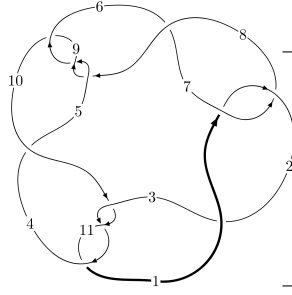
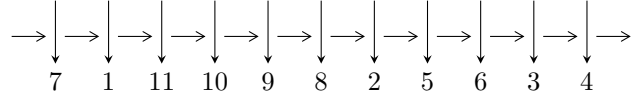


11a<sub>245</sub> (K11a<sub>245</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$3, 10 \xrightarrow{c_{10}} 11 \xrightarrow{c_3} 4 \xrightarrow{c_4} 5 \xrightarrow{c_{11}} 1 \xrightarrow{c_2} 2, 6 \xrightarrow{c_9} 9 \xrightarrow{c_8} 8 \xrightarrow{c_7} 7 \twoheadrightarrow c_1, c_5, c_6$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle b - u, -u^{12} + u^{11} + 5u^{10} - 4u^9 - 9u^8 + 4u^7 + 4u^6 + 4u^5 + 6u^4 - 7u^3 - 5u^2 + a - u - 1, \\ u^{14} - u^{13} - 6u^{12} + 5u^{11} + 14u^{10} - 8u^9 - 13u^8 - 2u^6 + 11u^5 + 11u^4 - 5u^3 - 4u^2 - 4u - 1 \rangle$$

$$I_2^u = \langle -u^{23} + 8u^{21} + \dots + b + 1, u^{22} - 7u^{20} + \dots + a - 1, u^{24} - u^{23} + \dots + 4u^2 + 1 \rangle$$

$$I_3^u = \langle b + 1, a, u - 1 \rangle$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 39 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle b - u, -u^{12} + u^{11} + \dots + a - 1, u^{14} - u^{13} + \dots - 4u - 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^3 - 2u \\ -u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^5 - 2u^3 + u \\ u^7 - 3u^5 + 2u^3 + u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^{12} - u^{11} + \dots + u + 1 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^{13} + u^{12} + \dots - u + 1 \\ -u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^{13} + u^{12} + \dots - u + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^{12} - u^{11} - 5u^{10} + 4u^9 + 9u^8 - 5u^7 - 4u^6 - 6u^4 + 3u^3 + 5u^2 + 1 \\ u^7 - 3u^5 + 2u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^{12} - u^{11} - 5u^{10} + 4u^9 + 9u^8 - 5u^7 - 4u^6 - 6u^4 + 3u^3 + 5u^2 + 1 \\ u^7 - 3u^5 + 2u^3 + u \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= -2u^{12} - 2u^{11} + 14u^{10} + 12u^9 - 34u^8 - 28u^7 + 24u^6 + 24u^5 + 28u^4 + 10u^3 - 38u^2 - 24u - 20$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_7$	$u^{14} + 3u^{13} + \dots + 4u + 2$
$c_2, c_4, c_6$	$u^{14} + 3u^{13} + \dots + 20u + 4$
$c_3, c_5, c_8$ $c_9, c_{10}, c_{11}$	$u^{14} - u^{13} + \dots - 4u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_7$	$y^{14} - 3y^{13} + \dots - 20y + 4$
$c_2, c_4, c_6$	$y^{14} + 13y^{13} + \dots - 168y + 16$
$c_3, c_5, c_8$ $c_9, c_{10}, c_{11}$	$y^{14} - 13y^{13} + \dots - 8y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.029285 + 0.881113I$ $a = 0.03342 - 1.87376I$ $b = -0.029285 + 0.881113I$	$8.40861 + 3.17852I$	$-5.65702 - 2.68027I$
$u = -0.029285 - 0.881113I$ $a = 0.03342 + 1.87376I$ $b = -0.029285 - 0.881113I$	$8.40861 - 3.17852I$	$-5.65702 + 2.68027I$
$u = -1.276220 + 0.129179I$ $a = -2.13229 - 1.54329I$ $b = -1.276220 + 0.129179I$	$-5.86531 + 2.46178I$	$-16.4162 - 2.9434I$
$u = -1.276220 - 0.129179I$ $a = -2.13229 + 1.54329I$ $b = -1.276220 - 0.129179I$	$-5.86531 - 2.46178I$	$-16.4162 + 2.9434I$
$u = -1.284590 + 0.394747I$ $a = -0.34217 - 2.13508I$ $b = -1.284590 + 0.394747I$	$0.58736 + 5.97274I$	$-12.69846 - 3.76747I$
$u = -1.284590 - 0.394747I$ $a = -0.34217 + 2.13508I$ $b = -1.284590 - 0.394747I$	$0.58736 - 5.97274I$	$-12.69846 + 3.76747I$
$u = 1.364060 + 0.212940I$ $a = 1.10215 - 1.44780I$ $b = 1.364060 + 0.212940I$	$-8.69313 - 7.21786I$	$-18.5779 + 6.6599I$
$u = 1.364060 - 0.212940I$ $a = 1.10215 + 1.44780I$ $b = 1.364060 - 0.212940I$	$-8.69313 + 7.21786I$	$-18.5779 - 6.6599I$
$u = 1.38564$ $a = 1.62659$ $b = 1.38564$	$-11.4128$	$-21.8330$
$u = 1.329060 + 0.410124I$ $a = 0.27755 - 1.96683I$ $b = 1.329060 + 0.410124I$	$-0.11168 - 12.47310I$	$-13.5601 + 7.9056I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.329060 - 0.410124I$ $a = 0.27755 + 1.96683I$ $b = 1.329060 - 0.410124I$	$-0.11168 + 12.47310I$	$-13.5601 - 7.9056I$
$u = -0.150725 + 0.518889I$ $a = 0.285959 - 1.368390I$ $b = -0.150725 + 0.518889I$	$1.00801 + 1.75508I$	$-6.01712 - 6.20279I$
$u = -0.150725 - 0.518889I$ $a = 0.285959 + 1.368390I$ $b = -0.150725 - 0.518889I$	$1.00801 - 1.75508I$	$-6.01712 + 6.20279I$
$u = -0.290248$ $a = 0.924145$ $b = -0.290248$	$-0.639037$	$-16.3130$

**II.**

$$I_2^u = \langle -u^{23} + 8u^{21} + \dots + b + 1, u^{22} - 7u^{20} + \dots + a - 1, u^{24} - u^{23} + \dots + 4u^2 + 1 \rangle$$

**(i) Arc colorings**

$$a_3 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^3 - 2u \\ -u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^5 - 2u^3 + u \\ u^7 - 3u^5 + 2u^3 + u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^{22} + 7u^{20} + \dots + 5u + 1 \\ u^{23} - 8u^{21} + \dots - u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^{21} + 8u^{19} + \dots + 5u + 2 \\ u^{23} - 7u^{21} + \dots - u - 2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^{19} - 6u^{17} + \dots + 4u + 1 \\ 2u^{23} - 15u^{21} + \dots - u - 2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^{16} + 5u^{14} + \dots + 4u + 1 \\ 2u^{23} - 16u^{21} + \dots - u - 2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^{16} + 5u^{14} + \dots + 4u + 1 \\ 2u^{23} - 16u^{21} + \dots - u - 2 \end{pmatrix}$$

**(ii) Obstruction class = -1**

**(iii) Cusp Shapes** =  $-4u^{20} + 28u^{18} + 4u^{17} - 80u^{16} - 24u^{15} + 100u^{14} + 56u^{13} - 4u^{12} - 48u^{11} - 124u^{10} - 24u^9 + 92u^8 + 64u^7 + 36u^6 - 12u^5 - 44u^4 - 24u^3 - 8u^2 - 10$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_7$	$(u^{12} - u^{11} - u^{10} + 2u^9 + 3u^8 - 4u^7 - 2u^6 + 4u^5 + 2u^4 - 3u^3 - u^2 + 1)^2$
$c_2, c_4, c_6$	$(u^{12} + 3u^{11} + \dots + 2u + 1)^2$
$c_3, c_5, c_8$ $c_9, c_{10}, c_{11}$	$u^{24} - u^{23} + \dots + 4u^2 + 1$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_7$	$(y^{12} - 3y^{11} + \dots - 2y + 1)^2$
$c_2, c_4, c_6$	$(y^{12} + 13y^{11} + \dots + 6y + 1)^2$
$c_3, c_5, c_8$ $c_9, c_{10}, c_{11}$	$y^{24} - 17y^{23} + \dots + 8y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.070751 + 0.894321I$ $a = -1.21139 + 1.52083I$ $b = 1.299300 - 0.409615I$	$4.26829 + 7.80134I$	$-9.63389 - 5.63981I$
$u = -0.070751 - 0.894321I$ $a = -1.21139 - 1.52083I$ $b = 1.299300 + 0.409615I$	$4.26829 - 7.80134I$	$-9.63389 + 5.63981I$
$u = -1.110590 + 0.134720I$ $a = 0.738153 + 0.451331I$ $b = 0.149210 - 0.343690I$	$-1.55013 + 0.71593I$	$-8.04353 - 0.64874I$
$u = -1.110590 - 0.134720I$ $a = 0.738153 - 0.451331I$ $b = 0.149210 + 0.343690I$	$-1.55013 - 0.71593I$	$-8.04353 + 0.64874I$
$u = -0.778878 + 0.387180I$ $a = -0.213014 + 0.440226I$ $b = 1.242510 + 0.071539I$	$-4.72717 - 0.35310I$	$-18.6669 + 0.6298I$
$u = -0.778878 - 0.387180I$ $a = -0.213014 - 0.440226I$ $b = 1.242510 - 0.071539I$	$-4.72717 + 0.35310I$	$-18.6669 - 0.6298I$
$u = 0.013292 + 0.856991I$ $a = 1.23384 + 1.58823I$ $b = -1.251930 - 0.421635I$	$4.62532 - 1.48234I$	$-8.84742 + 0.67542I$
$u = 0.013292 - 0.856991I$ $a = 1.23384 - 1.58823I$ $b = -1.251930 + 0.421635I$	$4.62532 + 1.48234I$	$-8.84742 - 0.67542I$
$u = 1.242510 + 0.071539I$ $a = -0.023283 - 0.340995I$ $b = -0.778878 + 0.387180I$	$-4.72717 - 0.35310I$	$-18.6669 + 0.6298I$
$u = 1.242510 - 0.071539I$ $a = -0.023283 + 0.340995I$ $b = -0.778878 - 0.387180I$	$-4.72717 + 0.35310I$	$-18.6669 - 0.6298I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.321894 + 0.643464I$	$-3.36661 + 4.24921I$	$-14.1765 - 6.9831I$
$a = -0.65810 + 1.42592I$		
$b = 1.279920 - 0.182904I$		
$u = -0.321894 - 0.643464I$	$-3.36661 - 4.24921I$	$-14.1765 + 6.9831I$
$a = -0.65810 - 1.42592I$		
$b = 1.279920 + 0.182904I$		
$u = 1.279920 + 0.182904I$	$-3.36661 - 4.24921I$	$-14.1765 + 6.9831I$
$a = -0.443771 + 0.752880I$		
$b = -0.321894 - 0.643464I$		
$u = 1.279920 - 0.182904I$	$-3.36661 + 4.24921I$	$-14.1765 - 6.9831I$
$a = -0.443771 - 0.752880I$		
$b = -0.321894 + 0.643464I$		
$u = -1.213270 + 0.447486I$	$0.75031 - 3.01307I$	$-12.63175 + 2.63251I$
$a = -0.537563 - 0.128960I$		
$b = 1.263090 + 0.396551I$		
$u = -1.213270 - 0.447486I$	$0.75031 + 3.01307I$	$-12.63175 - 2.63251I$
$a = -0.537563 + 0.128960I$		
$b = 1.263090 - 0.396551I$		
$u = -1.251930 + 0.421635I$	$4.62532 + 1.48234I$	$-8.84742 - 0.67542I$
$a = 0.704102 + 1.098600I$		
$b = 0.013292 - 0.856991I$		
$u = -1.251930 - 0.421635I$	$4.62532 - 1.48234I$	$-8.84742 + 0.67542I$
$a = 0.704102 - 1.098600I$		
$b = 0.013292 + 0.856991I$		
$u = 1.263090 + 0.396551I$	$0.75031 - 3.01307I$	$-12.63175 + 2.63251I$
$a = 0.492596 - 0.221226I$		
$b = -1.213270 + 0.447486I$		
$u = 1.263090 - 0.396551I$	$0.75031 + 3.01307I$	$-12.63175 - 2.63251I$
$a = 0.492596 + 0.221226I$		
$b = -1.213270 - 0.447486I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.299300 + 0.409615I$	$4.26829 - 7.80134I$	$-9.63389 + 5.63981I$
$a = -0.629315 + 1.115020I$		
$b = -0.070751 - 0.894321I$		
$u = 1.299300 - 0.409615I$	$4.26829 + 7.80134I$	$-9.63389 - 5.63981I$
$a = -0.629315 - 1.115020I$		
$b = -0.070751 + 0.894321I$		
$u = 0.149210 + 0.343690I$	$-1.55013 - 0.71593I$	$-8.04353 + 0.64874I$
$a = 0.04774 + 2.58289I$		
$b = -1.110590 - 0.134720I$		
$u = 0.149210 - 0.343690I$	$-1.55013 + 0.71593I$	$-8.04353 - 0.64874I$
$a = 0.04774 - 2.58289I$		
$b = -1.110590 + 0.134720I$		

$$\text{III. } I_3^u = \langle b + 1, a, u - 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = -12

(iv) **u**-Polynomials at the component

Crossings	<b>u</b> -Polynomials at each crossing
$c_1, c_2, c_4$ $c_6, c_7$	$u$
$c_3, c_8, c_9$	$u + 1$
$c_5, c_{10}, c_{11}$	$u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$ $c_6, c_7$	$y$
$c_3, c_5, c_8$ $c_9, c_{10}, c_{11}$	$y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$		
$a = 0$	-3.28987	-12.0000
$b = -1.00000$		



#### IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_7$	$u(u^{12} - u^{11} - u^{10} + 2u^9 + 3u^8 - 4u^7 - 2u^6 + 4u^5 + 2u^4 - 3u^3 - u^2 + 1)^2 \cdot (u^{14} + 3u^{13} + \dots + 4u + 2)$
$c_2, c_4, c_6$	$u(u^{12} + 3u^{11} + \dots + 2u + 1)^2(u^{14} + 3u^{13} + \dots + 20u + 4)$
$c_3, c_8, c_9$	$(u + 1)(u^{14} - u^{13} + \dots - 4u - 1)(u^{24} - u^{23} + \dots + 4u^2 + 1)$
$c_5, c_{10}, c_{11}$	$(u - 1)(u^{14} - u^{13} + \dots - 4u - 1)(u^{24} - u^{23} + \dots + 4u^2 + 1)$

### V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_7$	$y(y^{12} - 3y^{11} + \dots - 2y + 1)^2(y^{14} - 3y^{13} + \dots - 20y + 4)$
$c_2, c_4, c_6$	$y(y^{12} + 13y^{11} + \dots + 6y + 1)^2(y^{14} + 13y^{13} + \dots - 168y + 16)$
$c_3, c_5, c_8$ $c_9, c_{10}, c_{11}$	$(y - 1)(y^{14} - 13y^{13} + \dots - 8y + 1)(y^{24} - 17y^{23} + \dots + 8y + 1)$