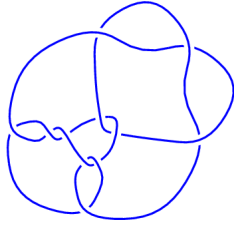
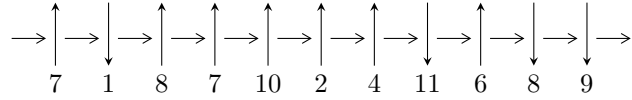


11n₉₈ (K11n₉₈)

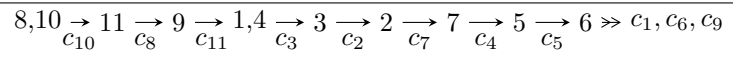


1

Arc Sequences



Solving Sequence



Representation Ideals

$$I = \bigcap_{i=1}^4 I_i^u$$

$$I_1^u = \langle u + 1, a - 1, 2b + 1 \rangle$$

$$I_2^u = \langle a^4 + 3a^2 + 1, -a^3 - 2a + u, -a^3 + a^2 + b - 2a + 2 \rangle$$

$$I_3^u = \langle u^{17} - u^{16} + \dots - 4u^2 - 1, -11u^{16} + 14u^{15} + \dots + 32b + 3, 17u^{16} - 26u^{15} + \dots + 16a + 7 \rangle$$

$$\begin{aligned} I_4^u = & \langle u^{22} + 3u^{21} + \dots + 24u + 9, \\ & - 749178430u^{21} - 3147363456u^{20} + \dots + 7660380639b + 10655174784, \\ & - 2694752718u^{21} - 5680799296u^{20} + \dots + 7660380639a - 11072995247 \rangle \end{aligned}$$

There are 4 irreducible components with 44 representations.

¹The knot diagram image is adapter from “C. Livingston and A. H. Moore, KnotInfo: Table of Knot Invariants, <http://www.indiana.edu/~knotinfo>”

$$\text{I. } I_1^u = \langle u + 1, a - 1, 2b + 1 \rangle$$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -\frac{1}{2} \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ \frac{1}{2} \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -\frac{1}{2} \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 2 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 2 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 2 \\ -1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.00000$		
$a = 1.00000$	0	-2.25000
$b = -0.500000$		

$$\text{II. } I_2^u = \langle a^4 + 3a^2 + 1, -a^3 - 2a + u, -a^3 + a^2 + b - 2a + 2 \rangle$$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 0 \\ a^3 + 2a \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a \\ a^3 - a^2 + 2a - 2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} a \\ a^3 - a^2 + a - 2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} a^3 + a \\ 2a - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} a^3 + a \\ -a^3 - a - 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a^3 + a + 1 \\ -a^3 - a - 2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -a^3 - 2a \\ a^3 + 2a \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} a^2 \\ -a^3 - a^2 - 2a \end{pmatrix}$$

$$a_6 = \begin{pmatrix} a^2 \\ -a^3 - a^2 - 2a \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.00000I$		
$a = -0.618034I$	-4.27683	-8.00000
$b = -1.61803 - 1.00000I$		
$u = 1.00000I$		
$a = 0.618034I$	-4.27683	-8.00000
$b = -1.61803 + 1.00000I$		
$u = 1.00000I$		
$a = -1.61803I$	-12.1725	-8.00000
$b = 0.618034 + 1.000000I$		
$u = -1.00000I$		
$a = 1.61803I$	-12.1725	-8.00000
$b = 0.618034 - 1.000000I$		

$$\text{III. } I_3^u = \langle u^{17} - u^{16} + \dots - 4u^2 - 1, -11u^{16} + 14u^{15} + \dots + 32b + 3, 17u^{16} - 26u^{15} + \dots + 16a + 7 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_8 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -1.06250u^{16} + 1.62500u^{15} + \dots + 5.43750u - 0.437500 \\ 0.343750u^{16} - 0.437500u^{15} + \dots - 1.15625u - 0.0937500 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -1.06250u^{16} + 1.62500u^{15} + \dots + 5.43750u - 0.437500 \\ 0.781250u^{16} - 1.31250u^{15} + \dots - 2.21875u + 0.468750 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -0.0625000u^{16} - 0.125000u^{15} + \dots + 3.93750u - 0.687500 \\ -0.0312500u^{16} + 0.562500u^{15} + \dots - 0.0312500u - 0.468750 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -\frac{1}{4}u^{15} + \frac{1}{4}u^{14} + \dots - \frac{5}{4}u^2 + \frac{5}{4} \\ \frac{1}{4}u^{15} - \frac{1}{4}u^{14} + \dots + \frac{5}{4}u^2 - \frac{1}{4} \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_3 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -\frac{1}{4}u^{15} + \frac{1}{4}u^{14} + \dots - \frac{1}{4}u^2 + \frac{5}{4} \\ \frac{1}{4}u^{15} - \frac{1}{4}u^{14} + \dots + \frac{1}{4}u^2 - \frac{1}{4} \end{pmatrix} \\ a_7 &= \begin{pmatrix} -u \\ u \end{pmatrix} \\ a_5 &= \begin{pmatrix} u^2 + 1 \\ -u^2 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -\frac{1}{4}u^{16} + \frac{1}{4}u^{15} + \dots - \frac{1}{4}u^3 + \frac{9}{4}u \\ \frac{1}{4}u^{16} - \frac{1}{4}u^{15} + \dots + \frac{1}{4}u^3 - \frac{5}{4}u \end{pmatrix} \\ a_6 &= \begin{pmatrix} -\frac{1}{4}u^{16} + \frac{1}{4}u^{15} + \dots - \frac{1}{4}u^3 + \frac{9}{4}u \\ \frac{1}{4}u^{16} - \frac{1}{4}u^{15} + \dots + \frac{1}{4}u^3 - \frac{5}{4}u \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.678472 - 1.240021I$ $a = -0.225489 + 1.034292I$ $b = 1.54769 - 1.47366I$	$-4.6382 + 13.7590I$	$-2.60534 - 8.09148I$
$u = -0.678472 + 1.240021I$ $a = -0.225489 - 1.034292I$ $b = 1.54769 + 1.47366I$	$-4.6382 - 13.7590I$	$-2.60534 + 8.09148I$
$u = -0.678341 - 1.093893I$ $a = -0.544216 - 0.556925I$ $b = -0.747437 + 1.180736I$	$0.65577 + 8.75138I$	$0.84209 - 7.19652I$
$u = -0.678341 + 1.093893I$ $a = -0.544216 + 0.556925I$ $b = -0.747437 - 1.180736I$	$0.65577 - 8.75138I$	$0.84209 + 7.19652I$
$u = -0.583285 - 0.914805I$ $a = 1.015806 - 0.479229I$ $b = 0.083408 - 0.398282I$	$-1.75655 + 3.15519I$	$-1.08772 - 4.41422I$
$u = -0.583285 + 0.914805I$ $a = 1.015806 + 0.479229I$ $b = 0.083408 + 0.398282I$	$-1.75655 - 3.15519I$	$-1.08772 + 4.41422I$
$u = -0.239314 - 0.869369I$ $a = -0.54621 + 1.78172I$ $b = 0.092556 - 1.046207I$	$-11.59492 + 1.04318I$	$-1.35194 - 7.04363I$
$u = -0.239314 + 0.869369I$ $a = -0.54621 - 1.78172I$ $b = 0.092556 + 1.046207I$	$-11.59492 - 1.04318I$	$-1.35194 + 7.04363I$
$u = -0.187558 - 0.379982I$ $a = 0.37683 - 2.21344I$ $b = -0.554103 + 0.502263I$	$-1.69658 + 0.80451I$	$-2.69480 - 2.52231I$
$u = -0.187558 + 0.379982I$ $a = 0.37683 + 2.21344I$ $b = -0.554103 - 0.502263I$	$-1.69658 - 0.80451I$	$-2.69480 + 2.52231I$

Solution to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.606656 - 1.024999I$ $a = -0.400728 - 1.170949I$ $b = 0.98051 + 1.70447I$	$-2.68580 - 6.31167I$	$-1.34813 + 5.64607I$
$u = 0.606656 + 1.024999I$ $a = -0.400728 + 1.170949I$ $b = 0.98051 - 1.70447I$	$-2.68580 + 6.31167I$	$-1.34813 - 5.64607I$
$u = 0.635251$ $a = 0.465730$ $b = 0.236283$	0.963952	10.6381
$u = 0.784905 - 0.787523I$ $a = -0.294224 + 0.608642I$ $b = -0.240378 - 1.166900I$	$2.78581 - 2.60100I$	$4.98680 + 3.49505I$
$u = 0.784905 + 0.787523I$ $a = -0.294224 - 0.608642I$ $b = -0.240378 + 1.166900I$	$2.78581 + 2.60100I$	$4.98680 - 3.49505I$
$u = 1.157785 - 0.487195I$ $a = 0.885367 + 0.183583I$ $b = -0.530392 + 0.376632I$	$0.354258 + 0.834124I$	$0.06498 - 5.84789I$
$u = 1.157785 + 0.487195I$ $a = 0.885367 - 0.183583I$ $b = -0.530392 - 0.376632I$	$0.354258 - 0.834124I$	$0.06498 + 5.84789I$

IV.

$$I_4^u = \langle u^{22} + 3u^{21} + \dots + 24u + 9, -7.49 \times 10^8 u^{21} - 3.15 \times 10^9 u^{20} + \dots + 7.66 \times 10^9 b + 1.07 \times 10^{10}, -2.69 \times 10^9 u^{21} - 5.68 \times 10^9 u^{20} + \dots + 7.66 \times 10^9 a - 1.11 \times 10^{10} \rangle$$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.351778u^{21} + 0.741582u^{20} + \dots + 5.88891u + 1.44549 \\ 0.0977991u^{21} + 0.410863u^{20} + \dots - 0.0725632u - 1.39095 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.351778u^{21} + 0.741582u^{20} + \dots + 5.88891u + 1.44549 \\ 0.109720u^{21} + 0.727196u^{20} + \dots + 4.29148u + 1.43282 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.205132u^{21} + 0.242650u^{20} + \dots + 0.665474u - 1.10003 \\ 0.0568315u^{21} + 0.584282u^{20} + \dots + 4.33085u + 2.13109 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0.242379u^{21} + 0.907777u^{20} + \dots + 9.08858u + 4.51788 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.106015u^{21} - 0.00995851u^{20} + \dots + 2.57184u + 2.89213 \\ 0.348395u^{21} + 0.917735u^{20} + \dots + 6.51674u + 0.625748 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.0163379u^{21} - 0.197272u^{20} + \dots - 1.51350u - 0.468886 \\ -0.0531897u^{21} + 0.337084u^{20} + \dots + 9.03495u + 5.31697 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.0163379u^{21} - 0.197272u^{20} + \dots - 1.51350u - 0.468886 \\ -0.0531897u^{21} + 0.337084u^{20} + \dots + 9.03495u + 5.31697 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = unknown

(iv) Complex Volumes and Cusp Shapes

Solution to I_4^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.081771 - 0.344108I$		
$a = -1.198122 + 0.024840I$	$-1.85809 - 7.47524I$	$-0.22908 + 5.55460I$
$b = 0.500831 + 0.714833I$		
$u = -1.081771 + 0.344108I$		
$a = -1.198122 - 0.024840I$	$-1.85809 + 7.47524I$	$-0.22908 - 5.55460I$
$b = 0.500831 - 0.714833I$		
$u = -0.853835 - 0.533591I$		
$a = 0.484207 + 0.691979I$	$2.35273 - 3.04152I$	$4.06121 + 2.82242I$
$b = 0.094966 - 1.198131I$		
$u = -0.853835 + 0.533591I$		
$a = 0.484207 - 0.691979I$	$2.35273 + 3.04152I$	$4.06121 - 2.82242I$
$b = 0.094966 + 1.198131I$		
$u = -0.752651 - 0.945347I$		
$a = -0.595091 + 0.919581I$	$-8.47148 + 2.94672I$	$-5.79937 - 4.11787I$
$b = 1.60394 - 0.21728I$		
$u = -0.752651 + 0.945347I$		
$a = -0.595091 - 0.919581I$	$-8.47148 - 2.94672I$	$-5.79937 + 4.11787I$
$b = 1.60394 + 0.21728I$		
$u = -0.555909 - 0.782909I$		
$a = 0.409273 - 1.283123I$	$-1.31282 + 1.41699I$	$0.791306 - 0.633731I$
$b = -0.99043 + 1.31114I$		
$u = -0.555909 + 0.782909I$		
$a = 0.409273 + 1.283123I$	$-1.31282 - 1.41699I$	$0.791306 + 0.633731I$
$b = -0.99043 - 1.31114I$		
$u = -0.285332 - 0.830788I$		
$a = -0.314160 - 0.435233I$	$-3.59460 + 1.13130I$	$-0.01220 - 6.05785I$
$b = -1.67105 + 0.02430I$		
$u = -0.285332 + 0.830788I$		
$a = -0.314160 + 0.435233I$	$-3.59460 - 1.13130I$	$-0.01220 + 6.05785I$
$b = -1.67105 - 0.02430I$		

Solution to I_4^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.14927 - 1.48798I$		
$a = -0.174119 + 0.867773I$	$-8.47148 - 2.94672I$	$-5.79937 + 4.11787I$
$b = 0.067031 - 0.806341I$		
$u = -0.14927 + 1.48798I$		
$a = -0.174119 - 0.867773I$	$-8.47148 + 2.94672I$	$-5.79937 - 4.11787I$
$b = 0.067031 + 0.806341I$		
$u = -0.087548 - 1.187665I$		
$a = 0.339357 - 0.203960I$	$-3.59460 - 1.13130I$	$-0.01220 + 6.05785I$
$b = -0.011775 - 0.775560I$		
$u = -0.087548 + 1.187665I$		
$a = 0.339357 + 0.203960I$	$-3.59460 + 1.13130I$	$-0.01220 - 6.05785I$
$b = -0.011775 + 0.775560I$		
$u = 0.181376 - 1.048185I$		
$a = -0.183886 - 1.062695I$	-5.48524	0.376257
$b = 2.71263 + 2.60065I$		
$u = 0.181376 + 1.048185I$		
$a = -0.183886 + 1.062695I$	-5.48524	0.376257
$b = 2.71263 - 2.60065I$		
$u = 0.623653 - 0.552777I$		
$a = -1.41909 - 0.62786I$	$-1.31282 + 1.41699I$	$0.791306 - 0.633731I$
$b = -0.134458 - 0.204944I$		
$u = 0.623653 + 0.552777I$		
$a = -1.41909 + 0.62786I$	$-1.31282 - 1.41699I$	$0.791306 + 0.633731I$
$b = -0.134458 + 0.204944I$		
$u = 0.714099 - 0.923041I$		
$a = 0.552364 - 0.475215I$	$2.35273 - 3.04152I$	$4.06121 + 2.82242I$
$b = 0.693911 + 0.889315I$		
$u = 0.714099 + 0.923041I$		
$a = 0.552364 + 0.475215I$	$2.35273 + 3.04152I$	$4.06121 - 2.82242I$
$b = 0.693911 - 0.889315I$		
Solution to I_4^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.747184 - 1.181246I$		
$a = 0.265936 + 0.936246I$	$-1.85809 - 7.47524I$	$-0.22908 + 5.55460I$
$b = -1.36561 - 1.12781I$		
$u = 0.747184 + 1.181246I$		
$a = 0.265936 - 0.936246I$	$-1.85809 + 7.47524I$	$-0.22908 - 5.55460I$
$b = -1.36561 + 1.12781I$		

V. u-Polynomials

Crossings	u-Polynomials at each crossings
c_1, c_3, c_4	$(u+1)(u^2+1)^2(u^{17}-u^{16}+\dots-4u^2-1)(u^{22}+3u^{21}+\dots+24u+9)$
c_2	$(u-1)(u+1)^4(u^{17}+5u^{16}+\dots-8u-1)$ $(u^{22}+11u^{21}+\dots+432u+81)$
c_5, c_9	$u(u^4+3u^2+1)$ $(u^{11}-u^{10}+2u^9-u^8+4u^7-2u^6+4u^5-u^4+3u^3+u^2+1)^2$ $(u^{17}+3u^{16}+\dots+22u+8)$
c_6, c_7	$(u-1)(u^2+1)^2(u^{17}-u^{16}+\dots-4u^2-1)(u^{22}+3u^{21}+\dots+24u+9)$
c_8	$(u-1)(u^2+u-1)^2$ $(u^{11}+u^{10}-4u^9-3u^8+6u^7+2u^6-2u^5+3u^4-3u^3-3u^2+2u-1)^2$ $(u^{17}+2u^{16}+\dots+13u+4)$
c_{10}, c_{11}	$(u+1)(u^2-u-1)^2$ $(u^{11}+u^{10}-4u^9-3u^8+6u^7+2u^6-2u^5+3u^4-3u^3-3u^2+2u-1)^2$ $(u^{17}+2u^{16}+\dots+13u+4)$

VI. Riley Polynomials

Crossings	Riley Polynomials at each crossings
c_1, c_3, c_4 c_6, c_7	$(y - 1)(y + 1)^4(y^{17} + 5y^{16} + \dots - 8y - 1)$ $(y^{22} + 11y^{21} + \dots + 432y + 81)$
c_2	$(y - 1)^5(y^{17} + 13y^{16} + \dots - 12y - 1)$ $(y^{22} - y^{21} + \dots + 35640y + 6561)$
c_5, c_9	$y(y^2 + 3y + 1)^2$ $(-1 - 2y + y^2 + 15y^3 + 29y^4 + 40y^5 + 40y^6 + 32y^7 + 19y^8 + 10y^9 + 3y^{10} + y^{11})^2$ $(y^{17} + 9y^{16} + \dots - 12y - 64)$
c_8, c_{10}, c_{11}	$(y - 1)(y^2 - 3y + 1)^2$ $(-1 - 2y - 15y^2 + 23y^3 + 33y^4 - 76y^5 + 24y^6 + 52y^7 - 65y^8 + 34y^9 - 9y^{10} + y^{11})^2$ $(y^{17} - 16y^{16} + \dots + 209y - 16)$