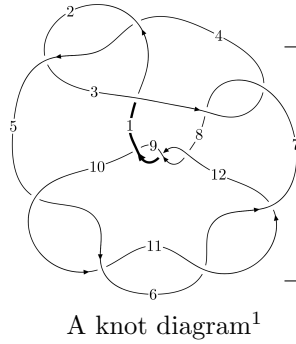
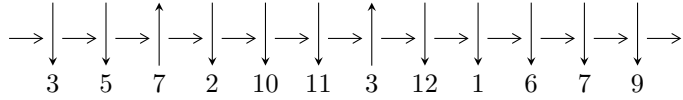


12n<sub>0191</sub> (K12n<sub>0191</sub>)



**Linearized knot diagram**



**Solving Sequence**

$$6, 10 \xrightarrow{c_{10}} 11 \xrightarrow{c_6} 3, 7 \xrightarrow{c_7} 8 \xrightarrow{c_{11}} 12 \xrightarrow{c_5} 5 \xrightarrow{c_2} 2 \xrightarrow{c_1} 1 \xrightarrow{c_4} 4 \xrightarrow{c_9} 9 \rightsquigarrow c_3, c_8, c_{12}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 2.93013 \times 10^{22} u^{41} - 2.55618 \times 10^{22} u^{40} + \dots + 3.19018 \times 10^{22} b + 3.37541 \times 10^{22},$$

$$3.37341 \times 10^{22} u^{41} - 5.52290 \times 10^{22} u^{40} + \dots + 3.19018 \times 10^{22} a - 5.34100 \times 10^{22}, u^{42} - 2u^{41} + \dots + 9u^2 - 1 \rangle$$

$$I_2^u = \langle b - 1, -u^2 + a - u + 1, u^3 + u^2 - 2u - 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 45 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle 2.93 \times 10^{22} u^{41} - 2.56 \times 10^{22} u^{40} + \dots + 3.19 \times 10^{22} b + 3.38 \times 10^{22}, 3.37 \times 10^{22} u^{41} - 5.52 \times 10^{22} u^{40} + \dots + 3.19 \times 10^{22} a - 5.34 \times 10^{22}, u^{42} - 2u^{41} + \dots + 9u^2 - 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -1.05743u^{41} + 1.73122u^{40} + \dots + 2.10719u + 1.67420 \\ -0.918482u^{41} + 0.801265u^{40} + \dots - 1.32965u - 1.05806 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -0.468740u^{41} + 1.75288u^{40} + \dots - 2.79645u + 2.00796 \\ 0.403032u^{41} - 0.477459u^{40} + \dots - 0.178275u - 0.123472 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.944557u^{41} + 1.20115u^{40} + \dots + 2.24614u + 1.02215 \\ -0.805605u^{41} + 0.271202u^{40} + \dots - 1.19070u - 1.71011 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0.557571u^{41} - 2.03034u^{40} + \dots + 3.30377u - 2.22423 \\ 0.0502449u^{41} - 0.799422u^{40} + \dots + 0.797791u - 1.15514 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -1.10864u^{41} + 1.93014u^{40} + \dots + 1.65865u + 1.89346 \\ -0.771455u^{41} + 0.605910u^{40} + \dots - 0.932314u - 1.18080 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -1.09560u^{41} + 2.57105u^{40} + \dots - 3.54399u + 2.46417 \\ 0.00573169u^{41} + 0.199584u^{40} + \dots - 0.855377u + 0.139917 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\mathbf{(iii) Cusp Shapes} = -\frac{14504839839598429454722}{31901842262824074426539} u^{41} + \frac{28913484959271594911639}{31901842262824074426539} u^{40} + \dots + \frac{572906090932607375763123}{31901842262824074426539} u - \frac{222969079138844677276793}{31901842262824074426539}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{42} + 20u^{41} + \dots + 439u + 1$
$c_2, c_4$	$u^{42} - 4u^{41} + \dots + 31u - 1$
$c_3, c_7$	$u^{42} - 3u^{41} + \dots + 4u + 8$
$c_5, c_6, c_{10}$ $c_{11}$	$u^{42} - 2u^{41} + \dots + 9u^2 - 1$
$c_8, c_9, c_{12}$	$u^{42} + 2u^{41} + \dots + 4u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{42} + 8y^{41} + \dots - 130935y + 1$
$c_2, c_4$	$y^{42} - 20y^{41} + \dots - 439y + 1$
$c_3, c_7$	$y^{42} - 21y^{41} + \dots - 4304y + 64$
$c_5, c_6, c_{10}$ $c_{11}$	$y^{42} - 46y^{41} + \dots - 18y + 1$
$c_8, c_9, c_{12}$	$y^{42} - 34y^{41} + \dots - 18y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.622716 + 0.726936I$ $a = 0.249920 - 0.575224I$ $b = -1.08189 - 1.07126I$	$-1.64578 + 10.08720I$	$-11.9616 - 7.8917I$
$u = -0.622716 - 0.726936I$ $a = 0.249920 + 0.575224I$ $b = -1.08189 + 1.07126I$	$-1.64578 - 10.08720I$	$-11.9616 + 7.8917I$
$u = 0.630110 + 0.667113I$ $a = -0.067316 - 0.527398I$ $b = 1.195850 - 0.754840I$	$3.26280 - 5.05879I$	$-7.66762 + 6.22497I$
$u = 0.630110 - 0.667113I$ $a = -0.067316 + 0.527398I$ $b = 1.195850 + 0.754840I$	$3.26280 + 5.05879I$	$-7.66762 - 6.22497I$
$u = -0.410576 + 0.797115I$ $a = 0.590560 + 0.729454I$ $b = 0.654792 - 0.588986I$	$-1.01128 - 5.04828I$	$-10.54510 + 3.70923I$
$u = -0.410576 - 0.797115I$ $a = 0.590560 - 0.729454I$ $b = 0.654792 + 0.588986I$	$-1.01128 + 5.04828I$	$-10.54510 - 3.70923I$
$u = -0.613330 + 0.550269I$ $a = -0.152550 - 0.404189I$ $b = -1.211510 - 0.276966I$	$0.340193 - 0.146534I$	$-9.04090 - 2.32576I$
$u = -0.613330 - 0.550269I$ $a = -0.152550 + 0.404189I$ $b = -1.211510 + 0.276966I$	$0.340193 + 0.146534I$	$-9.04090 + 2.32576I$
$u = 0.384114 + 0.702008I$ $a = -0.371736 + 1.039810I$ $b = -0.789326 - 0.194769I$	$3.99048 + 0.46078I$	$-5.35173 - 0.25994I$
$u = 0.384114 - 0.702008I$ $a = -0.371736 - 1.039810I$ $b = -0.789326 + 0.194769I$	$3.99048 - 0.46078I$	$-5.35173 + 0.25994I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.418033 + 0.606743I$ $a = 0.084600 + 1.400980I$ $b = 0.934140 + 0.238589I$	$0.90530 + 4.12360I$	$-8.68102 - 5.50502I$
$u = -0.418033 - 0.606743I$ $a = 0.084600 - 1.400980I$ $b = 0.934140 - 0.238589I$	$0.90530 - 4.12360I$	$-8.68102 + 5.50502I$
$u = 1.36749$ $a = 0.995996$ $b = 1.03484$	$-6.50001$	$-13.6470$
$u = 0.505963 + 0.303182I$ $a = 1.89815 + 1.24925I$ $b = -0.202771 + 1.082850I$	$-4.34422 - 3.06091I$	$-15.9828 + 7.3630I$
$u = 0.505963 - 0.303182I$ $a = 1.89815 - 1.24925I$ $b = -0.202771 - 1.082850I$	$-4.34422 + 3.06091I$	$-15.9828 - 7.3630I$
$u = 1.38819 + 0.34209I$ $a = -0.381252 + 0.184770I$ $b = 0.108566 - 0.214622I$	$-6.74773 + 0.95826I$	$0$
$u = 1.38819 - 0.34209I$ $a = -0.381252 - 0.184770I$ $b = 0.108566 + 0.214622I$	$-6.74773 - 0.95826I$	$0$
$u = -1.43233$ $a = 10.9436$ $b = 11.6572$	$-8.26088$	$77.1970$
$u = -0.561117$ $a = -2.94490$ $b = -0.320377$	$-5.90144$	$-19.1780$
$u = -1.44186 + 0.20173I$ $a = 0.423668 + 1.035100I$ $b = 0.236187 + 0.379056I$	$-1.83573 + 2.73592I$	$0$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.44186 - 0.20173I$ $a = 0.423668 - 1.035100I$ $b = 0.236187 - 0.379056I$	$-1.83573 - 2.73592I$	0
$u = -1.47192$ $a = 1.74936$ $b = 2.58881$	$-8.07301$	0
$u = 1.47089 + 0.06692I$ $a = 0.12566 + 2.06315I$ $b = -0.51913 + 1.71572I$	$-6.78843 - 2.26447I$	0
$u = 1.47089 - 0.06692I$ $a = 0.12566 - 2.06315I$ $b = -0.51913 - 1.71572I$	$-6.78843 + 2.26447I$	0
$u = 1.48233 + 0.17827I$ $a = -0.54943 + 1.55713I$ $b = -0.523659 + 0.673391I$	$-5.29803 - 6.90242I$	0
$u = 1.48233 - 0.17827I$ $a = -0.54943 - 1.55713I$ $b = -0.523659 - 0.673391I$	$-5.29803 + 6.90242I$	0
$u = -1.51313 + 0.07664I$ $a = -0.40049 + 1.89572I$ $b = 0.471789 + 1.251810I$	$-11.04660 + 4.37109I$	0
$u = -1.51313 - 0.07664I$ $a = -0.40049 - 1.89572I$ $b = 0.471789 - 1.251810I$	$-11.04660 - 4.37109I$	0
$u = 1.52457$ $a = 0.592680$ $b = -0.635110$	$-12.8376$	0
$u = -0.349126 + 0.309363I$ $a = -1.252420 + 0.444201I$ $b = 0.207903 + 0.938910I$	$-0.798095 + 1.043220I$	$-8.93837 - 6.28488I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.349126 - 0.309363I$ $a = -1.252420 - 0.444201I$ $b = 0.207903 - 0.938910I$	$-0.798095 - 1.043220I$	$-8.93837 + 6.28488I$
$u = -0.464350$ $a = -0.268787$ $b = -0.520788$	$-0.827896$	$-11.7750$
$u = 1.57075 + 0.24415I$ $a = 0.42013 - 1.89705I$ $b = 1.31507 - 1.60521I$	$-8.8765 - 13.6938I$	0
$u = 1.57075 - 0.24415I$ $a = 0.42013 + 1.89705I$ $b = 1.31507 + 1.60521I$	$-8.8765 + 13.6938I$	0
$u = 0.175152 + 0.368374I$ $a = 0.719520 - 0.426879I$ $b = 0.25392 + 1.93248I$	$-3.37453 + 0.76491I$	$-10.40964 + 7.93136I$
$u = 0.175152 - 0.368374I$ $a = 0.719520 + 0.426879I$ $b = 0.25392 - 1.93248I$	$-3.37453 - 0.76491I$	$-10.40964 - 7.93136I$
$u = -1.57812 + 0.22378I$ $a = -0.70680 - 1.63267I$ $b = -1.47281 - 1.33651I$	$-4.07471 + 8.38744I$	0
$u = -1.57812 - 0.22378I$ $a = -0.70680 + 1.63267I$ $b = -1.47281 + 1.33651I$	$-4.07471 - 8.38744I$	0
$u = 1.60757 + 0.18431I$ $a = 0.894775 - 1.082450I$ $b = 1.49803 - 0.87021I$	$-7.24321 - 2.57720I$	0
$u = 1.60757 - 0.18431I$ $a = 0.894775 + 1.082450I$ $b = 1.49803 + 0.87021I$	$-7.24321 + 2.57720I$	0



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.321929$ $a = 2.42803$ $b = -0.909883$	-2.06972	3.71630
$u = -1.82062$ $a = -0.545929$ $b = -1.04503$	-19.0753	0

$$\text{II. } I_2^u = \langle b - 1, -u^2 + a - u + 1, u^3 + u^2 - 2u - 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^2 + u - 1 \\ 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u \\ u^2 - u - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u \\ u^2 - u - 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^2 + 1 \\ -u^2 + u + 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^2 - 1 \\ -u + 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ -u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^2 + u - 1 \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-u^2 + 4u - 24$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$(u - 1)^3$
$c_3, c_7$	$u^3$
$c_4$	$(u + 1)^3$
$c_5, c_6, c_8$ $c_9$	$u^3 - u^2 - 2u + 1$
$c_{10}, c_{11}, c_{12}$	$u^3 + u^2 - 2u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y - 1)^3$
$c_3, c_7$	$y^3$
$c_5, c_6, c_8$ $c_9, c_{10}, c_{11}$ $c_{12}$	$y^3 - 5y^2 + 6y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.24698$ $a = 1.80194$ $b = 1.00000$	-7.98968	-20.5670
$u = -0.445042$ $a = -1.24698$ $b = 1.00000$	-2.34991	-25.9780
$u = -1.80194$ $a = 0.445042$ $b = 1.00000$	-19.2692	-34.4550

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u-1)^3)(u^{42} + 20u^{41} + \dots + 439u + 1)$
$c_2$	$((u-1)^3)(u^{42} - 4u^{41} + \dots + 31u - 1)$
$c_3, c_7$	$u^3(u^{42} - 3u^{41} + \dots + 4u + 8)$
$c_4$	$((u+1)^3)(u^{42} - 4u^{41} + \dots + 31u - 1)$
$c_5, c_6$	$(u^3 - u^2 - 2u + 1)(u^{42} - 2u^{41} + \dots + 9u^2 - 1)$
$c_8, c_9$	$(u^3 - u^2 - 2u + 1)(u^{42} + 2u^{41} + \dots + 4u + 1)$
$c_{10}, c_{11}$	$(u^3 + u^2 - 2u - 1)(u^{42} - 2u^{41} + \dots + 9u^2 - 1)$
$c_{12}$	$(u^3 + u^2 - 2u - 1)(u^{42} + 2u^{41} + \dots + 4u + 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y - 1)^3)(y^{42} + 8y^{41} + \dots - 130935y + 1)$
$c_2, c_4$	$((y - 1)^3)(y^{42} - 20y^{41} + \dots - 439y + 1)$
$c_3, c_7$	$y^3(y^{42} - 21y^{41} + \dots - 4304y + 64)$
$c_5, c_6, c_{10}$ $c_{11}$	$(y^3 - 5y^2 + 6y - 1)(y^{42} - 46y^{41} + \dots - 18y + 1)$
$c_8, c_9, c_{12}$	$(y^3 - 5y^2 + 6y - 1)(y^{42} - 34y^{41} + \dots - 18y + 1)$