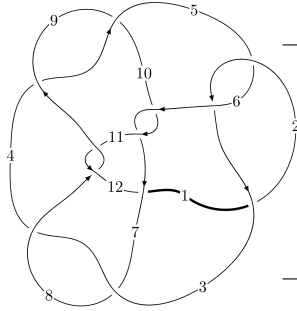
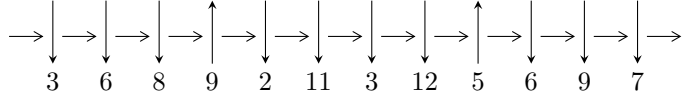


12n<sub>0375</sub> (K12n<sub>0375</sub>)

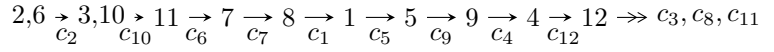


A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 339u^{19} - 3935u^{18} + \dots + 809b + 2456, -1439u^{19} + 6826u^{18} + \dots + 2427a + 13155, u^{20} - 8u^{19} + \dots + 12u - 3 \rangle$$

$$I_2^u = \langle -u^9a - 9u^9 + \dots - a - 15, -5u^9a - u^9 + \dots - 7a - 3, u^{10} + 2u^9 + u^8 - 3u^7 - 2u^6 + 2u^5 + 3u^4 - 2u^3 - u^2 + 2u + 1 \rangle$$

$$I_3^u = \langle 2u^{10} + 9u^9 + 14u^8 + u^7 - 24u^6 - 23u^5 + 11u^4 + 29u^3 + 7u^2 + b - 13u - 5, -3u^{10} - 14u^9 - 22u^8 + 42u^6 + 38u^5 - 22u^4 - 50u^3 - 9u^2 + a + 24u + 7, u^{11} + 5u^{10} + 9u^9 + 3u^8 - 13u^7 - 17u^6 + 2u^5 + 18u^4 + 9u^3 - 6u^2 - 5u - 1 \rangle$$

$$I_4^u = \langle b^2 + b - 1, a + 1, u - 1 \rangle$$

$$I_1^v = \langle a, b + 1, v - 1 \rangle$$

\* 5 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 54 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle 339u^{19} - 3935u^{18} + \dots + 809b + 2456, -1439u^{19} + 6826u^{18} + \dots + 2427a + 13155, u^{20} - 8u^{19} + \dots + 12u - 3 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.592913u^{19} - 2.81253u^{18} + \dots + 12.5904u - 5.42027 \\ -0.419036u^{19} + 4.86403u^{18} + \dots + 14.5278u - 3.03585 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.592913u^{19} - 2.81253u^{18} + \dots + 12.5904u - 5.42027 \\ 1.53276u^{19} - 10.3375u^{18} + \dots - 6.86279u + 2.75649 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -1.20231u^{19} + 7.31685u^{18} + \dots - 4.78451u + 3.02596 \\ -1.03585u^{19} + 7.02967u^{18} + \dots + 3.81211u - 0.846724 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -2.01937u^{19} + 15.3379u^{18} + \dots + 15.4157u - 3.03214 \\ 2.30161u^{19} - 16.5600u^{18} + \dots - 16.4536u + 3.60692 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^2 + 1 \\ -u^4 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -0.918830u^{19} + 5.81788u^{18} + \dots + 10.5979u - 4.16316 \\ -1.93078u^{19} + 13.4944u^{18} + \dots + 12.5352u - 1.77874 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -0.952616u^{19} + 6.38607u^{18} + \dots + 9.11042u - 2.28307 \\ 0.817058u^{19} - 8.02101u^{18} + \dots - 20.2002u + 6.05810 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.753605u^{19} - 5.80758u^{18} + \dots - 4.77421u + 2.27194 \\ -1.60939u^{19} + 12.5043u^{18} + \dots + 19.8059u - 5.39431 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = -\frac{277}{809}u^{19} + \frac{4609}{809}u^{18} + \dots + \frac{33642}{809}u - \frac{32682}{809}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{20} + 8u^{19} + \dots + 150u + 9$
$c_2, c_5$	$u^{20} + 8u^{19} + \dots - 12u - 3$
$c_3, c_7$	$u^{20} - 2u^{19} + \dots + u + 1$
$c_4, c_9$	$u^{20} - 8u^{18} + \dots + 3u + 1$
$c_6, c_{10}$	$u^{20} + 6u^{18} + \dots + 9u + 1$
$c_8, c_{11}$	$u^{20} - 7u^{19} + \dots + 12u - 3$
$c_{12}$	$u^{20} + 21u^{19} + \dots + 6656u + 512$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{20} + 16y^{19} + \dots - 5202y + 81$
$c_2, c_5$	$y^{20} - 8y^{19} + \dots - 150y + 9$
$c_3, c_7$	$y^{20} - 28y^{19} + \dots + 7y + 1$
$c_4, c_9$	$y^{20} - 16y^{19} + \dots + 5y + 1$
$c_6, c_{10}$	$y^{20} + 12y^{19} + \dots - 21y + 1$
$c_8, c_{11}$	$y^{20} + 11y^{19} + \dots - 132y + 9$
$c_{12}$	$y^{20} - 9y^{19} + \dots - 2621440y + 262144$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.739766 + 0.810627I$ $a = -0.332052 - 0.863055I$ $b = -1.178040 - 0.181845I$	$-1.201950 + 0.670281I$	$-8.29063 + 0.06466I$
$u = 0.739766 - 0.810627I$ $a = -0.332052 + 0.863055I$ $b = -1.178040 + 0.181845I$	$-1.201950 - 0.670281I$	$-8.29063 - 0.06466I$
$u = 0.579374 + 0.935372I$ $a = -1.121180 - 0.363583I$ $b = -0.996152 + 0.778841I$	$6.00051 - 2.90762I$	$-6.41870 + 3.35662I$
$u = 0.579374 - 0.935372I$ $a = -1.121180 + 0.363583I$ $b = -0.996152 - 0.778841I$	$6.00051 + 2.90762I$	$-6.41870 - 3.35662I$
$u = 0.725363$ $a = 0.248162$ $b = -0.655437$	$-1.32826$	$-7.40410$
$u = -0.641694 + 0.281021I$ $a = 1.66993 - 0.14677I$ $b = 0.666818 - 0.229080I$	$2.15316 + 3.41819I$	$1.21797 - 1.44999I$
$u = -0.641694 - 0.281021I$ $a = 1.66993 + 0.14677I$ $b = 0.666818 + 0.229080I$	$2.15316 - 3.41819I$	$1.21797 + 1.44999I$
$u = 1.009590 + 0.838851I$ $a = 1.119650 + 0.309640I$ $b = 1.50399 - 1.02071I$	$-1.88231 - 6.91835I$	$-9.67007 + 4.45150I$
$u = 1.009590 - 0.838851I$ $a = 1.119650 - 0.309640I$ $b = 1.50399 + 1.02071I$	$-1.88231 + 6.91835I$	$-9.67007 - 4.45150I$
$u = 0.522186 + 0.274434I$ $a = 0.715817 + 0.493479I$ $b = 0.035362 - 0.930126I$	$-0.818282 - 1.020500I$	$-8.50734 + 6.76581I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.522186 - 0.274434I$		
$a = 0.715817 - 0.493479I$	$-0.818282 + 1.020500I$	$-8.50734 - 6.76581I$
$b = 0.035362 + 0.930126I$		
$u = 0.82856 + 1.18903I$		
$a = 0.665734 + 0.836247I$	$1.33376 + 6.29384I$	$-5.85142 - 3.79279I$
$b = 1.275630 + 0.188413I$		
$u = 0.82856 - 1.18903I$		
$a = 0.665734 - 0.836247I$	$1.33376 - 6.29384I$	$-5.85142 + 3.79279I$
$b = 1.275630 - 0.188413I$		
$u = 1.28182 + 0.74255I$		
$a = 0.465354 + 0.427519I$	$3.78911 - 3.43912I$	$-5.47667 + 2.61689I$
$b = 1.176510 + 0.070724I$		
$u = 1.28182 - 0.74255I$		
$a = 0.465354 - 0.427519I$	$3.78911 + 3.43912I$	$-5.47667 - 2.61689I$
$b = 1.176510 - 0.070724I$		
$u = 1.14224 + 0.95656I$		
$a = -1.149420 - 0.323355I$	$0.28633 - 13.95250I$	$-7.83055 + 7.44247I$
$b = -1.65497 + 0.80309I$		
$u = 1.14224 - 0.95656I$		
$a = -1.149420 + 0.323355I$	$0.28633 + 13.95250I$	$-7.83055 - 7.44247I$
$b = -1.65497 - 0.80309I$		
$u = -1.65206 + 0.05162I$		
$a = -0.199755 - 0.409902I$	$-9.08165 + 2.30266I$	$-5.04461 + 4.85763I$
$b = -0.127470 - 0.253935I$		
$u = -1.65206 - 0.05162I$		
$a = -0.199755 + 0.409902I$	$-9.08165 - 2.30266I$	$-5.04461 - 4.85763I$
$b = -0.127470 + 0.253935I$		
$u = -0.344930$		
$a = -2.91630$	$-1.47402$	$-6.85190$
$b = -0.747935$		

**II.**

$$I_2^u = \langle -u^9 a - 9u^9 + \dots - a - 15, -5u^9 a - u^9 + \dots - 7a - 3, u^{10} + 2u^9 + \dots + 2u + 1 \rangle$$

**(i) Arc colorings**

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a \\ \frac{1}{2}u^9 a + \frac{9}{2}u^9 + \dots + \frac{1}{2}a + \frac{15}{2} \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} a \\ \frac{1}{2}u^9 a + \frac{9}{2}u^9 + \dots + \frac{1}{2}a + \frac{15}{2} \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 3u^9 a + u^9 + \dots + 5a + 1 \\ -\frac{1}{2}u^9 a + \frac{1}{2}u^9 + \dots - \frac{1}{2}a - \frac{1}{2} \end{pmatrix}$$

$$a_8 = \begin{pmatrix} \frac{9}{2}u^9 a + \frac{1}{2}u^9 + \dots + \frac{15}{2}a + \frac{3}{2} \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^2 + 1 \\ -u^4 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -\frac{1}{2}u^9 a - \frac{3}{2}u^9 + \dots + \frac{1}{2}a - \frac{5}{2} \\ 3u^9 + 4u^8 - 9u^6 + u^5 + 7u^4 + 4u^3 + au - 10u^2 + 3u + 5 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 6u^9 a + u^9 + \dots + 10a + 2 \\ \frac{3}{2}u^9 a - \frac{1}{2}u^9 + \dots + \frac{5}{2}a + \frac{1}{2} \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 3u^9 a + u^9 + \dots + 5a + 2 \\ -\frac{1}{2}u^9 a + \frac{1}{2}u^9 + \dots - \frac{1}{2}a - \frac{1}{2} \end{pmatrix}$$

**(ii) Obstruction class = -1**

**(iii) Cusp Shapes =  $-11u^9 - 17u^8 + 37u^6 + 3u^5 - 35u^4 - 20u^3 + 38u^2 - 3u - 35$**

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$(u^{10} + 2u^9 + 9u^8 + 15u^7 + 28u^6 + 36u^5 + 35u^4 + 22u^3 + 15u^2 + 6u + 1)^2$
$c_2, c_5$	$(u^{10} - 2u^9 + u^8 + 3u^7 - 2u^6 - 2u^5 + 3u^4 + 2u^3 - u^2 - 2u + 1)^2$
$c_3, c_7$	$u^{20} + 2u^{19} + \dots - 19u + 61$
$c_4, c_9$	$u^{20} - 6u^{18} + \dots - 15u + 85$
$c_6, c_{10}$	$u^{20} - 3u^{19} + \dots - 108u + 59$
$c_8, c_{11}$	$(u^{10} + 3u^9 + 6u^8 + 7u^7 + 9u^6 + 9u^5 + 10u^4 + 6u^3 + 5u^2 + 3u + 2)^2$
$c_{12}$	$(u - 1)^{20}$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^{10} + 14y^9 + \dots - 6y + 1)^2$
$c_2, c_5$	$(y^{10} - 2y^9 + 9y^8 - 15y^7 + 28y^6 - 36y^5 + 35y^4 - 22y^3 + 15y^2 - 6y + 1)^2$
$c_3, c_7$	$y^{20} - 12y^{19} + \dots - 40987y + 3721$
$c_4, c_9$	$y^{20} - 12y^{19} + \dots - 97975y + 7225$
$c_6, c_{10}$	$y^{20} + 13y^{19} + \dots + 76246y + 3481$
$c_8, c_{11}$	$(y^{10} + 3y^9 + \dots + 11y + 4)^2$
$c_{12}$	$(y - 1)^{20}$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.975430 + 0.320615I$ $a = -1.065150 + 0.247050I$ $b = -1.63832 + 0.24814I$	$-3.87176 + 0.60085I$	$-13.31849 - 3.40041I$
$u = 0.975430 + 0.320615I$ $a = 0.880921 - 0.910530I$ $b = -0.559442 - 0.182706I$	$-3.87176 + 0.60085I$	$-13.31849 - 3.40041I$
$u = 0.975430 - 0.320615I$ $a = -1.065150 - 0.247050I$ $b = -1.63832 - 0.24814I$	$-3.87176 - 0.60085I$	$-13.31849 + 3.40041I$
$u = 0.975430 - 0.320615I$ $a = 0.880921 + 0.910530I$ $b = -0.559442 + 0.182706I$	$-3.87176 - 0.60085I$	$-13.31849 + 3.40041I$
$u = 0.541733 + 0.670646I$ $a = 1.294850 - 0.350726I$ $b = 1.70668 - 0.48449I$	$-2.20007 - 4.58635I$	$-7.79322 + 7.42430I$
$u = 0.541733 + 0.670646I$ $a = -0.49398 + 2.09684I$ $b = 0.312809 + 0.203725I$	$-2.20007 - 4.58635I$	$-7.79322 + 7.42430I$
$u = 0.541733 - 0.670646I$ $a = 1.294850 + 0.350726I$ $b = 1.70668 + 0.48449I$	$-2.20007 + 4.58635I$	$-7.79322 - 7.42430I$
$u = 0.541733 - 0.670646I$ $a = -0.49398 - 2.09684I$ $b = 0.312809 - 0.203725I$	$-2.20007 + 4.58635I$	$-7.79322 - 7.42430I$
$u = -0.876556 + 1.026090I$ $a = -0.533352 + 0.614318I$ $b = -1.129040 - 0.385187I$	$6.17677 + 1.75340I$	$-6.60526 + 0.85033I$
$u = -0.876556 + 1.026090I$ $a = 1.221340 - 0.556605I$ $b = 1.54773 + 0.26490I$	$6.17677 + 1.75340I$	$-6.60526 + 0.85033I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.876556 - 1.026090I$ $a = -0.533352 - 0.614318I$ $b = -1.129040 + 0.385187I$	$6.17677 - 1.75340I$	$-6.60526 - 0.85033I$
$u = -0.876556 - 1.026090I$ $a = 1.221340 + 0.556605I$ $b = 1.54773 - 0.26490I$	$6.17677 - 1.75340I$	$-6.60526 - 0.85033I$
$u = -0.580680 + 0.133301I$ $a = -0.062064 + 0.507460I$ $b = 0.18768 + 2.50740I$	$-4.85763 + 3.93250I$	$-20.2791 - 6.7139I$
$u = -0.580680 + 0.133301I$ $a = -1.04621 + 3.04432I$ $b = -0.411614 - 1.128030I$	$-4.85763 + 3.93250I$	$-20.2791 - 6.7139I$
$u = -0.580680 - 0.133301I$ $a = -0.062064 - 0.507460I$ $b = 0.18768 - 2.50740I$	$-4.85763 - 3.93250I$	$-20.2791 + 6.7139I$
$u = -0.580680 - 0.133301I$ $a = -1.04621 - 3.04432I$ $b = -0.411614 + 1.128030I$	$-4.85763 - 3.93250I$	$-20.2791 + 6.7139I$
$u = -1.059930 + 0.922349I$ $a = 0.797570 - 0.248575I$ $b = 1.51824 + 0.58719I$	$5.57516 + 5.36397I$	$-8.50388 - 6.50559I$
$u = -1.059930 + 0.922349I$ $a = -0.993922 + 0.803452I$ $b = -1.53472 - 0.22114I$	$5.57516 + 5.36397I$	$-8.50388 - 6.50559I$
$u = -1.059930 - 0.922349I$ $a = 0.797570 + 0.248575I$ $b = 1.51824 - 0.58719I$	$5.57516 - 5.36397I$	$-8.50388 + 6.50559I$
$u = -1.059930 - 0.922349I$ $a = -0.993922 - 0.803452I$ $b = -1.53472 + 0.22114I$	$5.57516 - 5.36397I$	$-8.50388 + 6.50559I$

III.

$$I_3^u = \langle 2u^{10} + 9u^9 + \dots + b - 5, -3u^{10} - 14u^9 + \dots + a + 7, u^{11} + 5u^{10} + \dots - 5u - 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_2 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_3 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 3u^{10} + 14u^9 + 22u^8 - 42u^6 - 38u^5 + 22u^4 + 50u^3 + 9u^2 - 24u - 7 \\ -2u^{10} - 9u^9 + \dots + 13u + 5 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 3u^{10} + 14u^9 + 22u^8 - 42u^6 - 38u^5 + 22u^4 + 50u^3 + 9u^2 - 24u - 7 \\ -2u^{10} - 9u^9 + \dots + 11u + 4 \end{pmatrix} \\ a_7 &= \begin{pmatrix} u^{10} + 5u^9 + 9u^8 + 3u^7 - 13u^6 - 17u^5 + 2u^4 + 18u^3 + 9u^2 - 7u - 6 \\ u^{10} + 4u^9 + 5u^8 - 2u^7 - 11u^6 - 6u^5 + 8u^4 + 9u^3 - 2u^2 - 4u \end{pmatrix} \\ a_8 &= \begin{pmatrix} u^9 + 4u^8 + 5u^7 - 2u^6 - 11u^5 - 6u^4 + 8u^3 + 10u^2 - 2u - 6 \\ -u^3 - u^2 + 1 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -u^2 + 1 \\ -u^4 \end{pmatrix} \\ a_5 &= \begin{pmatrix} u \\ u \end{pmatrix} \\ a_9 &= \begin{pmatrix} 4u^{10} + 18u^9 + \dots - 29u - 9 \\ -u^{10} - 5u^9 - 9u^8 - 3u^7 + 13u^6 + 16u^5 - 4u^4 - 18u^3 - 6u^2 + 8u + 3 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -u^{10} - 4u^9 - 4u^8 + 5u^7 + 13u^6 + 2u^5 - 15u^4 - 9u^3 + 8u^2 + 8u - 4 \\ u^{10} + 4u^9 + 5u^8 - 2u^7 - 11u^6 - 6u^5 + 8u^4 + 10u^3 - u^2 - 5u \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -u^{10} - 5u^9 - 9u^8 - 3u^7 + 13u^6 + 17u^5 - 3u^4 - 20u^3 - 10u^2 + 8u + 7 \\ -u^{10} - 4u^9 - 5u^8 + 2u^7 + 10u^6 + 4u^5 - 9u^4 - 8u^3 + 3u^2 + 4u \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes

$$= u^{10} + 6u^9 + 10u^8 - u^7 - 24u^6 - 21u^5 + 17u^4 + 35u^3 + 5u^2 - 26u - 14$$

(iv)  $u$ -Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{11} - 7u^{10} + \dots + 13u - 1$
$c_2$	$u^{11} + 5u^{10} + \dots - 5u - 1$
$c_3$	$u^{11} - u^{10} + \dots + 6u - 1$
$c_4$	$u^{11} + u^{10} - u^9 - 2u^8 - 5u^7 + 4u^6 + 12u^5 - 4u^4 + u^3 + 5u^2 - 1$
$c_5$	$u^{11} - 5u^{10} + \dots - 5u + 1$
$c_6$	$u^{11} + u^{10} + 5u^9 + 5u^8 + 9u^7 + 8u^6 + 6u^5 - u^3 - 6u^2 - 2u - 1$
$c_7$	$u^{11} + u^{10} + \dots + 6u + 1$
$c_8$	$u^{11} - 4u^{10} + \dots + 15u - 5$
$c_9$	$u^{11} - u^{10} - u^9 + 2u^8 - 5u^7 - 4u^6 + 12u^5 + 4u^4 + u^3 - 5u^2 + 1$
$c_{10}$	$u^{11} - u^{10} + 5u^9 - 5u^8 + 9u^7 - 8u^6 + 6u^5 - u^3 + 6u^2 - 2u + 1$
$c_{11}$	$u^{11} + 4u^{10} + \dots + 15u + 5$
$c_{12}$	$u^{11} - 3u^{10} - u^8 + 8u^7 + 8u^6 + 10u^5 - 13u^4 - 17u^3 - 8u^2 + 11u + 5$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{11} + y^{10} + \dots - 11y - 1$
$c_2, c_5$	$y^{11} - 7y^{10} + \dots + 13y - 1$
$c_3, c_7$	$y^{11} - 7y^{10} + \dots + 8y - 1$
$c_4, c_9$	$y^{11} - 3y^{10} + \dots + 10y - 1$
$c_6, c_{10}$	$y^{11} + 9y^{10} + \dots - 8y - 1$
$c_8, c_{11}$	$y^{11} + 8y^{10} + \dots - 65y - 25$
$c_{12}$	$y^{11} - 9y^{10} + \dots + 201y - 25$



(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.888248 + 0.348807I$ $a = 1.094700 + 0.166339I$ $b = 0.518352 + 0.184714I$	$1.62880 - 3.55605I$	$-13.8351 + 4.8849I$
$u = 0.888248 - 0.348807I$ $a = 1.094700 - 0.166339I$ $b = 0.518352 - 0.184714I$	$1.62880 + 3.55605I$	$-13.8351 - 4.8849I$
$u = 0.865988$ $a = -0.906257$ $b = -0.420586$	$-2.51061$	$-16.1470$
$u = -0.794068 + 1.051540I$ $a = -1.013640 + 0.571990I$ $b = -1.35569 - 0.45895I$	$7.94404 + 2.78344I$	$-1.36367 - 2.55365I$
$u = -0.794068 - 1.051540I$ $a = -1.013640 - 0.571990I$ $b = -1.35569 + 0.45895I$	$7.94404 - 2.78344I$	$-1.36367 + 2.55365I$
$u = -1.12350 + 0.92492I$ $a = 0.823218 - 0.546732I$ $b = 1.52074 + 0.25018I$	$6.92380 + 4.41989I$	$-2.52937 - 2.98344I$
$u = -1.12350 - 0.92492I$ $a = 0.823218 + 0.546732I$ $b = 1.52074 - 0.25018I$	$6.92380 - 4.41989I$	$-2.52937 + 2.98344I$
$u = -1.56100 + 0.06449I$ $a = -0.120564 + 0.249710I$ $b = -0.383171 + 0.664642I$	$-9.38029 - 2.74226I$	$-13.9541 + 7.1206I$
$u = -1.56100 - 0.06449I$ $a = -0.120564 - 0.249710I$ $b = -0.383171 - 0.664642I$	$-9.38029 + 2.74226I$	$-13.9541 - 7.1206I$
$u = -0.342676 + 0.154468I$ $a = 1.16941 - 2.73498I$ $b = 0.41006 + 1.60424I$	$-4.21611 + 3.79963I$	$-5.24446 - 3.20279I$

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.342676 - 0.154468I$		
$a = 1.16941 + 2.73498I$	$-4.21611 - 3.79963I$	$-5.24446 + 3.20279I$
$b = 0.41006 - 1.60424I$		

$$\text{IV. } I_4^u = \langle b^2 + b - 1, a + 1, u - 1 \rangle$$

**(i) Arc colorings**

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1 \\ b \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -1 \\ b - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -1 \\ b \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -b - 2 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -b - 2 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -2b - 2 \\ -b \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -1 \\ b - 1 \end{pmatrix}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes = -7**

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_6$	$(u - 1)^2$
$c_3, c_4$	$u^2 - u - 1$
$c_5, c_{10}, c_{12}$	$(u + 1)^2$
$c_7, c_9$	$u^2 + u - 1$
$c_8, c_{11}$	$u^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_5$ $c_6, c_{10}, c_{12}$	$(y - 1)^2$
$c_3, c_4, c_7$ $c_9$	$y^2 - 3y + 1$
$c_8, c_{11}$	$y^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$ $a = -1.00000$ $b = 0.618034$	-3.28987	-7.00000
$u = 1.00000$ $a = -1.00000$ $b = -1.61803$	-3.28987	-7.00000

$$\mathbf{V. } I_1^v = \langle a, b + 1, v - 1 \rangle$$

**(i) Arc colorings**

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

**(ii) Obstruction class = -1**

**(iii) Cusp Shapes = -6**

(iv) **u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_5$ $c_8, c_{11}$	$u$
$c_3, c_4, c_6$ $c_7, c_9, c_{10}$ $c_{12}$	$u + 1$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_5$ $c_8, c_{11}$	$y$
$c_3, c_4, c_6$ $c_7, c_9, c_{10}$ $c_{12}$	$y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = 1.00000$		
$a = 0$	-1.64493	-6.00000
$b = -1.00000$		

## VI. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$u(u-1)^2 \cdot (u^{10} + 2u^9 + 9u^8 + 15u^7 + 28u^6 + 36u^5 + 35u^4 + 22u^3 + 15u^2 + 6u + 1)^2 \cdot (u^{11} - 7u^{10} + \dots + 13u - 1)(u^{20} + 8u^{19} + \dots + 150u + 9)$
$c_2$	$u(u-1)^2 \cdot (u^{10} - 2u^9 + u^8 + 3u^7 - 2u^6 - 2u^5 + 3u^4 + 2u^3 - u^2 - 2u + 1)^2 \cdot (u^{11} + 5u^{10} + \dots - 5u - 1)(u^{20} + 8u^{19} + \dots - 12u - 3)$
$c_3$	$(u+1)(u^2 - u - 1)(u^{11} - u^{10} + \dots + 6u - 1)(u^{20} - 2u^{19} + \dots + u + 1) \cdot (u^{20} + 2u^{19} + \dots - 19u + 61)$
$c_4$	$(u+1)(u^2 - u - 1) \cdot (u^{11} + u^{10} - u^9 - 2u^8 - 5u^7 + 4u^6 + 12u^5 - 4u^4 + u^3 + 5u^2 - 1) \cdot (u^{20} - 8u^{18} + \dots + 3u + 1)(u^{20} - 6u^{18} + \dots - 15u + 85)$
$c_5$	$u(u+1)^2 \cdot (u^{10} - 2u^9 + u^8 + 3u^7 - 2u^6 - 2u^5 + 3u^4 + 2u^3 - u^2 - 2u + 1)^2 \cdot (u^{11} - 5u^{10} + \dots - 5u + 1)(u^{20} + 8u^{19} + \dots - 12u - 3)$
$c_6$	$(u-1)^2(u+1) \cdot (u^{11} + u^{10} + 5u^9 + 5u^8 + 9u^7 + 8u^6 + 6u^5 - u^3 - 6u^2 - 2u - 1) \cdot (u^{20} + 6u^{18} + \dots + 9u + 1)(u^{20} - 3u^{19} + \dots - 108u + 59)$
$c_7$	$(u+1)(u^2 + u - 1)(u^{11} + u^{10} + \dots + 6u + 1)(u^{20} - 2u^{19} + \dots + u + 1) \cdot (u^{20} + 2u^{19} + \dots - 19u + 61)$
$c_8$	$u^3(u^{10} + 3u^9 + 6u^8 + 7u^7 + 9u^6 + 9u^5 + 10u^4 + 6u^3 + 5u^2 + 3u + 2)^2 \cdot (u^{11} - 4u^{10} + \dots + 15u - 5)(u^{20} - 7u^{19} + \dots + 12u - 3)$
$c_9$	$(u+1)(u^2 + u - 1) \cdot (u^{11} - u^{10} - u^9 + 2u^8 - 5u^7 - 4u^6 + 12u^5 + 4u^4 + u^3 - 5u^2 + 1) \cdot (u^{20} - 8u^{18} + \dots + 3u + 1)(u^{20} - 6u^{18} + \dots - 15u + 85)$
$c_{10}$	$((u+1)^3)(u^{11} - u^{10} + \dots - 2u + 1) \cdot (u^{20} + 6u^{18} + \dots + 9u + 1)(u^{20} - 3u^{19} + \dots - 108u + 59)$
$c_{11}$	$u^3(u^{10} + 3u^9 + 6u^8 + 7u^7 + 9u^6 + 9u^5 + 10u^4 + 6u^3 + 5u^2 + 3u + 2)^2 \cdot (u^{11} + 4u^{10} + \dots + \frac{15u}{27} + 5)(u^{20} - 7u^{19} + \dots + 12u - 3)$
$c_{12}$	$(u-1)^{20}(u+1)^3 \cdot (u^{11} - 3u^{10} - u^8 + 8u^7 + 8u^6 + 10u^5 - 13u^4 - 17u^3 - 8u^2 + 11u + 5) \cdot (u^{20} + 21u^{19} + \dots + 6656u + 512)$

## VII. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$y(y-1)^2(y^{10} + 14y^9 + \dots - 6y + 1)^2(y^{11} + y^{10} + \dots - 11y - 1)$ $\cdot (y^{20} + 16y^{19} + \dots - 5202y + 81)$
$c_2, c_5$	$y(y-1)^2$ $\cdot (y^{10} - 2y^9 + 9y^8 - 15y^7 + 28y^6 - 36y^5 + 35y^4 - 22y^3 + 15y^2 - 6y + 1)^2$ $\cdot (y^{11} - 7y^{10} + \dots + 13y - 1)(y^{20} - 8y^{19} + \dots - 150y + 9)$
$c_3, c_7$	$(y-1)(y^2 - 3y + 1)(y^{11} - 7y^{10} + \dots + 8y - 1)(y^{20} - 28y^{19} + \dots + 7y + 1)$ $\cdot (y^{20} - 12y^{19} + \dots - 40987y + 3721)$
$c_4, c_9$	$(y-1)(y^2 - 3y + 1)(y^{11} - 3y^{10} + \dots + 10y - 1)$ $\cdot (y^{20} - 16y^{19} + \dots + 5y + 1)(y^{20} - 12y^{19} + \dots - 97975y + 7225)$
$c_6, c_{10}$	$((y-1)^3)(y^{11} + 9y^{10} + \dots - 8y - 1)(y^{20} + 12y^{19} + \dots - 21y + 1)$ $\cdot (y^{20} + 13y^{19} + \dots + 76246y + 3481)$
$c_8, c_{11}$	$y^3(y^{10} + 3y^9 + \dots + 11y + 4)^2(y^{11} + 8y^{10} + \dots - 65y - 25)$ $\cdot (y^{20} + 11y^{19} + \dots - 132y + 9)$
$c_{12}$	$((y-1)^{23})(y^{11} - 9y^{10} + \dots + 201y - 25)$ $\cdot (y^{20} - 9y^{19} + \dots - 2621440y + 262144)$