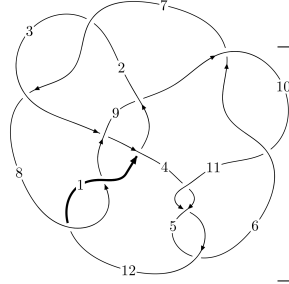
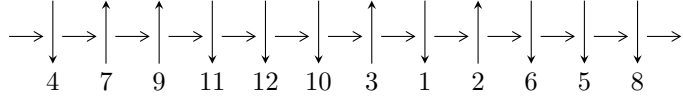


12a<sub>1060</sub> (K12a<sub>1060</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$5,12 \xrightarrow{c_5} 6,8 \xrightarrow{c_{12}} 1 \xrightarrow{c_8} 9 \xrightarrow{c_{11}} 11 \xrightarrow{c_4} 4 \xrightarrow{c_1} 2 \xrightarrow{c_3} 3 \xrightarrow{c_{10}} 10 \xrightarrow{c_6} 7 \rightsquigarrow c_2, c_7, c_9$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -2.57346 \times 10^{89} u^{110} + 1.88636 \times 10^{89} u^{109} + \dots + 1.74794 \times 10^{88} b + 1.38329 \times 10^{89}, \\ -1.32168 \times 10^{89} u^{110} + 1.72858 \times 10^{89} u^{109} + \dots + 1.74794 \times 10^{88} a + 4.52966 \times 10^{89}, \\ u^{111} - 2u^{110} + \dots - 17u + 1 \rangle$$

$$I_2^u = \langle u^{20} - u^{19} + \dots + b - u, -u^{20} + 10u^{18} + \dots + a + 1, \\ u^{21} - 10u^{19} + 42u^{17} - 92u^{15} + 99u^{13} - 14u^{11} - u^{10} - 78u^9 + 5u^8 + 60u^7 - 9u^6 + 9u^5 + 6u^4 - 18u^3 - 1 \rangle$$

$$I_3^u = \langle b, a + 1, u + 1 \rangle$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 133 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -2.57 \times 10^{89} u^{110} + 1.89 \times 10^{89} u^{109} + \dots + 1.75 \times 10^{88} b + 1.38 \times 10^{89}, -1.32 \times 10^{89} u^{110} + 1.73 \times 10^{89} u^{109} + \dots + 1.75 \times 10^{88} a + 4.53 \times 10^{89}, u^{111} - 2u^{110} + \dots - 17u + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_5 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_6 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 7.56139u^{110} - 9.88923u^{109} + \dots + 305.838u - 25.9143 \\ 14.7228u^{110} - 10.7919u^{109} + \dots + 165.490u - 7.91382 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -0.131615u^{110} + 1.70010u^{109} + \dots - 107.174u + 6.20078 \\ -8.70767u^{110} + 7.11868u^{109} + \dots - 150.414u + 11.0406 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 3.79909u^{110} - 4.42765u^{109} + \dots + 61.8715u - 3.31532 \\ 10.8836u^{110} - 8.05693u^{109} + \dots + 113.483u - 5.21542 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} u \\ u \end{pmatrix} \\ a_4 &= \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix} \\ a_2 &= \begin{pmatrix} 3.46413u^{110} - 1.77921u^{109} + \dots - 21.8214u - 0.849966 \\ 0.698222u^{110} - 0.237275u^{109} + \dots - 24.5823u + 3.29697 \end{pmatrix} \\ a_3 &= \begin{pmatrix} 0.676351u^{110} + 1.22744u^{109} + \dots - 101.879u + 5.95117 \\ -5.00556u^{110} + 4.25267u^{109} + \dots - 104.692u + 8.32936 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -u^3 + 2u \\ -u^5 + u^3 + u \end{pmatrix} \\ a_7 &= \begin{pmatrix} u^6 - 3u^4 + 2u^2 + 1 \\ u^8 - 2u^6 + 2u^2 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = -13.5527u^{110} + 17.8532u^{109} + \dots - 506.209u + 43.1001$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{111} - 16u^{110} + \dots + 15u + 1$
$c_2, c_7$	$u^{111} - u^{110} + \dots + 2080u - 1879$
$c_3$	$u^{111} - u^{110} + \dots - 49u - 5$
$c_4, c_5, c_{11}$	$u^{111} - 2u^{110} + \dots - 17u + 1$
$c_6, c_{10}$	$u^{111} + 3u^{110} + \dots - 42277u + 3245$
$c_8, c_{12}$	$u^{111} - u^{110} + \dots - 882u + 271$
$c_9$	$u^{111} + 2u^{110} + \dots - 123711u + 123383$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{111} - 4y^{110} + \dots + 567y - 1$
$c_2, c_7$	$y^{111} - 85y^{110} + \dots + 140050328y - 3530641$
$c_3$	$y^{111} - y^{110} + \dots + 881y - 25$
$c_4, c_5, c_{11}$	$y^{111} - 92y^{110} + \dots + 81y - 1$
$c_6, c_{10}$	$y^{111} + 87y^{110} + \dots + 1070147809y - 10530025$
$c_8, c_{12}$	$y^{111} - 63y^{110} + \dots + 624538y - 73441$
$c_9$	$y^{111} - 34y^{110} + \dots + 1350344005825y - 15223364689$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.081166 + 0.904115I$ $a = -0.344352 + 0.904100I$ $b = -0.205252 + 0.162622I$	$7.50937 + 0.87155I$	0
$u = -0.081166 - 0.904115I$ $a = -0.344352 - 0.904100I$ $b = -0.205252 - 0.162622I$	$7.50937 - 0.87155I$	0
$u = -0.121934 + 0.870862I$ $a = -0.96469 - 1.31541I$ $b = -1.313980 + 0.103964I$	$6.3847 + 13.3757I$	0
$u = -0.121934 - 0.870862I$ $a = -0.96469 + 1.31541I$ $b = -1.313980 - 0.103964I$	$6.3847 - 13.3757I$	0
$u = 0.154867 + 0.858936I$ $a = -0.632403 + 0.871576I$ $b = -0.954252 - 0.565366I$	$7.30644 - 4.30172I$	0
$u = 0.154867 - 0.858936I$ $a = -0.632403 - 0.871576I$ $b = -0.954252 + 0.565366I$	$7.30644 + 4.30172I$	0
$u = -0.028698 + 0.855465I$ $a = -0.428888 - 0.916164I$ $b = -0.819599 - 0.897102I$	$7.25427 + 3.69556I$	0
$u = -0.028698 - 0.855465I$ $a = -0.428888 + 0.916164I$ $b = -0.819599 + 0.897102I$	$7.25427 - 3.69556I$	0
$u = 0.091469 + 0.844247I$ $a = -1.35317 - 0.57053I$ $b = -0.863472 - 0.322494I$	$9.30952 - 6.81701I$	0
$u = 0.091469 - 0.844247I$ $a = -1.35317 + 0.57053I$ $b = -0.863472 + 0.322494I$	$9.30952 + 6.81701I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.084410 + 0.417528I$	$4.45379 - 0.29837I$	0
$a = 0.442236 - 0.588081I$		
$b = 1.139120 + 0.401544I$		
$u = 1.084410 - 0.417528I$	$4.45379 + 0.29837I$	0
$a = 0.442236 + 0.588081I$		
$b = 1.139120 - 0.401544I$		
$u = 0.080213 + 0.812540I$	$1.52000 - 6.82635I$	$0. + 6.98056I$
$a = 0.73148 - 1.41337I$		
$b = 1.282600 + 0.337159I$		
$u = 0.080213 - 0.812540I$	$1.52000 + 6.82635I$	$0. - 6.98056I$
$a = 0.73148 + 1.41337I$		
$b = 1.282600 - 0.337159I$		
$u = -0.025621 + 0.814330I$	$4.98734 + 2.15996I$	0
$a = 1.019490 - 0.056681I$		
$b = 0.598997 - 0.234326I$		
$u = -0.025621 - 0.814330I$	$4.98734 - 2.15996I$	0
$a = 1.019490 + 0.056681I$		
$b = 0.598997 + 0.234326I$		
$u = -0.526631 + 0.615019I$	$0.59594 - 4.27717I$	0
$a = -0.47851 - 1.41722I$		
$b = -0.547739 - 0.056493I$		
$u = -0.526631 - 0.615019I$	$0.59594 + 4.27717I$	0
$a = -0.47851 + 1.41722I$		
$b = -0.547739 + 0.056493I$		
$u = -1.179560 + 0.191654I$	$-1.82003 + 0.41789I$	0
$a = -0.551352 - 0.599227I$		
$b = -0.158132 - 0.269581I$		
$u = -1.179560 - 0.191654I$	$-1.82003 - 0.41789I$	0
$a = -0.551352 + 0.599227I$		
$b = -0.158132 + 0.269581I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.012361 + 0.800991I$ $a = -0.442197 - 1.094450I$ $b = -1.60146 + 0.33849I$	$6.98387 - 0.56475I$	$1.87354 + 0.I$
$u = 0.012361 - 0.800991I$ $a = -0.442197 + 1.094450I$ $b = -1.60146 - 0.33849I$	$6.98387 + 0.56475I$	$1.87354 + 0.I$
$u = 0.025664 + 0.796748I$ $a = -1.23003 + 1.38707I$ $b = -1.250320 + 0.348318I$	$2.91600 - 3.82224I$	$0. + 4.16476I$
$u = 0.025664 - 0.796748I$ $a = -1.23003 - 1.38707I$ $b = -1.250320 - 0.348318I$	$2.91600 + 3.82224I$	$0. - 4.16476I$
$u = -0.524571 + 0.585182I$ $a = 1.51013 + 0.68318I$ $b = 1.199700 - 0.103549I$	$0.56437 + 8.53514I$	$-4.00000 - 8.97660I$
$u = -0.524571 - 0.585182I$ $a = 1.51013 - 0.68318I$ $b = 1.199700 + 0.103549I$	$0.56437 - 8.53514I$	$-4.00000 + 8.97660I$
$u = 1.215450 + 0.034160I$ $a = -0.655743 - 0.538750I$ $b = -0.82287 - 1.17849I$	$-4.37066 - 2.85132I$	$0$
$u = 1.215450 - 0.034160I$ $a = -0.655743 + 0.538750I$ $b = -0.82287 + 1.17849I$	$-4.37066 + 2.85132I$	$0$
$u = -1.142310 + 0.441405I$ $a = 0.741922 + 0.868519I$ $b = 0.759050 - 0.116604I$	$3.25745 - 8.68324I$	$0$
$u = -1.142310 - 0.441405I$ $a = 0.741922 - 0.868519I$ $b = 0.759050 + 0.116604I$	$3.25745 + 8.68324I$	$0$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.230730 + 0.129770I$ $a = 0.847427 + 0.283143I$ $b = 1.58411 - 1.41763I$	$-3.36757 - 4.77773I$	0
$u = 1.230730 - 0.129770I$ $a = 0.847427 - 0.283143I$ $b = 1.58411 + 1.41763I$	$-3.36757 + 4.77773I$	0
$u = 1.175080 + 0.397243I$ $a = -0.586512 - 0.763040I$ $b = -1.220310 + 0.097965I$	$5.98708 + 2.35229I$	0
$u = 1.175080 - 0.397243I$ $a = -0.586512 + 0.763040I$ $b = -1.220310 - 0.097965I$	$5.98708 - 2.35229I$	0
$u = 1.190270 + 0.350522I$ $a = -0.790578 + 0.647954I$ $b = -1.292380 - 0.473108I$	$-1.87331 + 2.61985I$	0
$u = 1.190270 - 0.350522I$ $a = -0.790578 - 0.647954I$ $b = -1.292380 + 0.473108I$	$-1.87331 - 2.61985I$	0
$u = 1.25185$ $a = 0.708215$ $b = 6.74388$	$-0.842109$	0
$u = -0.129040 + 0.730302I$ $a = 1.05885 + 1.38972I$ $b = 0.986008 + 0.154802I$	$1.16972 + 3.02941I$	$0.581656 - 0.502191I$
$u = -0.129040 - 0.730302I$ $a = 1.05885 - 1.38972I$ $b = 0.986008 - 0.154802I$	$1.16972 - 3.02941I$	$0.581656 + 0.502191I$
$u = -1.273620 + 0.076602I$ $a = -0.344736 - 0.467111I$ $b = 0.378767 + 0.209717I$	$-1.89161 + 0.63320I$	0



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.273620 - 0.076602I$ $a = -0.344736 + 0.467111I$ $b = 0.378767 - 0.209717I$	$-1.89161 - 0.63320I$	0
$u = -0.052261 + 0.719313I$ $a = 0.56144 + 1.85689I$ $b = 0.362230 + 0.199391I$	$0.82057 + 2.54626I$	$-3.60718 - 1.85382I$
$u = -0.052261 - 0.719313I$ $a = 0.56144 - 1.85689I$ $b = 0.362230 - 0.199391I$	$0.82057 - 2.54626I$	$-3.60718 + 1.85382I$
$u = -1.193200 + 0.465317I$ $a = -0.743332 + 0.064065I$ $b = -1.140780 - 0.292617I$	$4.08896 + 4.00061I$	0
$u = -1.193200 - 0.465317I$ $a = -0.743332 - 0.064065I$ $b = -1.140780 + 0.292617I$	$4.08896 - 4.00061I$	0
$u = 1.279440 + 0.124995I$ $a = -0.161902 - 0.194584I$ $b = -0.565355 - 1.026320I$	$-4.72872 - 2.56138I$	0
$u = 1.279440 - 0.124995I$ $a = -0.161902 + 0.194584I$ $b = -0.565355 + 1.026320I$	$-4.72872 + 2.56138I$	0
$u = -1.292750 + 0.034714I$ $a = 1.015070 - 0.528316I$ $b = 3.98562 - 0.36189I$	$-5.84342 + 3.49242I$	0
$u = -1.292750 - 0.034714I$ $a = 1.015070 + 0.528316I$ $b = 3.98562 + 0.36189I$	$-5.84342 - 3.49242I$	0
$u = -1.260740 + 0.296765I$ $a = -0.974598 - 0.581114I$ $b = -1.86237 - 1.41018I$	$-2.94268 + 1.10354I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.260740 - 0.296765I$ $a = -0.974598 + 0.581114I$ $b = -1.86237 + 1.41018I$	$-2.94268 - 1.10354I$	0
$u = 1.249570 + 0.345703I$ $a = 0.603798 - 0.930670I$ $b = -0.138375 - 0.619119I$	$-0.866061 - 0.293007I$	0
$u = 1.249570 - 0.345703I$ $a = 0.603798 + 0.930670I$ $b = -0.138375 + 0.619119I$	$-0.866061 + 0.293007I$	0
$u = -1.245970 + 0.359010I$ $a = 0.251361 - 0.577708I$ $b = 0.535194 - 0.101397I$	$1.21676 + 2.06299I$	0
$u = -1.245970 - 0.359010I$ $a = 0.251361 + 0.577708I$ $b = 0.535194 + 0.101397I$	$1.21676 - 2.06299I$	0
$u = 1.261040 + 0.349927I$ $a = -0.733629 - 0.044182I$ $b = -3.33029 + 2.29901I$	$3.11498 - 3.57845I$	0
$u = 1.261040 - 0.349927I$ $a = -0.733629 + 0.044182I$ $b = -3.33029 - 2.29901I$	$3.11498 + 3.57845I$	0
$u = -1.246320 + 0.399264I$ $a = 0.508156 + 0.407138I$ $b = -0.756437 + 0.263088I$	$3.48869 + 0.80412I$	0
$u = -1.246320 - 0.399264I$ $a = 0.508156 - 0.407138I$ $b = -0.756437 - 0.263088I$	$3.48869 - 0.80412I$	0
$u = -1.279340 + 0.353280I$ $a = 0.525220 + 0.477688I$ $b = 0.562776 - 1.283690I$	$2.96533 + 4.72137I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.279340 - 0.353280I$ $a = 0.525220 - 0.477688I$ $b = 0.562776 + 1.283690I$	$2.96533 - 4.72137I$	0
$u = -1.288410 + 0.349720I$ $a = -1.044060 + 0.445837I$ $b = -2.76410 - 1.24036I$	$-1.17957 + 7.95243I$	0
$u = -1.288410 - 0.349720I$ $a = -1.044060 - 0.445837I$ $b = -2.76410 + 1.24036I$	$-1.17957 - 7.95243I$	0
$u = 1.286620 + 0.362863I$ $a = 0.215037 + 0.603548I$ $b = 1.142380 + 0.534124I$	$0.90063 - 6.39648I$	0
$u = 1.286620 - 0.362863I$ $a = 0.215037 - 0.603548I$ $b = 1.142380 - 0.534124I$	$0.90063 + 6.39648I$	0
$u = 1.293240 + 0.390759I$ $a = -0.647394 - 0.092804I$ $b = -0.62304 + 1.60161I$	$3.13563 - 8.16662I$	0
$u = 1.293240 - 0.390759I$ $a = -0.647394 + 0.092804I$ $b = -0.62304 - 1.60161I$	$3.13563 + 8.16662I$	0
$u = 1.316370 + 0.314217I$ $a = 1.066920 - 0.099320I$ $b = 2.70014 - 1.07266I$	$-3.50013 - 6.30583I$	0
$u = 1.316370 - 0.314217I$ $a = 1.066920 + 0.099320I$ $b = 2.70014 + 1.07266I$	$-3.50013 + 6.30583I$	0
$u = -1.357420 + 0.123005I$ $a = 0.055884 - 0.790870I$ $b = 0.219826 - 1.339850I$	$-1.79691 + 5.42824I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.357420 - 0.123005I$ $a = 0.055884 + 0.790870I$ $b = 0.219826 + 1.339850I$	$-1.79691 - 5.42824I$	0
$u = -1.361100 + 0.084061I$ $a = -0.889472 + 0.178559I$ $b = -4.43462 - 0.05589I$	$-8.65164 + 5.28818I$	0
$u = -1.361100 - 0.084061I$ $a = -0.889472 - 0.178559I$ $b = -4.43462 + 0.05589I$	$-8.65164 - 5.28818I$	0
$u = -1.354580 + 0.206679I$ $a = 0.753347 + 0.206126I$ $b = 3.12215 + 1.39177I$	$-7.16797 + 1.58311I$	0
$u = -1.354580 - 0.206679I$ $a = 0.753347 - 0.206126I$ $b = 3.12215 - 1.39177I$	$-7.16797 - 1.58311I$	0
$u = -1.322880 + 0.358837I$ $a = 0.959315 - 0.094899I$ $b = 3.52906 + 1.42336I$	$-2.87719 + 11.04810I$	0
$u = -1.322880 - 0.358837I$ $a = 0.959315 + 0.094899I$ $b = 3.52906 - 1.42336I$	$-2.87719 - 11.04810I$	0
$u = 0.527747 + 0.332177I$ $a = 0.694115 + 0.501497I$ $b = 1.059300 + 0.321123I$	$3.19985 + 0.32140I$	$1.59922 + 2.05291I$
$u = 0.527747 - 0.332177I$ $a = 0.694115 - 0.501497I$ $b = 1.059300 - 0.321123I$	$3.19985 - 0.32140I$	$1.59922 - 2.05291I$
$u = 1.341820 + 0.311397I$ $a = 1.028620 + 0.219802I$ $b = 2.94137 - 1.00859I$	$-3.46066 - 6.81605I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.341820 - 0.311397I$ $a = 1.028620 - 0.219802I$ $b = 2.94137 + 1.00859I$	$-3.46066 + 6.81605I$	0
$u = 1.380850 + 0.001402I$ $a = -1.002190 + 0.099681I$ $b = -3.63865 + 0.11066I$	$-7.48663 + 0.05717I$	0
$u = 1.380850 - 0.001402I$ $a = -1.002190 - 0.099681I$ $b = -3.63865 - 0.11066I$	$-7.48663 - 0.05717I$	0
$u = -0.618101 + 0.029425I$ $a = -1.74047 + 0.02330I$ $b = -0.535160 - 0.050220I$	$-1.53250 + 0.00940I$	$-7.61099 + 0.23089I$
$u = -0.618101 - 0.029425I$ $a = -1.74047 - 0.02330I$ $b = -0.535160 + 0.050220I$	$-1.53250 - 0.00940I$	$-7.61099 - 0.23089I$
$u = -1.332360 + 0.374895I$ $a = -0.013321 + 0.926101I$ $b = -0.998412 + 0.993180I$	$4.84444 + 11.19960I$	0
$u = -1.332360 - 0.374895I$ $a = -0.013321 - 0.926101I$ $b = -0.998412 - 0.993180I$	$4.84444 - 11.19960I$	0
$u = 0.387681 + 0.471766I$ $a = 0.94998 + 1.12985I$ $b = 0.192196 - 0.091930I$	$3.65065 - 3.48280I$	$1.08914 + 6.57604I$
$u = 0.387681 - 0.471766I$ $a = 0.94998 - 1.12985I$ $b = 0.192196 + 0.091930I$	$3.65065 + 3.48280I$	$1.08914 - 6.57604I$
$u = 1.331550 + 0.416484I$ $a = 0.431825 - 0.390425I$ $b = 0.625797 - 0.534575I$	$3.09221 - 5.59637I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.331550 - 0.416484I$ $a = 0.431825 + 0.390425I$ $b = 0.625797 + 0.534575I$	$3.09221 + 5.59637I$	0
$u = 0.239442 + 0.553403I$ $a = 0.29215 - 1.63161I$ $b = 0.814891 + 0.000066I$	$-2.15238 + 1.18175I$	$-5.85912 + 1.80919I$
$u = 0.239442 - 0.553403I$ $a = 0.29215 + 1.63161I$ $b = 0.814891 - 0.000066I$	$-2.15238 - 1.18175I$	$-5.85912 - 1.80919I$
$u = 1.354290 + 0.385786I$ $a = -1.013040 - 0.215829I$ $b = -3.22338 + 1.21261I$	$1.7439 - 17.8882I$	0
$u = 1.354290 - 0.385786I$ $a = -1.013040 + 0.215829I$ $b = -3.22338 - 1.21261I$	$1.7439 + 17.8882I$	0
$u = -1.37149 + 0.37859I$ $a = -0.688647 + 0.081503I$ $b = -2.89193 - 0.66737I$	$2.49624 + 8.75887I$	0
$u = -1.37149 - 0.37859I$ $a = -0.688647 - 0.081503I$ $b = -2.89193 + 0.66737I$	$2.49624 - 8.75887I$	0
$u = 1.42545 + 0.14891I$ $a = 0.929723 + 0.271581I$ $b = 3.68084 - 0.20743I$	$-5.71189 - 10.93540I$	0
$u = 1.42545 - 0.14891I$ $a = 0.929723 - 0.271581I$ $b = 3.68084 + 0.20743I$	$-5.71189 + 10.93540I$	0
$u = 0.449955 + 0.306106I$ $a = -2.03754 + 0.58119I$ $b = -1.245410 - 0.306755I$	$-3.08409 - 4.01496I$	$-8.48201 + 7.35166I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.449955 - 0.306106I$ $a = -2.03754 - 0.58119I$ $b = -1.245410 + 0.306755I$	$-3.08409 + 4.01496I$	$-8.48201 - 7.35166I$
$u = -0.105666 + 0.512091I$ $a = 0.97329 + 1.87270I$ $b = 0.490136 + 0.627445I$	$0.52426 + 2.56205I$	$0.27637 - 5.10765I$
$u = -0.105666 - 0.512091I$ $a = 0.97329 - 1.87270I$ $b = 0.490136 - 0.627445I$	$0.52426 - 2.56205I$	$0.27637 + 5.10765I$
$u = 1.47079 + 0.14608I$ $a = -0.745847 + 0.294962I$ $b = -2.71132 + 0.77604I$	$-5.95978 + 1.70857I$	0
$u = 1.47079 - 0.14608I$ $a = -0.745847 - 0.294962I$ $b = -2.71132 - 0.77604I$	$-5.95978 - 1.70857I$	0
$u = -1.50434$ $a = 0.492040$ $b = 2.97475$	$-3.63276$	0
$u = -0.225847 + 0.327044I$ $a = -0.800511 + 0.558951I$ $b = -0.020085 + 0.267612I$	$-0.235196 + 0.938220I$	$-4.68352 - 7.13050I$
$u = -0.225847 - 0.327044I$ $a = -0.800511 - 0.558951I$ $b = -0.020085 - 0.267612I$	$-0.235196 - 0.938220I$	$-4.68352 + 7.13050I$
$u = 0.151934 + 0.115584I$ $a = 6.77942 - 0.80780I$ $b = 0.686578 - 0.179927I$	$-1.43186 - 2.95721I$	$-9.1241 + 11.4688I$
$u = 0.151934 - 0.115584I$ $a = 6.77942 + 0.80780I$ $b = 0.686578 + 0.179927I$	$-1.43186 + 2.95721I$	$-9.1241 - 11.4688I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.119052$		
$a = -5.01443$	2.72207	12.4830
$b = 1.98261$		



**II.**

$$I_2^u = \langle u^{20} - u^{19} + \dots + b - u, -u^{20} + 10u^{18} + \dots + a + 1, u^{21} - 10u^{19} + \dots - 18u^3 - 1 \rangle$$

**(i) Arc colorings**

$$\begin{aligned} a_5 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_6 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_8 &= \begin{pmatrix} u^{20} - 10u^{18} + \dots - 3u - 1 \\ -u^{20} + u^{19} + \dots - 6u^2 + u \end{pmatrix} \\ a_1 &= \begin{pmatrix} u^{19} + u^{18} + \dots + 5u + 2 \\ -u^{20} + 3u^{19} + \dots - u + 2 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -u^{19} + 9u^{17} + \dots + 3u + 1 \\ -2u^{20} - u^{19} + \dots + u - 1 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} u \\ u \end{pmatrix} \\ a_4 &= \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix} \\ a_2 &= \begin{pmatrix} u^{20} + u^{19} + \dots + 6u + 2 \\ u^{20} + 3u^{19} + \dots + 6u^2 + 2 \end{pmatrix} \\ a_3 &= \begin{pmatrix} u^{19} + u^{18} + \dots + 5u + 3 \\ 3u^{19} + u^{18} + \dots - u + 2 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -u^3 + 2u \\ -u^5 + u^3 + u \end{pmatrix} \\ a_7 &= \begin{pmatrix} u^6 - 3u^4 + 2u^2 + 1 \\ u^8 - 2u^6 + 2u^2 \end{pmatrix} \end{aligned}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes**

$$\begin{aligned} &= -12u^{19} - 2u^{18} + 100u^{17} + 17u^{16} - 336u^{15} - 58u^{14} + 535u^{13} + 92u^{12} - 271u^{11} - \\ &41u^{10} - 324u^9 - 56u^8 + 442u^7 + 40u^6 - 28u^5 + 46u^4 - 134u^3 - 32u^2 + 12u - 14 \end{aligned}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{21} - 2u^{19} + \dots - 6u + 1$
$c_2$	$u^{21} + u^{20} + \dots + u + 1$
$c_3$	$u^{21} - 2u^{19} + \dots + 3u^2 + 1$
$c_4, c_5$	$u^{21} - 10u^{19} + \dots - 18u^3 - 1$
$c_6$	$u^{21} + 6u^{19} + \dots + 3u^2 - 1$
$c_7$	$u^{21} - u^{20} + \dots + u - 1$
$c_8$	$u^{21} - u^{20} + \dots + u - 1$
$c_9$	$u^{21} + 3u^{19} + \dots - 2u^2 + 1$
$c_{10}$	$u^{21} + 6u^{19} + \dots - 3u^2 + 1$
$c_{11}$	$u^{21} - 10u^{19} + \dots - 18u^3 + 1$
$c_{12}$	$u^{21} + u^{20} + \dots + u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{21} - 4y^{20} + \dots + 10y - 1$
$c_2, c_7$	$y^{21} - 21y^{20} + \dots + 15y - 1$
$c_3$	$y^{21} - 4y^{20} + \dots - 6y - 1$
$c_4, c_5, c_{11}$	$y^{21} - 20y^{20} + \dots + 12y^2 - 1$
$c_6, c_{10}$	$y^{21} + 12y^{20} + \dots + 6y - 1$
$c_8, c_{12}$	$y^{21} - 15y^{20} + \dots + 21y - 1$
$c_9$	$y^{21} + 6y^{20} + \dots + 4y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.062614 + 0.857160I$ $a = 0.275352 + 0.744219I$ $b = 0.991659 + 0.241341I$	$7.09483 + 2.69700I$	$0.204052 - 0.960418I$
$u = -0.062614 - 0.857160I$ $a = 0.275352 - 0.744219I$ $b = 0.991659 - 0.241341I$	$7.09483 - 2.69700I$	$0.204052 + 0.960418I$
$u = -1.18462$ $a = 0.514078$ $b = -3.17275$	$-0.0653881$	$2.89470$
$u = 1.235030 + 0.104057I$ $a = -0.770955 - 0.434248I$ $b = -1.68506 - 0.31727I$	$-4.45553 - 3.99750I$	$-8.33700 + 7.35069I$
$u = 1.235030 - 0.104057I$ $a = -0.770955 + 0.434248I$ $b = -1.68506 + 0.31727I$	$-4.45553 + 3.99750I$	$-8.33700 - 7.35069I$
$u = 1.234780 + 0.272929I$ $a = 0.736844 - 0.846584I$ $b = 0.398323 - 0.870978I$	$-2.77607 + 0.23467I$	$-9.48318 - 3.28637I$
$u = 1.234780 - 0.272929I$ $a = 0.736844 + 0.846584I$ $b = 0.398323 + 0.870978I$	$-2.77607 - 0.23467I$	$-9.48318 + 3.28637I$
$u = -1.212920 + 0.392860I$ $a = -0.439696 - 0.262167I$ $b = 0.203010 + 0.888489I$	$3.55654 + 1.79152I$	$-2.35096 - 2.63279I$
$u = -1.212920 - 0.392860I$ $a = -0.439696 + 0.262167I$ $b = 0.203010 - 0.888489I$	$3.55654 - 1.79152I$	$-2.35096 + 2.63279I$
$u = 0.072517 + 0.710236I$ $a = -1.26753 + 1.64767I$ $b = -1.045360 + 0.236003I$	$0.77767 - 3.77401I$	$-4.35410 + 8.39040I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.072517 - 0.710236I$ $a = -1.26753 - 1.64767I$ $b = -1.045360 - 0.236003I$	$0.77767 + 3.77401I$	$-4.35410 - 8.39040I$
$u = -1.323560 + 0.298366I$ $a = -1.111640 + 0.313500I$ $b = -3.17414 - 0.98120I$	$-3.62134 + 7.43161I$	$-8.6486 - 11.9040I$
$u = -1.323560 - 0.298366I$ $a = -1.111640 - 0.313500I$ $b = -3.17414 + 0.98120I$	$-3.62134 - 7.43161I$	$-8.6486 + 11.9040I$
$u = 1.316400 + 0.393822I$ $a = 0.515998 + 0.022497I$ $b = 1.35440 - 1.33801I$	$2.78443 - 7.19164I$	$-4.22867 + 4.01785I$
$u = 1.316400 - 0.393822I$ $a = 0.515998 - 0.022497I$ $b = 1.35440 + 1.33801I$	$2.78443 + 7.19164I$	$-4.22867 - 4.01785I$
$u = -1.391350 + 0.102602I$ $a = 0.845334 + 0.317790I$ $b = 3.00093 + 0.78369I$	$-6.34020 - 0.86818I$	$-9.18780 - 0.27914I$
$u = -1.391350 - 0.102602I$ $a = 0.845334 - 0.317790I$ $b = 3.00093 - 0.78369I$	$-6.34020 + 0.86818I$	$-9.18780 + 0.27914I$
$u = 1.47523$ $a = -0.549398$ $b = -3.38448$	$-3.89149$	$-19.3050$
$u = -0.385686$ $a = -1.78797$ $b = -2.12563$	$2.41587$	$-14.8360$
$u = 0.179252 + 0.337282I$ $a = 0.12794 - 3.11208I$ $b = 0.297662 - 0.095157I$	$-1.18464 + 2.46905I$	$-1.99075 + 0.76816I$

	Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u =$	$0.179252 - 0.337282I$		
$a =$	$0.12794 + 3.11208I$	$-1.18464 - 2.46905I$	$-1.99075 - 0.76816I$
$b =$	$0.297662 + 0.095157I$		

$$\text{III. } I_3^u = \langle b, a + 1, u + 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

(ii) Obstruction class =  $-1$

(iii) Cusp Shapes =  $-6$

(iv) **u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u - 1$
$c_2, c_4, c_5$ $c_7, c_8, c_9$ $c_{11}, c_{12}$	$u + 1$
$c_3, c_6, c_{10}$	$u$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$ $c_5, c_7, c_8$ $c_9, c_{11}, c_{12}$	$y - 1$
$c_3, c_6, c_{10}$	$y$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.00000$		
$a = -1.00000$	-1.64493	-6.00000
$b = 0$		

#### IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u - 1)(u^{21} - 2u^{19} + \dots - 6u + 1)(u^{111} - 16u^{110} + \dots + 15u + 1)$
$c_2$	$(u + 1)(u^{21} + u^{20} + \dots + u + 1)(u^{111} - u^{110} + \dots + 2080u - 1879)$
$c_3$	$u(u^{21} - 2u^{19} + \dots + 3u^2 + 1)(u^{111} - u^{110} + \dots - 49u - 5)$
$c_4, c_5$	$(u + 1)(u^{21} - 10u^{19} + \dots - 18u^3 - 1)(u^{111} - 2u^{110} + \dots - 17u + 1)$
$c_6$	$u(u^{21} + 6u^{19} + \dots + 3u^2 - 1)(u^{111} + 3u^{110} + \dots - 42277u + 3245)$
$c_7$	$(u + 1)(u^{21} - u^{20} + \dots + u - 1)(u^{111} - u^{110} + \dots + 2080u - 1879)$
$c_8$	$(u + 1)(u^{21} - u^{20} + \dots + u - 1)(u^{111} - u^{110} + \dots - 882u + 271)$
$c_9$	$(u + 1)(u^{21} + 3u^{19} + \dots - 2u^2 + 1)$ $\cdot (u^{111} + 2u^{110} + \dots - 123711u + 123383)$
$c_{10}$	$u(u^{21} + 6u^{19} + \dots - 3u^2 + 1)(u^{111} + 3u^{110} + \dots - 42277u + 3245)$
$c_{11}$	$(u + 1)(u^{21} - 10u^{19} + \dots - 18u^3 + 1)(u^{111} - 2u^{110} + \dots - 17u + 1)$
$c_{12}$	$(u + 1)(u^{21} + u^{20} + \dots + u + 1)(u^{111} - u^{110} + \dots - 882u + 271)$

## V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$(y - 1)(y^{21} - 4y^{20} + \dots + 10y - 1)(y^{111} - 4y^{110} + \dots + 567y - 1)$
$c_2, c_7$	$(y - 1)(y^{21} - 21y^{20} + \dots + 15y - 1)$ $\cdot (y^{111} - 85y^{110} + \dots + 140050328y - 3530641)$
$c_3$	$y(y^{21} - 4y^{20} + \dots - 6y - 1)(y^{111} - y^{110} + \dots + 881y - 25)$
$c_4, c_5, c_{11}$	$(y - 1)(y^{21} - 20y^{20} + \dots + 12y^2 - 1)(y^{111} - 92y^{110} + \dots + 81y - 1)$
$c_6, c_{10}$	$y(y^{21} + 12y^{20} + \dots + 6y - 1)$ $\cdot (y^{111} + 87y^{110} + \dots + 1070147809y - 10530025)$
$c_8, c_{12}$	$(y - 1)(y^{21} - 15y^{20} + \dots + 21y - 1)$ $\cdot (y^{111} - 63y^{110} + \dots + 624538y - 73441)$
$c_9$	$(y - 1)(y^{21} + 6y^{20} + \dots + 4y - 1)$ $\cdot (y^{111} - 34y^{110} + \dots + 1350344005825y - 15223364689)$