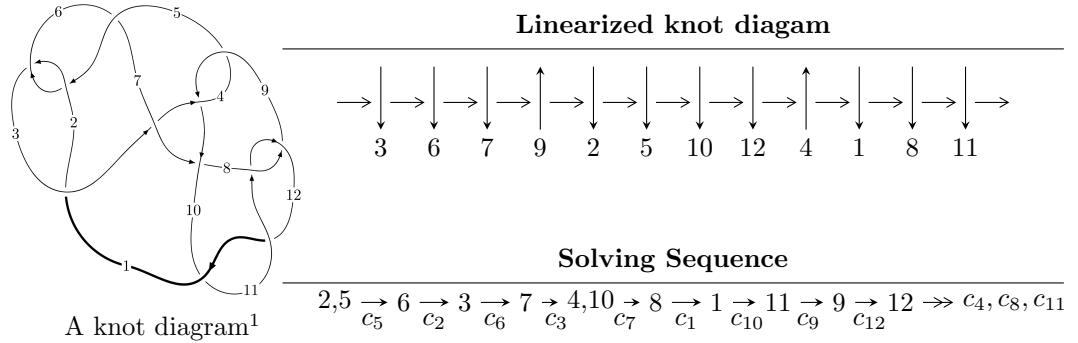


## $12a_{0210}$ ( $K12a_{0210}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$\begin{aligned}
 I_1^u &= \langle -u^{17} + 3u^{15} + u^{14} - 7u^{13} - 2u^{12} + 9u^{11} + 5u^{10} - 10u^9 - 5u^8 + 7u^7 + 6u^6 - 5u^5 - 3u^4 + u^3 + 2u^2 + b, \\
 &\quad -u^{15} + 2u^{13} + u^{12} - 4u^{11} - u^{10} + 3u^9 + 3u^8 - 3u^7 - u^6 + u^5 + 2u^4 - u^3 + a - u, u^{18} - 3u^{16} + \dots + 2u + \\
 I_2^u &= \langle 3u^{83} + 6u^{82} + \dots + b - 1, 7u^{83} + 10u^{82} + \dots + 2a - 11, u^{84} + 3u^{83} + \dots + 2u - 1 \rangle \\
 I_3^u &= \langle b, a + 1, u^3 - u^2 + 1 \rangle \\
 I_4^u &= \langle b, a^2 - au + 2u^2 - 3u + 2, u^3 - u^2 + 1 \rangle \\
 I_5^u &= \langle b - 2, a - 1, u + 1 \rangle
 \end{aligned}$$

\* 5 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 112 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -u^{17} + 3u^{15} + \dots + 2u^2 + b, -u^{15} + 2u^{13} + \dots + a - u, u^{18} - 3u^{16} + \dots + 2u + 1 \rangle$$

(i) **Arc colorings**

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^7 - 2u^5 + 2u^3 - 2u \\ -u^7 + u^5 - 2u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^{15} - 2u^{13} - u^{12} + 4u^{11} + u^{10} - 3u^9 - 3u^8 + 3u^7 + u^6 - u^5 - 2u^4 + u^3 + u \\ u^{17} - 3u^{15} + \dots - u^3 - 2u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^{16} + 3u^{14} + \dots - u^2 + 1 \\ u^{16} - 2u^{14} + \dots - u^4 + 2u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^3 \\ u^5 - u^3 + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^{15} - 2u^{13} - u^{12} + 4u^{11} + u^{10} - 3u^9 - 3u^8 + 3u^7 + u^6 - 2u^4 + u^3 + u \\ u^{17} - 3u^{15} + \dots + 3u^4 - 2u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^{14} - 3u^{12} + \dots + 2u^2 + 2u \\ -u^{14} + 2u^{12} + u^{11} - 5u^{10} - u^9 + 5u^8 + 3u^7 - 6u^6 - u^5 + 3u^4 + 2u^3 - 2u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^{17} - 2u^{15} - u^{14} + 4u^{13} + u^{12} - 3u^{11} - 3u^{10} + 3u^9 + u^8 - 2u^6 + u^5 + 2u^3 \\ -u^{15} + 3u^{13} + \dots - 2u^3 - 2u^2 \end{pmatrix}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $-2u^{17} + 4u^{16} + 8u^{15} - 10u^{14} - 24u^{13} + 26u^{12} + 42u^{11} - 30u^{10} - 66u^9 + 34u^8 + 66u^7 - 16u^6 - 66u^5 + 8u^4 + 32u^3 + 8u^2 - 16u - 14$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_6, c_{10}$ $c_{12}$	$u^{18} + 6u^{17} + \cdots + 2u + 1$
$c_2, c_5, c_8$ $c_{11}$	$u^{18} - 3u^{16} + \cdots + 2u + 1$
$c_3, c_7$	$u^{18} - 2u^{17} + \cdots + 4u + 1$
$c_4, c_9$	$u^{18} - 6u^{17} + \cdots - 24u + 8$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_6, c_{10}$ $c_{12}$	$y^{18} + 14y^{17} + \cdots + 22y + 1$
$c_2, c_5, c_8$ $c_{11}$	$y^{18} - 6y^{17} + \cdots - 2y + 1$
$c_3, c_7$	$y^{18} - 10y^{17} + \cdots - 2y + 1$
$c_4, c_9$	$y^{18} + 8y^{17} + \cdots + 256y + 64$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.852988 + 0.599070I$		
$a = 1.86967 + 1.04403I$	$2.34312 - 4.73471I$	$-7.07668 + 6.82584I$
$b = -1.54451 + 0.51046I$		
$u = 0.852988 - 0.599070I$		
$a = 1.86967 - 1.04403I$	$2.34312 + 4.73471I$	$-7.07668 - 6.82584I$
$b = -1.54451 - 0.51046I$		
$u = 0.713575 + 0.772455I$		
$a = -1.68389 + 1.91803I$	$5.76795 - 0.42490I$	$-2.62552 + 1.94246I$
$b = 0.92095 - 1.86302I$		
$u = 0.713575 - 0.772455I$		
$a = -1.68389 - 1.91803I$	$5.76795 + 0.42490I$	$-2.62552 - 1.94246I$
$b = 0.92095 + 1.86302I$		
$u = -0.680242 + 0.830816I$		
$a = 1.80309 + 1.05417I$	$3.89996 - 5.56871I$	$-4.31829 + 2.06139I$
$b = -1.63673 - 1.25883I$		
$u = -0.680242 - 0.830816I$		
$a = 1.80309 - 1.05417I$	$3.89996 + 5.56871I$	$-4.31829 - 2.06139I$
$b = -1.63673 + 1.25883I$		
$u = 1.088500 + 0.110069I$		
$a = -0.751912 + 0.070278I$	$-9.12746 - 5.02050I$	$-18.4222 + 4.8342I$
$b = -1.65982 + 0.10721I$		
$u = 1.088500 - 0.110069I$		
$a = -0.751912 - 0.070278I$	$-9.12746 + 5.02050I$	$-18.4222 - 4.8342I$
$b = -1.65982 - 0.10721I$		
$u = -1.012600 + 0.591290I$		
$a = -0.91949 - 1.13440I$	$-3.35551 + 7.83027I$	$-12.5543 - 7.9398I$
$b = 0.066057 + 0.911088I$		
$u = -1.012600 - 0.591290I$		
$a = -0.91949 + 1.13440I$	$-3.35551 - 7.83027I$	$-12.5543 + 7.9398I$
$b = 0.066057 - 0.911088I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.997184 + 0.703282I$		
$a = 1.01150 - 3.14671I$	$4.02002 - 10.78450I$	$-6.41328 + 8.53348I$
$b = 1.47517 + 2.11590I$		
$u = 0.997184 - 0.703282I$		
$a = 1.01150 + 3.14671I$	$4.02002 + 10.78450I$	$-6.41328 - 8.53348I$
$b = 1.47517 - 2.11590I$		
$u = -0.623040 + 0.431726I$		
$a = -0.237344 + 0.890114I$	$-0.68211 + 1.26711I$	$-9.25343 - 4.35410I$
$b = 0.157083 + 0.325898I$		
$u = -0.623040 - 0.431726I$		
$a = -0.237344 - 0.890114I$	$-0.68211 - 1.26711I$	$-9.25343 + 4.35410I$
$b = 0.157083 - 0.325898I$		
$u = -1.029700 + 0.727727I$		
$a = -0.09346 - 2.99952I$	$1.7668 + 17.2595I$	$-7.77898 - 11.27344I$
$b = -2.04495 + 1.32035I$		
$u = -1.029700 - 0.727727I$		
$a = -0.09346 + 2.99952I$	$1.7668 - 17.2595I$	$-7.77898 + 11.27344I$
$b = -2.04495 - 1.32035I$		
$u = -0.306671 + 0.477938I$		
$a = 0.001829 + 0.467096I$	$-0.520477 + 1.222060I$	$-5.55737 - 4.78188I$
$b = -0.233244 + 0.353264I$		
$u = -0.306671 - 0.477938I$		
$a = 0.001829 - 0.467096I$	$-0.520477 - 1.222060I$	$-5.55737 + 4.78188I$
$b = -0.233244 - 0.353264I$		

$$\text{II. } I_2^u = \langle 3u^{83} + 6u^{82} + \dots + b - 1, \ 7u^{83} + 10u^{82} + \dots + 2a - 11, \ u^{84} + 3u^{83} + \dots + 2u - 1 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_2 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_5 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix} \\ a_7 &= \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix} \\ a_4 &= \begin{pmatrix} u^7 - 2u^5 + 2u^3 - 2u \\ -u^7 + u^5 - 2u^3 + u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -\frac{7}{2}u^{83} - 5u^{82} + \dots - 3u + \frac{11}{2} \\ -3u^{83} - 6u^{82} + \dots - 3u + 1 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -\frac{1}{2}u^{83} - \frac{3}{2}u^{82} + \dots - \frac{15}{2}u^2 - \frac{9}{2}u \\ u^{19} - 3u^{17} + \dots + 4u^2 + u \end{pmatrix} \\ a_1 &= \begin{pmatrix} u^3 \\ u^5 - u^3 + u \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -12.5000u^{83} - 28.5000u^{82} + \dots - 28.5000u + 15.5000 \\ 8u^{83} + 16u^{82} + \dots + 9u - \frac{9}{2} \end{pmatrix} \\ a_9 &= \begin{pmatrix} -\frac{21}{2}u^{83} - 23u^{82} + \dots - 21u + \frac{25}{2} \\ 5u^{83} + 10u^{82} + \dots + 5u - 3 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} u^{83} + 3u^{82} + \dots + 6u + \frac{1}{2} \\ -\frac{1}{2}u^{83} - u^{82} + \dots - u + \frac{1}{2} \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** =  $-\frac{33}{2}u^{82} - \frac{35}{2}u^{81} + \dots - \frac{97}{2}u + \frac{21}{2}$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_6, c_{10}$ $c_{12}$	$u^{84} + 27u^{83} + \cdots + 20u + 1$
$c_2, c_5, c_8$ $c_{11}$	$u^{84} + 3u^{83} + \cdots + 2u - 1$
$c_3, c_7$	$u^{84} - 3u^{83} + \cdots + 76888u - 5953$
$c_4, c_9$	$(u^{42} + 3u^{41} + \cdots - 36u - 8)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_6, c_{10}$ $c_{12}$	$y^{84} + 61y^{83} + \cdots - 492y + 1$
$c_2, c_5, c_8$ $c_{11}$	$y^{84} - 27y^{83} + \cdots - 20y + 1$
$c_3, c_7$	$y^{84} + y^{83} + \cdots - 880217508y + 35438209$
$c_4, c_9$	$(y^{42} + 21y^{41} + \cdots + 304y + 64)^2$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.712297 + 0.693306I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 2.23429 - 0.72427I$	$-0.0807684 + 0.0270051I$	0
$b = -1.31799 + 1.19951I$		
$u = 0.712297 - 0.693306I$		
$a = 2.23429 + 0.72427I$	$-0.0807684 - 0.0270051I$	0
$b = -1.31799 - 1.19951I$		
$u = -0.981209 + 0.106389I$		
$a = -1.063230 + 0.239722I$	$-0.0807684 + 0.0270051I$	0
$b = -1.31799 + 1.19951I$		
$u = -0.981209 - 0.106389I$		
$a = -1.063230 - 0.239722I$	$-0.0807684 - 0.0270051I$	0
$b = -1.31799 - 1.19951I$		
$u = -1.013640 + 0.084832I$		
$a = 1.108450 - 0.126642I$	$-0.87551 + 5.31550I$	0
$b = 1.84271 - 1.22555I$		
$u = -1.013640 - 0.084832I$		
$a = 1.108450 + 0.126642I$	$-0.87551 - 5.31550I$	0
$b = 1.84271 + 1.22555I$		
$u = -0.672327 + 0.781209I$		
$a = 1.046300 + 0.176265I$	$1.33500 - 3.00337I$	0
$b = -1.139890 - 0.738004I$		
$u = -0.672327 - 0.781209I$		
$a = 1.046300 - 0.176265I$	$1.33500 + 3.00337I$	0
$b = -1.139890 + 0.738004I$		
$u = -0.622637 + 0.740255I$		
$a = -0.917148 + 0.701158I$	$-0.916866 + 0.809895I$	0
$b = 0.958255 + 0.174252I$		
$u = -0.622637 - 0.740255I$		
$a = -0.917148 - 0.701158I$	$-0.916866 - 0.809895I$	0
$b = 0.958255 - 0.174252I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.693162 + 0.769076I$		
$a = 2.10791 - 2.00976I$	$4.93754 + 5.19661I$	0
$b = -1.18015 + 1.94588I$		
$u = 0.693162 - 0.769076I$		
$a = 2.10791 + 2.00976I$	$4.93754 - 5.19661I$	0
$b = -1.18015 - 1.94588I$		
$u = -0.648818 + 0.814325I$		
$a = -1.87305 - 0.13963I$	$-2.74884 - 5.46887I$	0
$b = 1.66800 + 0.67324I$		
$u = -0.648818 - 0.814325I$		
$a = -1.87305 + 0.13963I$	$-2.74884 + 5.46887I$	0
$b = 1.66800 - 0.67324I$		
$u = 1.048020 + 0.087930I$		
$a = 0.740915 + 0.375139I$	$-4.65419 - 2.84221I$	0
$b = 0.938320 - 0.000865I$		
$u = 1.048020 - 0.087930I$		
$a = 0.740915 - 0.375139I$	$-4.65419 + 2.84221I$	0
$b = 0.938320 + 0.000865I$		
$u = -0.761114 + 0.735215I$		
$a = 0.528661 + 0.102908I$	$6.06758 + 3.93578I$	0
$b = 0.294442 + 0.779185I$		
$u = -0.761114 - 0.735215I$		
$a = 0.528661 - 0.102908I$	$6.06758 - 3.93578I$	0
$b = 0.294442 - 0.779185I$		
$u = -0.749660 + 0.749510I$		
$a = -0.377620 + 0.179779I$	$6.42114 - 2.03089I$	0
$b = -0.382925 - 0.879824I$		
$u = -0.749660 - 0.749510I$		
$a = -0.377620 - 0.179779I$	$6.42114 + 2.03089I$	0
$b = -0.382925 + 0.879824I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.958216 + 0.461454I$		
$a = -0.29023 + 1.63234I$	$-0.916866 + 0.809895I$	0
$b = 0.958255 + 0.174252I$		
$u = -0.958216 - 0.461454I$		
$a = -0.29023 - 1.63234I$	$-0.916866 - 0.809895I$	0
$b = 0.958255 - 0.174252I$		
$u = -0.674263 + 0.839731I$		
$a = -2.12227 - 1.06881I$	$2.85235 - 11.39960I$	0
$b = 1.83778 + 1.26952I$		
$u = -0.674263 - 0.839731I$		
$a = -2.12227 + 1.06881I$	$2.85235 + 11.39960I$	0
$b = 1.83778 - 1.26952I$		
$u = 1.078220 + 0.052470I$		
$a = -0.355684 - 0.249586I$	$-6.62757 + 1.48268I$	0
$b = -0.803714 + 0.656750I$		
$u = 1.078220 - 0.052470I$		
$a = -0.355684 + 0.249586I$	$-6.62757 - 1.48268I$	0
$b = -0.803714 - 0.656750I$		
$u = 0.791471 + 0.735596I$		
$a = -0.975220 + 0.562204I$	$3.25378 - 1.67585I$	0
$b = 0.633168 - 0.948263I$		
$u = 0.791471 - 0.735596I$		
$a = -0.975220 - 0.562204I$	$3.25378 + 1.67585I$	0
$b = 0.633168 + 0.948263I$		
$u = 1.071840 + 0.149484I$		
$a = 1.208950 - 0.123740I$	$-2.74884 - 5.46887I$	0
$b = 1.66800 + 0.67324I$		
$u = 1.071840 - 0.149484I$		
$a = 1.208950 + 0.123740I$	$-2.74884 + 5.46887I$	0
$b = 1.66800 - 0.67324I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.914052 + 0.017611I$		
$a = 0.28796 + 2.10554I$	$1.30504 - 2.96740I$	$-16.6019 + 3.9985I$
$b = 0.029606 + 0.357540I$		
$u = 0.914052 - 0.017611I$		
$a = 0.28796 - 2.10554I$	$1.30504 + 2.96740I$	$-16.6019 - 3.9985I$
$b = 0.029606 - 0.357540I$		
$u = 1.087550 + 0.152734I$		
$a = -1.157320 + 0.302919I$	$-3.89961 - 11.18750I$	0
$b = -1.97161 - 0.66469I$		
$u = 1.087550 - 0.152734I$		
$a = -1.157320 - 0.302919I$	$-3.89961 + 11.18750I$	0
$b = -1.97161 + 0.66469I$		
$u = -0.999343 + 0.459478I$		
$a = 0.30537 - 1.95122I$	$-2.06219 - 4.61435I$	0
$b = -1.345570 - 0.027761I$		
$u = -0.999343 - 0.459478I$		
$a = 0.30537 + 1.95122I$	$-2.06219 + 4.61435I$	0
$b = -1.345570 + 0.027761I$		
$u = 0.926856 + 0.616107I$		
$a = -1.48117 - 1.93854I$	2.04966	0
$b = 1.95814$		
$u = 0.926856 - 0.616107I$		
$a = -1.48117 + 1.93854I$	2.04966	0
$b = 1.95814$		
$u = -0.971842 + 0.584202I$		
$a = 0.378274 + 1.128680I$	$-1.77536 + 3.05903I$	0
$b = 0.110057 - 0.403021I$		
$u = -0.971842 - 0.584202I$		
$a = 0.378274 - 1.128680I$	$-1.77536 - 3.05903I$	0
$b = 0.110057 + 0.403021I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.004520 + 0.529184I$		
$a = -0.37789 - 1.78426I$	$-6.62757 + 1.48268I$	0
$b = -0.803714 + 0.656750I$		
$u = -1.004520 - 0.529184I$		
$a = -0.37789 + 1.78426I$	$-6.62757 - 1.48268I$	0
$b = -0.803714 - 0.656750I$		
$u = 0.822047 + 0.815086I$		
$a = 0.503520 + 0.685512I$	$6.42114 - 2.03089I$	0
$b = -0.382925 - 0.879824I$		
$u = 0.822047 - 0.815086I$		
$a = 0.503520 - 0.685512I$	$6.42114 + 2.03089I$	0
$b = -0.382925 + 0.879824I$		
$u = 0.929297 + 0.706689I$		
$a = -0.162531 + 1.378400I$	$2.82931 - 3.82448I$	0
$b = -0.897351 - 0.739849I$		
$u = 0.929297 - 0.706689I$		
$a = -0.162531 - 1.378400I$	$2.82931 + 3.82448I$	0
$b = -0.897351 + 0.739849I$		
$u = -0.830789$		
$a = -0.529711$	$-1.36262$	$-6.28990$
$b = -0.524897$		
$u = 0.835882 + 0.822680I$		
$a = -0.705257 - 0.359402I$	$5.77020 - 7.57055I$	0
$b = 0.488855 + 0.663264I$		
$u = 0.835882 - 0.822680I$		
$a = -0.705257 + 0.359402I$	$5.77020 + 7.57055I$	0
$b = 0.488855 - 0.663264I$		
$u = -0.952690 + 0.699025I$		
$a = -1.161850 + 0.128348I$	$5.47969 + 1.54222I$	0
$b = -0.383270 + 0.555402I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.952690 - 0.699025I$		
$a = -1.161850 - 0.128348I$	$5.47969 - 1.54222I$	0
$b = -0.383270 - 0.555402I$		
$u = 0.879439 + 0.791896I$		
$a = 0.143018 + 0.204296I$	$1.30504 - 2.96740I$	0
$b = 0.029606 + 0.357540I$		
$u = 0.879439 - 0.791896I$		
$a = 0.143018 - 0.204296I$	$1.30504 + 2.96740I$	0
$b = 0.029606 - 0.357540I$		
$u = 0.974010 + 0.672846I$		
$a = -0.13241 - 2.73914I$	$-0.87551 - 5.31550I$	0
$b = 1.84271 + 1.22555I$		
$u = 0.974010 - 0.672846I$		
$a = -0.13241 + 2.73914I$	$-0.87551 + 5.31550I$	0
$b = 1.84271 - 1.22555I$		
$u = -0.962485 + 0.705411I$		
$a = 1.230370 + 0.245638I$	$5.77020 + 7.57055I$	0
$b = 0.488855 - 0.663264I$		
$u = -0.962485 - 0.705411I$		
$a = 1.230370 - 0.245638I$	$5.77020 - 7.57055I$	0
$b = 0.488855 + 0.663264I$		
$u = -0.431386 + 0.666039I$		
$a = -0.225386 - 1.395600I$	$-1.77536 - 3.05903I$	$-9.76833 + 2.76622I$
$b = 0.110057 + 0.403021I$		
$u = -0.431386 - 0.666039I$		
$a = -0.225386 + 1.395600I$	$-1.77536 + 3.05903I$	$-9.76833 - 2.76622I$
$b = 0.110057 - 0.403021I$		
$u = 0.987595 + 0.710734I$		
$a = -1.11733 + 2.72417I$	$4.93754 - 5.19661I$	0
$b = -1.18015 - 1.94588I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.987595 - 0.710734I$		
$a = -1.11733 - 2.72417I$	$4.93754 + 5.19661I$	0
$b = -1.18015 + 1.94588I$		
$u = 0.937037 + 0.779487I$		
$a = -1.369200 + 0.010031I$	$6.06758 - 3.93578I$	0
$b = 0.294442 - 0.779185I$		
$u = 0.937037 - 0.779487I$		
$a = -1.369200 - 0.010031I$	$6.06758 + 3.93578I$	0
$b = 0.294442 + 0.779185I$		
$u = -1.015290 + 0.678143I$		
$a = 0.593516 - 0.877102I$	$-2.06219 + 4.61435I$	0
$b = -1.345570 + 0.027761I$		
$u = -1.015290 - 0.678143I$		
$a = 0.593516 + 0.877102I$	$-2.06219 - 4.61435I$	0
$b = -1.345570 - 0.027761I$		
$u = 0.930205 + 0.791978I$		
$a = 1.228620 + 0.396768I$	$5.47969 + 1.54222I$	0
$b = -0.383270 + 0.555402I$		
$u = 0.930205 - 0.791978I$		
$a = 1.228620 - 0.396768I$	$5.47969 - 1.54222I$	0
$b = -0.383270 - 0.555402I$		
$u = -1.010270 + 0.702765I$		
$a = 0.06764 + 1.52585I$	$0.31756 + 8.62089I$	0
$b = 1.40467 - 0.62102I$		
$u = -1.010270 - 0.702765I$		
$a = 0.06764 - 1.52585I$	$0.31756 - 8.62089I$	0
$b = 1.40467 + 0.62102I$		
$u = -1.029790 + 0.708012I$		
$a = 0.48664 - 2.20279I$	$-3.89961 + 11.18750I$	0
$b = -1.97161 + 0.66469I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.029790 - 0.708012I$		
$a = 0.48664 + 2.20279I$	$-3.89961 - 11.18750I$	0
$b = -1.97161 - 0.66469I$		
$u = -1.023700 + 0.726192I$		
$a = 0.28327 + 2.73696I$	$2.85235 + 11.39960I$	0
$b = 1.83778 - 1.26952I$		
$u = -1.023700 - 0.726192I$		
$a = 0.28327 - 2.73696I$	$2.85235 - 11.39960I$	0
$b = 1.83778 + 1.26952I$		
$u = -0.284139 + 0.668066I$		
$a = -1.170660 - 0.642188I$	$-4.65419 + 2.84221I$	$-12.59242 - 3.99568I$
$b = 0.938320 + 0.000865I$		
$u = -0.284139 - 0.668066I$		
$a = -1.170660 + 0.642188I$	$-4.65419 - 2.84221I$	$-12.59242 + 3.99568I$
$b = 0.938320 - 0.000865I$		
$u = -0.193209 + 0.694467I$		
$a = -1.71483 + 0.37751I$	$0.31756 + 8.62089I$	$-6.58174 - 7.44305I$
$b = 1.40467 - 0.62102I$		
$u = -0.193209 - 0.694467I$		
$a = -1.71483 - 0.37751I$	$0.31756 - 8.62089I$	$-6.58174 + 7.44305I$
$b = 1.40467 + 0.62102I$		
$u = -0.181530 + 0.663240I$		
$a = 1.289870 - 0.508739I$	$1.33500 + 3.00337I$	$-4.59894 - 2.71098I$
$b = -1.139890 + 0.738004I$		
$u = -0.181530 - 0.663240I$		
$a = 1.289870 + 0.508739I$	$1.33500 - 3.00337I$	$-4.59894 + 2.71098I$
$b = -1.139890 - 0.738004I$		
$u = 0.210352 + 0.417710I$		
$a = 2.58989 + 0.96746I$	$2.82931 - 3.82448I$	$-1.91908 + 4.03755I$
$b = -0.897351 - 0.739849I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.210352 - 0.417710I$		
$a = 2.58989 - 0.96746I$	$2.82931 + 3.82448I$	$-1.91908 - 4.03755I$
$b = -0.897351 + 0.739849I$		
$u = 0.122077 + 0.444395I$		
$a = -2.03594 - 1.04124I$	$3.25378 + 1.67585I$	$-1.01897 - 2.48260I$
$b = 0.633168 + 0.948263I$		
$u = 0.122077 - 0.444395I$		
$a = -2.03594 + 1.04124I$	$3.25378 - 1.67585I$	$-1.01897 + 2.48260I$
$b = 0.633168 - 0.948263I$		
$u = 0.212119$		
$a = 3.37531$	$-1.36262$	$-6.28990$
$b = -0.524897$		

$$\text{III. } I_3^u = \langle b, a+1, u^3 - u^2 + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_2 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_5 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -u \\ -u^2 + u + 1 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -1 \\ 0 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -2u^2 + 1 \\ u^2 \end{pmatrix} \\ a_1 &= \begin{pmatrix} u^2 - 1 \\ -u^2 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -u - 2 \\ -u^2 + u + 1 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -1 \\ 0 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -2u^2 \\ u \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $8u - 12$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_7$ $c_{10}$	$u^3 - u^2 + 2u - 1$
$c_2, c_8$	$u^3 + u^2 - 1$
$c_4, c_9$	$u^3$
$c_5, c_{11}$	$u^3 - u^2 + 1$
$c_6, c_{12}$	$u^3 + u^2 + 2u + 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_6$ $c_7, c_{10}, c_{12}$	$y^3 + 3y^2 + 2y - 1$
$c_2, c_5, c_8$ $c_{11}$	$y^3 - y^2 + 2y - 1$
$c_4, c_9$	$y^3$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.877439 + 0.744862I$		
$a = -1.00000$	$6.04826 - 5.65624I$	$-4.98049 + 5.95889I$
$b = 0$		
$u = 0.877439 - 0.744862I$		
$a = -1.00000$	$6.04826 + 5.65624I$	$-4.98049 - 5.95889I$
$b = 0$		
$u = -0.754878$		
$a = -1.00000$	$-2.22691$	$-18.0390$
$b = 0$		

$$\text{IV. } I_4^u = \langle b, a^2 - au + 2u^2 - 3u + 2, u^3 - u^2 + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u \\ -u^2 + u + 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^2a + a - 2u + 2 \\ u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^2 - 1 \\ -u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} au + 2a \\ u^2a - au - a \end{pmatrix}$$

$$a_9 = \begin{pmatrix} a \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -3u^2a + au + 2u^2 + 3a - 3u \\ 2u^2a - u^2 - a + 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-u^2a + u^2 - 5$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_7$ $c_{10}$	$(u^3 - u^2 + 2u - 1)^2$
$c_2, c_8$	$(u^3 + u^2 - 1)^2$
$c_4, c_9$	$u^6$
$c_5, c_{11}$	$(u^3 - u^2 + 1)^2$
$c_6, c_{12}$	$(u^3 + u^2 + 2u + 1)^2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_6$ $c_7, c_{10}, c_{12}$	$(y^3 + 3y^2 + 2y - 1)^2$
$c_2, c_5, c_8$ $c_{11}$	$(y^3 - y^2 + 2y - 1)^2$
$c_4, c_9$	$y^6$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.877439 + 0.744862I$		
$a = 0.947279 + 0.320410I$	6.04826	$-4.56984 + 0.I$
$b = 0$		
$u = 0.877439 + 0.744862I$		
$a = -0.069840 + 0.424452I$	1.91067 - 2.82812I	$-4.21508 + 1.30714I$
$b = 0$		
$u = 0.877439 - 0.744862I$		
$a = 0.947279 - 0.320410I$	6.04826	$-4.56984 + 0.I$
$b = 0$		
$u = 0.877439 - 0.744862I$		
$a = -0.069840 - 0.424452I$	1.91067 + 2.82812I	$-4.21508 - 1.30714I$
$b = 0$		
$u = -0.754878$		
$a = -0.37744 + 2.29387I$	1.91067 + 2.82812I	$-4.21508 - 1.30714I$
$b = 0$		
$u = -0.754878$		
$a = -0.37744 - 2.29387I$	1.91067 - 2.82812I	$-4.21508 + 1.30714I$
$b = 0$		

$$\mathbf{V} \cdot I_5^u = \langle b - 2, a - 1, u + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = -18

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_3$	
$c_5, c_6, c_7$	$u + 1$
$c_8, c_{10}, c_{11}$	
$c_{12}$	
<hr/>	
$c_4, c_9$	$u - 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$	
$c_4, c_5, c_6$	
$c_7, c_8, c_9$	$y - 1$
$c_{10}, c_{11}, c_{12}$	

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.00000$		
$a = 1.00000$	-4.93480	-18.0000
$b = 2.00000$		

## VI. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_{10}$	$(u + 1)(u^3 - u^2 + 2u - 1)^3(u^{18} + 6u^{17} + \dots + 2u + 1) \\ \cdot (u^{84} + 27u^{83} + \dots + 20u + 1)$
$c_2, c_8$	$(u + 1)(u^3 + u^2 - 1)^3(u^{18} - 3u^{16} + \dots + 2u + 1) \\ \cdot (u^{84} + 3u^{83} + \dots + 2u - 1)$
$c_3, c_7$	$(u + 1)(u^3 - u^2 + 2u - 1)^3(u^{18} - 2u^{17} + \dots + 4u + 1) \\ \cdot (u^{84} - 3u^{83} + \dots + 76888u - 5953)$
$c_4, c_9$	$u^9(u - 1)(u^{18} - 6u^{17} + \dots - 24u + 8)(u^{42} + 3u^{41} + \dots - 36u - 8)^2$
$c_5, c_{11}$	$(u + 1)(u^3 - u^2 + 1)^3(u^{18} - 3u^{16} + \dots + 2u + 1) \\ \cdot (u^{84} + 3u^{83} + \dots + 2u - 1)$
$c_6, c_{12}$	$(u + 1)(u^3 + u^2 + 2u + 1)^3(u^{18} + 6u^{17} + \dots + 2u + 1) \\ \cdot (u^{84} + 27u^{83} + \dots + 20u + 1)$

## VII. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_6, c_{10}$ $c_{12}$	$(y - 1)(y^3 + 3y^2 + 2y - 1)^3(y^{18} + 14y^{17} + \cdots + 22y + 1)$ $\cdot (y^{84} + 61y^{83} + \cdots - 492y + 1)$
$c_2, c_5, c_8$ $c_{11}$	$(y - 1)(y^3 - y^2 + 2y - 1)^3(y^{18} - 6y^{17} + \cdots - 2y + 1)$ $\cdot (y^{84} - 27y^{83} + \cdots - 20y + 1)$
$c_3, c_7$	$(y - 1)(y^3 + 3y^2 + 2y - 1)^3(y^{18} - 10y^{17} + \cdots - 2y + 1)$ $\cdot (y^{84} + y^{83} + \cdots - 880217508y + 35438209)$
$c_4, c_9$	$y^9(y - 1)(y^{18} + 8y^{17} + \cdots + 256y + 64)$ $\cdot (y^{42} + 21y^{41} + \cdots + 304y + 64)^2$