_{\mathbb{C}} = 1$ for $11n_{71}$

$$\text{I. } \Gamma_1^u = \langle b + u, c - a, d - b - 1, ba - 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 0 \\ -b \end{pmatrix}$$

$$a_9 = \begin{pmatrix} a \\ b \end{pmatrix}$$

$$a_7 = \begin{pmatrix} b^{-1} \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} a \\ b + 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} b^{-1} \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1 + b^{-1} \\ 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} b^{-1} \\ 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} b^{-1} \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ b \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ b \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

| Solution to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---------------------|---------------------------------------|---------------------|
| $u = \dots$ | | |
| $a = \dots$ | | |
| $b = \dots$ | -1.64493 | -9.18057 - 0.23194I |
| $c = \dots$ | | |
| $d = \dots$ | | |

$$\text{II. } I_2^u = \langle c, u - 1, a + 1, d + 1, b + 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =unknown

(iv) Complex Volumes and Cusp Shapes

| Solution to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---------------------|---------------------------------------|------------|
| $u = 1.00000$ | | |
| $a = -1.00000$ | | |
| $b = -1.00000$ | -3.28987 | -12.0000 |
| $c = 0$ | | |
| $d = -1.00000$ | | |

$$\text{III. } I_3^u = \langle b - 1, c - 1, d - 1, u + 1, a - 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =unknown

(iv) Complex Volumes and Cusp Shapes

| Solution to I_3^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---------------------|---------------------------------------|------------|
| $u = -1.00000$ | | |
| $a = 1.00000$ | | |
| $b = 1.00000$ | 0 | 0 |
| $c = 1.00000$ | | |
| $d = 1.00000$ | | |

IV. $I_4^u = \langle -u^3 - 3u^2 + 8b + u - 5, -u^3 - 3u^2 + 8d + u - 5, -u^5 - 6u^4 + \dots + 176a + 168, -u^5 - 6u^4 + \dots + 176c + 168, u^6 + 6u^5 + \dots + 30u - 11 \rangle$

(i) Arc colorings

$$\begin{aligned}
a_6 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\
a_9 &= \begin{pmatrix} 0.00568182u^5 + 0.0340909u^4 + \dots - 0.505682u - 0.954545 \\ \frac{1}{8}u^3 + \frac{3}{8}u^2 - \frac{1}{8}u + \frac{5}{8} \end{pmatrix} \\
a_7 &= \begin{pmatrix} -0.0198864u^5 - 0.150568u^4 + \dots - 0.542614u - 0.127841 \\ -0.0312500u^5 - 0.156250u^4 + \dots + 1.09375u + 0.218750 \end{pmatrix} \\
a_{11} &= \begin{pmatrix} 0.00568182u^5 + 0.0340909u^4 + \dots - 0.505682u - 0.954545 \\ \frac{1}{8}u^3 + \frac{3}{8}u^2 - \frac{1}{8}u + \frac{5}{8} \end{pmatrix} \\
a_1 &= \begin{pmatrix} 0.00568182u^5 + 0.0340909u^4 + \dots - 0.505682u - 0.954545 \\ \frac{1}{16}u^5 + \frac{3}{8}u^4 + \dots - \frac{3}{16}u + \frac{5}{8} \end{pmatrix} \\
a_4 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\
a_2 &= \begin{pmatrix} -0.0568182u^5 - 0.340909u^4 + \dots - 0.318182u - 1.57955 \\ \frac{1}{16}u^5 + \frac{3}{8}u^4 + \dots - \frac{3}{16}u + \frac{5}{8} \end{pmatrix} \\
a_3 &= \begin{pmatrix} 0.0482955u^5 + 0.258523u^4 + \dots - 0.860795u + 1.41761 \\ -0.0312500u^5 - 0.218750u^4 + \dots - 0.906250u + 0.156250 \end{pmatrix} \\
a_5 &= \begin{pmatrix} -0.0198864u^5 - 0.150568u^4 + \dots - 0.542614u - 0.127841 \\ -0.0312500u^5 - 0.156250u^4 + \dots + 1.09375u + 0.218750 \end{pmatrix} \\
a_8 &= \begin{pmatrix} 0.00568182u^5 + 0.0340909u^4 + \dots - 0.505682u - 0.954545 \\ \frac{1}{16}u^5 + \frac{3}{8}u^4 + \dots - \frac{3}{16}u + \frac{5}{8} \end{pmatrix} \\
a_{10} &= \begin{pmatrix} 0.0142045u^5 + 0.0539773u^4 + \dots - 1.45170u - 0.480114 \\ \frac{1}{8}u^3 + \frac{1}{8}u^2 - \frac{9}{8}u + \frac{7}{8} \end{pmatrix} \\
a_{10} &= \begin{pmatrix} 0.0142045u^5 + 0.0539773u^4 + \dots - 1.45170u - 0.480114 \\ \frac{1}{8}u^3 + \frac{1}{8}u^2 - \frac{9}{8}u + \frac{7}{8} \end{pmatrix}
\end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

| Solution to I_4^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = -4.98061$ $a = -0.227714$ $b = -4.89390$ $c = -0.227714$ $d = -4.89390$ | -1.11345 | -9.01951 |
| $u = -0.79253 - 2.21570I$ $a = 0.169365 - 0.603060I$ $b = 0.51544 + 2.43179I$ $c = 0.169365 - 0.603060I$ $d = 0.51544 + 2.43179I$ | $3.02413 - 2.82812I$ | $-2.49024 + 2.97945I$ |
| $u = -0.79253 + 2.21570I$ $a = 0.169365 + 0.603060I$ $b = 0.51544 - 2.43179I$ $c = 0.169365 + 0.603060I$ $d = 0.51544 - 2.43179I$ | $3.02413 + 2.82812I$ | $-2.49024 - 2.97945I$ |
| $u = 0.117251 - 1.091142I$ $a = -0.710151 + 0.619768I$ $b = 0.116880 + 0.197202I$ $c = -0.710151 + 0.619768I$ $d = 0.116880 + 0.197202I$ | $3.02413 + 2.82812I$ | $-2.49024 - 2.97945I$ |
| $u = 0.117251 + 1.091142I$ $a = -0.710151 - 0.619768I$ $b = 0.116880 - 0.197202I$ $c = -0.710151 - 0.619768I$ $d = 0.116880 - 0.197202I$ | $3.02413 - 2.82812I$ | $-2.49024 + 2.97945I$ |
| $u = 0.331172$ $a = -1.14526$ $b = 0.629272$ $c = -1.14526$ $d = 0.629272$ | -1.11345 | -9.01951 |

$$\mathbf{V. } I_5^u = \langle u^{10} + 10u^8 + \dots - 188u + 122, -273u^9 + 61u^8 + \dots + 1.56 \times 10^4 a + 2.46 \times 10^4, 3u^9 + 3u^8 + \dots + 128b + 154, 167u^9 + 61u^8 + \dots + 1.56 \times 10^4 c + 4350, -3u^9 + 7u^8 + \dots + 256d + 90 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_6 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_9 &= \begin{pmatrix} 0.0174821u^9 - 0.00390625u^8 + \dots + 2.95351u - 1.57569 \\ -0.0234375u^9 - 0.0234375u^8 + \dots + 0.0156250u - 1.20313 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 0.00832480u^9 + 0.00781250u^8 + \dots + 3.13858u - 1.73694 \\ 0.00390625u^9 - 0.00390625u^8 + \dots - 1.64844u + 0.539063 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -0.0106942u^9 - 0.00390625u^8 + \dots - 0.621286u - 0.278560 \\ 0.0117188u^9 - 0.0273438u^8 + \dots - 0.00781250u - 0.351563 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -0.0106942u^9 - 0.00390625u^8 + \dots - 0.621286u - 0.278560 \\ -0.00781250u^9 + 0.00781250u^8 + \dots - 0.578125u - 0.828125 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -0.00288166u^9 - 0.0117188u^8 + \dots - 0.0431609u + 0.549565 \\ -0.00781250u^9 + 0.00781250u^8 + \dots - 0.578125u - 0.828125 \end{pmatrix} \\ a_3 &= \begin{pmatrix} 0.00582736u^9 + 0.00390625u^8 + \dots - 0.890497u + 0.0685195 \\ 0.00781250u^9 - 0.0234375u^8 + \dots + 0.640625u + 0.234375 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 0.000128074u^9 - 0.00781250u^8 + \dots + 0.983863u - 0.164703 \\ 0.0156250u^8 + 0.109375u^6 + \dots - 0.312500u + 0.968750 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 0.0174821u^9 - 0.00390625u^8 + \dots + 2.95351u - 1.57569 \\ -0.0117188u^9 - 0.0507813u^8 + \dots + 2.88281u - 1.67969 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -0.00192111u^9 + 0.00781250u^8 + \dots - 2.50794u + 1.00179 \\ 0.0273438u^9 - 0.0429688u^8 + \dots - 0.539063u + 0.242188 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -0.00192111u^9 + 0.00781250u^8 + \dots - 2.50794u + 1.00179 \\ 0.0273438u^9 - 0.0429688u^8 + \dots - 0.539063u + 0.242188 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

| Solution to I_5^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|-----------------------|
| $u = -0.80416 - 1.99039I$ $a = -0.226170 - 0.467647I$ $b = -1.66008 + 0.82623I$ $c = -0.261376 + 0.646937I$ $d = -0.45558 - 2.15506I$ | 5.22495 | -1.71424 |
| $u = -0.80416 + 1.99039I$ $a = -0.226170 + 0.467647I$ $b = -1.66008 - 0.82623I$ $c = -0.261376 - 0.646937I$ $d = -0.45558 + 2.15506I$ | 5.22495 | -1.71424 |
| $u = -0.58512 - 1.64721I$ $a = 0.226955 + 0.770761I$ $b = 1.33238 - 1.82753I$ $c = 0.454928 - 0.797797I$ $d = 0.01574 + 1.66108I$ | $10.17382 + 6.99719I$ | $-0.86096 - 3.54683I$ |
| $u = -0.58512 + 1.64721I$ $a = 0.226955 - 0.770761I$ $b = 1.33238 + 1.82753I$ $c = 0.454928 + 0.797797I$ $d = 0.01574 - 1.66108I$ | $10.17382 - 6.99719I$ | $-0.86096 + 3.54683I$ |
| $u = -0.42487 - 2.28349I$ $a = 0.433800 + 0.274942I$ $b = 0.639086 - 0.104692I$ $c = 0.004860 - 0.691166I$ $d = 0.17983 + 2.66378I$ | $10.17382 - 6.99719I$ | $-0.86096 + 3.54683I$ |
| $u = -0.42487 + 2.28349I$ $a = 0.433800 - 0.274942I$ $b = 0.639086 + 0.104692I$ $c = 0.004860 + 0.691166I$ $d = 0.17983 - 2.66378I$ | $10.17382 + 6.99719I$ | $-0.86096 - 3.54683I$ |

| Solution to I_5^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = 0.390335 - 0.601190I$ $a = -0.78431 - 1.46141I$ $b = -0.424715 + 1.136223I$ $c = -0.200209 + 0.681246I$ $d = -0.491733 + 0.238896I$ | $-2.91669 + 1.13882I$ | $-7.28192 - 6.05450I$ |
| $u = 0.390335 + 0.601190I$ $a = -0.78431 + 1.46141I$ $b = -0.424715 - 1.136223I$ $c = -0.200209 - 0.681246I$ $d = -0.491733 - 0.238896I$ | $-2.91669 - 1.13882I$ | $-7.28192 + 6.05450I$ |
| $u = 1.42381 - 1.04807I$ $a = 0.292349 + 0.417022I$ $b = 1.61333 - 0.94778I$ $c = 0.280485 - 0.064832I$ $d = 1.25175 - 0.99625I$ | $-2.91669 - 1.13882I$ | $-7.28192 + 6.05450I$ |
| $u = 1.42381 + 1.04807I$ $a = 0.292349 - 0.417022I$ $b = 1.61333 + 0.94778I$ $c = 0.280485 + 0.064832I$ $d = 1.25175 + 0.99625I$ | $-2.91669 + 1.13882I$ | $-7.28192 - 6.05450I$ |

$$\text{VI. } I_6^u = \langle u^{13} + 3u^{12} + \dots + 79u - 11, 397u^{12} + 1268u^{11} + \dots + 5632a + 2.56 \times 10^4, u^{12} + u^{11} + \dots + 128b - 36, 47u^{12} + 174u^{11} + \dots + 1408c + 4791, -3u^{12} - 4u^{11} + \dots + 512d - 265 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_6 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_9 &= \begin{pmatrix} -0.0704901u^{12} - 0.225142u^{11} + \dots - 5.47940u - 4.54528 \\ -0.00781250u^{12} - 0.00781250u^{11} + \dots + 3.42969u + 0.281250 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -0.0316051u^{12} - 0.0909091u^{11} + \dots - 2.59943u - 3.07493 \\ 0.00585938u^{12} + 0.0156250u^{11} + \dots + 1.75000u + 0.369141 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -0.0333807u^{12} - 0.123580u^{11} + \dots - 5.73722u - 3.40270 \\ 0.00585938u^{12} + 0.00781250u^{11} + \dots + 0.460938u + 0.517578 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -0.0333807u^{12} - 0.123580u^{11} + \dots - 5.73722u - 3.40270 \\ 0.0136719u^{12} + 0.0234375u^{11} + \dots - 1.02344u + 0.775391 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -0.0470526u^{12} - 0.147017u^{11} + \dots - 4.71378u - 4.17809 \\ 0.0136719u^{12} + 0.0234375u^{11} + \dots - 1.02344u + 0.775391 \end{pmatrix} \\ a_3 &= \begin{pmatrix} 0.0150923u^{12} + 0.0355114u^{11} + \dots + 2.49148u + 2.77042 \\ -0.0273438u^{12} - 0.0859375u^{11} + \dots + 0.476563u - 0.402344 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -0.0276989u^{12} - 0.0830966u^{11} + \dots - 2.71662u - 1.72727 \\ -0.00390625u^{12} - 0.0156250u^{11} + \dots + 0.578125u + 0.347656 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -0.0704901u^{12} - 0.225142u^{11} + \dots - 5.47940u - 4.54528 \\ -0.0253906u^{12} - 0.0781250u^{11} + \dots + 3.12500u + 0.431641 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -0.0365767u^{12} - 0.137074u^{11} + \dots - 4.92116u - 2.41300 \\ -0.00585938u^{12} - 0.0390625u^{11} + \dots - 0.179688u + 0.466797 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -0.0365767u^{12} - 0.137074u^{11} + \dots - 4.92116u - 2.41300 \\ -0.00585938u^{12} - 0.0390625u^{11} + \dots - 0.179688u + 0.466797 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

| Solution to I_6^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|----------------------|
| $u = -0.62719 - 2.30924I$ $a = 0.415187 - 0.318981I$ $b = 2.19716 + 0.25380I$ $c = -0.089361 + 0.625967I$ $d = -0.37484 - 2.59192I$ | 4.46546 - 5.94244I | -3.19547 + 4.81410I |
| $u = -0.62719 + 2.30924I$ $a = 0.415187 + 0.318981I$ $b = 2.19716 - 0.25380I$ $c = -0.089361 - 0.625967I$ $d = -0.37484 + 2.59192I$ | 4.46546 + 5.94244I | -3.19547 - 4.81410I |
| $u = -0.60300 - 1.80443I$ $a = -0.641818 + 0.144610I$ $b = -0.481693 + 0.542167I$ $c = 0.339649 - 0.789509I$ $d = 0.08775 + 1.95176I$ | 11.70801 + 0.17366I | 0.445368 + 1.147630I |
| $u = -0.60300 + 1.80443I$ $a = -0.641818 - 0.144610I$ $b = -0.481693 - 0.542167I$ $c = 0.339649 + 0.789509I$ $d = 0.08775 - 1.95176I$ | 11.70801 - 0.17366I | 0.445368 - 1.147630I |
| $u = -0.550790 - 0.607220I$ $a = 0.161605 + 0.505870I$ $b = -0.323915 - 0.475651I$ $c = -0.983962 + 0.634772I$ $d = -0.578466 - 0.322896I$ | 1.70980 + 0.77307I | 3.13297 - 1.88722I |
| $u = -0.550790 + 0.607220I$ $a = 0.161605 - 0.505870I$ $b = -0.323915 + 0.475651I$ $c = -0.983962 - 0.634772I$ $d = -0.578466 + 0.322896I$ | 1.70980 - 0.77307I | 3.13297 + 1.88722I |

| Solution to I_6^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = -0.30470 - 2.39480I$ $a = -0.365209 + 0.469173I$ $b = -2.00636 - 1.88555I$ $c = -0.077826 - 0.645545I$ $d = 0.14634 + 2.79708I$ | $7.6949 - 13.5931I$ | $-3.46569 + 7.45820I$ |
| $u = -0.30470 + 2.39480I$ $a = -0.365209 - 0.469173I$ $b = -2.00636 + 1.88555I$ $c = -0.077826 + 0.645545I$ $d = 0.14634 - 2.79708I$ | $7.6949 + 13.5931I$ | $-3.46569 - 7.45820I$ |
| $u = 0.118527$ $a = -5.43568$ $b = 0.768845$ $c = -4.28367$ $d = 0.584095$ | -1.13096 | -8.32650 |
| $u = 0.257371 - 1.182512I$ $a = 0.763415 + 0.750288I$ $b = 1.57519 - 1.27790I$ $c = -0.714631 + 0.489015I$ $d = 0.165909 + 0.493218I$ | $1.53986 + 8.66555I$ | $-5.43123 - 7.16460I$ |
| $u = 0.257371 + 1.182512I$ $a = 0.763415 - 0.750288I$ $b = 1.57519 + 1.27790I$ $c = -0.714631 - 0.489015I$ $d = 0.165909 - 0.493218I$ | $1.53986 - 8.66555I$ | $-5.43123 + 7.16460I$ |
| $u = 0.269046 - 0.841548I$ $a = -0.797160 - 0.773649I$ $b = -1.344806 - 0.047817I$ $c = 0.486147 - 0.651855I$ $d = 0.261255 - 0.268383I$ | $-1.87851 + 3.16005I$ | $-8.32269 - 6.37622I$ |
| Solution to I_6^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
| $u = 0.269046 + 0.841548I$ $a = -0.797160 + 0.773649I$ $b = -1.344806 + 0.047817I$ $c = 0.486147 + 0.651855I$ $d = 0.261255 + 0.268383I$ | $-1.87851 - 3.16005I$ | $-8.32269 + 6.37622I$ |

$$\text{VII. } I_1^v = \langle b, c, v - 1, d + 1, a - 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =unknown

(iv) Complex Volumes and Cusp Shapes

| Solution to I_1^v | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---------------------|---------------------------------------|------------|
| $v = 1.00000$ | | |
| $a = 1.00000$ | | |
| $b = 0$ | 0 | 0 |
| $c = 0$ | | |
| $d = -1.00000$ | | |

$$\text{VIII. } I_2^v = \langle a, v - 1, d - b, c - a, b^3 + b^2 - 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ b \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ b^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ b \end{pmatrix}$$

$$a_1 = \begin{pmatrix} b \\ b \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0 \\ b \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -b^2 + 1 \\ -b^2 - b + 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ b^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} b \\ b \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} b^2 - 1 \\ b^2 + b - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} b^2 - 1 \\ b^2 + b - 1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =unknown

(iv) Complex Volumes and Cusp Shapes

| Solution to I_2^v | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|-----------------------|
| $v = 1.00000$ $a = 0$ $b = -0.877439 - 0.744862I$ $c = 0$ $d = -0.877439 - 0.744862I$ | $3.02413 - 2.82812I$ | $-2.49024 + 2.97945I$ |
| $v = 1.00000$ $a = 0$ $b = -0.877439 + 0.744862I$ $c = 0$ $d = -0.877439 + 0.744862I$ | $3.02413 + 2.82812I$ | $-2.49024 - 2.97945I$ |
| $v = 1.00000$ $a = 0$ $b = 0.754878$ $c = 0$ $d = 0.754878$ | -1.11345 | -9.01951 |

IX. $I_3^v = \langle a, v-1, b^3 + b^2 - 1, 2bd - ad + \dots + bc - 1, 2d^2 + ad + \dots + 2b^2 - 1, -4cd + a^2d + \dots + a - 3, -12cd + 3a^2d + \dots + 3a - 8, -acd - 18cd + \dots + 7a - 14, 2c^2d - acd + \dots - 12a + 21, -10c^2d - 6acd + \dots + 12a - 27, -14c^2d - 10acd + \dots + 24a - 49, 2c^3d + 4ac^2d + \dots - 57a + 115, c^6 + 3ac^5 + \dots + 27a - 11 \rangle$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} a \\ b \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ -d^5 + d^3 + d^2 + d \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} c \\ d \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 2d^4 - d^3 - 2d^2 - 2d + 1 \\ d \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 2d^4 - d^3 - 2d^2 - 3d + 1 \\ d \end{pmatrix}$$

$$a_3 = \begin{pmatrix} d^5 - d^3 - d^2 - d + 1 \\ d^3 - d \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 2d^5 - d^4 - 2d^3 - 3d^2 + d + 1 \\ d^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} d^5 - 2d^3 - d^2 + 1 \\ d^5 - 2d^3 - d^2 + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -d^5 + d^3 + d^2 + d - 1 \\ -d^3 + d \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -d^5 + d^3 + d^2 + d - 1 \\ -d^3 + d \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

| Solution to I_3^v | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $v = 1.00000$ $a = 0$ $b = 0.754878$ $c = 6.59790$ $d = -1.13416$ | -1.11345 | -9.01951 |
| $v = 1.00000$ $a = 0$ $b = -0.877439 - 0.744862I$ $c = 0.691189 + 0.656800I$ $d = -0.592989 + 0.847544I$ | $3.02413 - 2.82812I$ | $-2.49024 + 2.97945I$ |
| $v = 1.00000$ $a = 0$ $b = -0.877439 + 0.744862I$ $c = 0.691189 - 0.656800I$ $d = -0.592989 - 0.847544I$ | $3.02413 + 2.82812I$ | $-2.49024 - 2.97945I$ |
| $v = 1.00000$ $a = 0$ $b = -0.877439 - 0.744862I$ $c = -1.77078 - 1.02196I$ $d = 1.47043 - 0.10268I$ | $3.02413 - 2.82812I$ | $-2.49024 + 2.97945I$ |
| $v = 1.00000$ $a = 0$ $b = -0.877439 + 0.744862I$ $c = -1.77078 + 1.02196I$ $d = 1.47043 + 0.10268I$ | $3.02413 + 2.82812I$ | $-2.49024 - 2.97945I$ |
| $v = 1.00000$ $a = 0$ $b = 0.754878$ $c = -0.438709$ $d = 0.379278$ | -1.11345 | -9.01951 |

X. u-Polynomials

| Crossings | u-Polynomials at each crossings |
|---------------|---|
| c_1, c_6 | $u(u-1)^3(u^3+u^2-1)^3(u^6-u^5-2u^4+2u^2+2u-1)$ $(u^{10}+u^9-u^8-3u^7+2u^5+u^4-4u^3-3u^2+4u+4)$ $(u^{13}+2u^{12}-4u^{10}+8u^8+7u^7-7u^6-8u^5+3u^4+9u^3-u^2-u-1)$ |
| c_2, c_9 | $u(u+1)^3(u^3+u^2+2u+1)^3(u^6+5u^5+8u^4+6u^3+8u^2+8u+1)$ $(u^{10}+3u^9+\dots+40u+16)(u^{13}+4u^{12}+\dots-u+1)$ |
| c_3, c_7 | $u^4(u^3+u^2+2u+1)^5(u^5-3u^4+6u^3-7u^2+4u-2)^2$ $(u^{13}+2u^{12}+\dots-4u^2+8)$ |
| c_4, c_8 | $u(u-1)(u+1)^2(u^3+u^2-1)^3(u^6-u^5-2u^4+2u^2+2u-1)$ $(u^{10}+u^9-u^8-3u^7+2u^5+u^4-4u^3-3u^2+4u+4)$ $(u^{13}+2u^{12}-4u^{10}+8u^8+7u^7-7u^6-8u^5+3u^4+9u^3-u^2-u-1)$ |
| c_5, c_{11} | $u(u-1)(u+1)^2(u^3-u^2+1)(u^5+u^4-3u^3-2u^2+2u-1)^2$ $(-1-2u+2u^2-2u^4+u^5+u^6)^2(u^{13}+2u^{12}+\dots+8u+4)$ |
| c_{10} | $u(u+1)^3(u^3+u^2+2u+1)(u^5+7u^4+17u^3+14u^2+1)^2$ $(1+8u+8u^2+6u^3+8u^4+5u^5+u^6)^2(u^{13}+14u^{12}+\dots+88u+16)$ |

XI. Riley Polynomials

| Crossings | Riley Polynomials at each crossings |
|--------------------------|---|
| c_1, c_4, c_6 c_8 | $y(y-1)^3(y^3-y^2+2y-1)^3(y^6-5y^5+8y^4-6y^3+8y^2-8y+1)$ $(y^{10}-3y^9+\dots-40y+16)(y^{13}-4y^{12}+\dots-y-1)$ |
| c_2, c_9 | $y(y-1)^3(y^3+3y^2+2y-1)^3$ $(y^6-9y^5+20y^4+14y^3-16y^2-48y+1)$ $(y^{10}+5y^9+\dots-32y+256)(y^{13}+16y^{12}+\dots-25y-1)$ |
| c_3, c_7 | $y^4(y^3+3y^2+2y-1)^5(y^5+3y^4+2y^3-13y^2-12y-4)^2$ $(y^{13}+6y^{12}+\dots+64y-64)$ |
| c_5, c_{11} | $y(y-1)^3(y^3-y^2+2y-1)(y^5-7y^4+17y^3-14y^2-1)^2$ $(1-8y+8y^2-6y^3+8y^4-5y^5+y^6)^2(y^{13}-14y^{12}+\dots+88y-16)$ |
| c_{10} | $(y)(y-1)^3(y^3+3y^2+2y-1)(-1-28y-210y^2+93y^3-15y^4+y^5)^2$ $(y^6-9y^5+20y^4+14y^3-16y^2-48y+1)^2$ $(y^{13}-30y^{12}+\dots+2848y-256)$ |