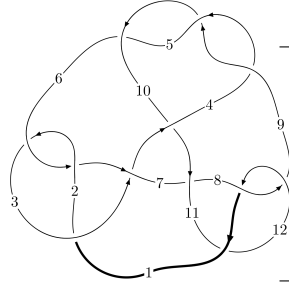
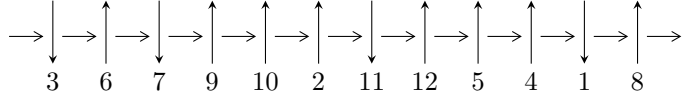


12a<sub>0215</sub> (K12a<sub>0215</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$2,7 \xrightarrow{c_6} 6 \xrightarrow{c_2} 3 \xrightarrow{c_3} 4,10 \xrightarrow{c_{10}} 11 \xrightarrow{c_7} 8 \xrightarrow{c_1} 1 \xrightarrow{c_5} 5 \xrightarrow{c_9} 9 \xrightarrow{c_{12}} 12 \Rightarrow c_4, c_8, c_{11}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -u^{25} + u^{24} + \dots + 2b + 1, u^{25} - u^{24} + \dots + 2a - 1, u^{27} - u^{26} + \dots + 2u - 1 \rangle$$

$$I_2^u = \langle -8.39891 \times 10^{38} u^{81} + 2.15045 \times 10^{38} u^{80} + \dots + 2.93276 \times 10^{39} b - 1.22548 \times 10^{40}, \\ 2.50222 \times 10^{40} u^{81} - 4.66705 \times 10^{40} u^{80} + \dots + 2.05293 \times 10^{40} a - 7.74216 \times 10^{40}, u^{82} - 2u^{81} + \dots - 19u + 1 \rangle$$

$$I_3^u = \langle b + a + u, a^2 - 2a - 2u + 1, u^2 + u + 1 \rangle$$

$$I_4^u = \langle b + u - 1, a + 1, u^2 - u + 1 \rangle$$

$$I_5^u = \langle b + a + 1, a^2 + 2au + 2a - u, u^2 + u + 1 \rangle$$

$$I_6^u = \langle b - u, a + u - 1, u^2 - u + 1 \rangle$$

\* 6 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 121 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I_1^u = \langle -u^{25} + u^{24} + \cdots + 2b + 1, u^{25} - u^{24} + \cdots + 2a - 1, u^{27} - u^{26} + \cdots + 2u - 1 \rangle \quad \text{I.}$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^3 \\ u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -\frac{1}{2}u^{25} + \frac{1}{2}u^{24} + \cdots - 2u + \frac{1}{2} \\ \frac{1}{2}u^{25} - \frac{1}{2}u^{24} + \cdots + 2u - \frac{1}{2} \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -\frac{1}{2}u^{23} + \frac{1}{2}u^{22} + \cdots - 2u + \frac{1}{2} \\ u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -\frac{1}{2}u^{26} + \frac{1}{2}u^{25} + \cdots + \frac{1}{2}u + 1 \\ u^6 + 2u^4 + u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^3 \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -\frac{1}{2}u^{26} - 3u^{24} + \cdots - 2u + \frac{3}{2} \\ \frac{1}{2}u^{25} - \frac{1}{2}u^{24} + \cdots + 2u - \frac{1}{2} \end{pmatrix}$$

$$a_9 = \begin{pmatrix} \frac{1}{2}u^{26} - \frac{1}{2}u^{25} + \cdots - \frac{1}{2}u^3 - 1 \\ -u^8 - 2u^6 - 2u^4 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -\frac{1}{2}u^{23} + \frac{1}{2}u^{22} + \cdots - 2u + \frac{1}{2} \\ -u^7 - u^5 + u \end{pmatrix}$$

(ii) Obstruction class = -1

$$\begin{aligned} \text{(iii) Cusp Shapes} &= 5u^{26} - 2u^{25} + 36u^{24} - 11u^{23} + 127u^{22} - 33u^{21} + 270u^{20} - 62u^{19} + \\ &367u^{18} - 85u^{17} + 313u^{16} - 86u^{15} + 164u^{14} - 67u^{13} + 84u^{12} - 29u^{11} + 98u^{10} - 8u^9 + \\ &82u^8 - 9u^7 + 17u^6 - 25u^5 - 9u^3 + 9u^2 - 2u + 6 \end{aligned}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_{11}$	$u^{27} + 15u^{26} + \dots - 2u - 1$
$c_2, c_6, c_8$ $c_{12}$	$u^{27} - u^{26} + \dots + 2u - 1$
$c_3, c_7$	$u^{27} + u^{26} + \dots - 3u - 2$
$c_4, c_5, c_9$	$u^{27} + 5u^{26} + \dots + 4u - 4$
$c_{10}$	$u^{27} - 15u^{26} + \dots + 212u + 32$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_{11}$	$y^{27} - y^{26} + \dots - 2y - 1$
$c_2, c_6, c_8$ $c_{12}$	$y^{27} + 15y^{26} + \dots - 2y - 1$
$c_3, c_7$	$y^{27} - 17y^{26} + \dots - 35y - 4$
$c_4, c_5, c_9$	$y^{27} - 25y^{26} + \dots + 48y - 16$
$c_{10}$	$y^{27} - 5y^{26} + \dots + 206224y - 1024$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.803618 + 0.349348I$ $a = 1.007060 + 0.949020I$ $b = -1.41653 + 1.34230I$	$5.22371 - 6.72306I$	$9.84931 + 3.39478I$
$u = 0.803618 - 0.349348I$ $a = 1.007060 - 0.949020I$ $b = -1.41653 - 1.34230I$	$5.22371 + 6.72306I$	$9.84931 - 3.39478I$
$u = -0.299281 + 0.820284I$ $a = -0.48606 - 1.73494I$ $b = 0.88880 + 1.18954I$	$4.11938 - 2.82450I$	$2.13183 + 1.79598I$
$u = -0.299281 - 0.820284I$ $a = -0.48606 + 1.73494I$ $b = 0.88880 - 1.18954I$	$4.11938 + 2.82450I$	$2.13183 - 1.79598I$
$u = 0.116549 + 0.860765I$ $a = 0.078400 - 1.016090I$ $b = -0.278709 + 0.364691I$	$-1.97453 + 1.43518I$	$-2.24818 - 4.96930I$
$u = 0.116549 - 0.860765I$ $a = 0.078400 + 1.016090I$ $b = -0.278709 - 0.364691I$	$-1.97453 - 1.43518I$	$-2.24818 + 4.96930I$
$u = -0.513874 + 1.069060I$ $a = 0.352532 + 0.981625I$ $b = -0.76543 - 1.34247I$	$4.01281 - 6.61800I$	$3.83990 + 7.93477I$
$u = -0.513874 - 1.069060I$ $a = 0.352532 - 0.981625I$ $b = -0.76543 + 1.34247I$	$4.01281 + 6.61800I$	$3.83990 - 7.93477I$
$u = -0.615180 + 0.518291I$ $a = 1.61732 + 1.21180I$ $b = -0.501601 - 0.764150I$	$7.40368 - 2.31507I$	$12.17043 + 2.39012I$
$u = -0.615180 - 0.518291I$ $a = 1.61732 - 1.21180I$ $b = -0.501601 + 0.764150I$	$7.40368 + 2.31507I$	$12.17043 - 2.39012I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.743850 + 0.296760I$ $a = -0.370434 + 0.541518I$ $b = 0.339092 + 1.113750I$	$-0.14900 + 3.15153I$	$5.48053 - 3.24594I$
$u = -0.743850 - 0.296760I$ $a = -0.370434 - 0.541518I$ $b = 0.339092 - 1.113750I$	$-0.14900 - 3.15153I$	$5.48053 + 3.24594I$
$u = 0.264221 + 1.179210I$ $a = -1.117430 + 0.645366I$ $b = -0.213710 - 1.207370I$	$-4.23123 - 0.71359I$	$-1.52661 - 0.31939I$
$u = 0.264221 - 1.179210I$ $a = -1.117430 - 0.645366I$ $b = -0.213710 + 1.207370I$	$-4.23123 + 0.71359I$	$-1.52661 + 0.31939I$
$u = -0.338826 + 1.179080I$ $a = 0.42150 + 1.47832I$ $b = 0.72240 - 1.41289I$	$-8.48034 - 3.42330I$	$-5.15562 + 3.33733I$
$u = -0.338826 - 1.179080I$ $a = 0.42150 - 1.47832I$ $b = 0.72240 + 1.41289I$	$-8.48034 + 3.42330I$	$-5.15562 - 3.33733I$
$u = 0.411435 + 1.173870I$ $a = 0.52311 + 1.66108I$ $b = -1.11519 - 1.11629I$	$-5.27423 + 7.72991I$	$-0.94876 - 7.44715I$
$u = 0.411435 - 1.173870I$ $a = 0.52311 - 1.66108I$ $b = -1.11519 + 1.11629I$	$-5.27423 - 7.72991I$	$-0.94876 + 7.44715I$
$u = 0.528079 + 1.138480I$ $a = 0.703762 - 0.059607I$ $b = 0.123706 + 0.371890I$	$-3.65072 + 8.53958I$	$0.93638 - 5.62468I$
$u = 0.528079 - 1.138480I$ $a = 0.703762 + 0.059607I$ $b = 0.123706 - 0.371890I$	$-3.65072 - 8.53958I$	$0.93638 + 5.62468I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.568964 + 1.151920I$ $a = -0.84587 - 1.38262I$ $b = -0.64504 + 1.69437I$	$-5.12208 - 13.17930I$	$-0.30650 + 10.03114I$
$u = -0.568964 - 1.151920I$ $a = -0.84587 + 1.38262I$ $b = -0.64504 - 1.69437I$	$-5.12208 + 13.17930I$	$-0.30650 - 10.03114I$
$u = 0.597410 + 1.146880I$ $a = 0.30821 - 2.43725I$ $b = 1.60210 + 2.43878I$	$0.5058 + 17.2462I$	$3.99567 - 10.69153I$
$u = 0.597410 - 1.146880I$ $a = 0.30821 + 2.43725I$ $b = 1.60210 - 2.43878I$	$0.5058 - 17.2462I$	$3.99567 + 10.69153I$
$u = 0.541018 + 0.346561I$ $a = -0.594979 + 0.357100I$ $b = 0.282228 + 0.197681I$	$1.153800 + 0.433800I$	$8.89068 - 3.10738I$
$u = 0.541018 - 0.346561I$ $a = -0.594979 - 0.357100I$ $b = 0.282228 - 0.197681I$	$1.153800 - 0.433800I$	$8.89068 + 3.10738I$
$u = 0.635291$ $a = -0.194238$ $b = 0.955765$	$1.41139$	$7.78190$

$$\text{II. } I_2^u = \langle -8.40 \times 10^{38} u^{81} + 2.15 \times 10^{38} u^{80} + \dots + 2.93 \times 10^{39} b - 1.23 \times 10^{40}, 2.50 \times 10^{40} u^{81} - 4.67 \times 10^{40} u^{80} + \dots + 2.05 \times 10^{40} a - 7.74 \times 10^{40}, u^{82} - 2u^{81} + \dots - 19u + 7 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^3 \\ u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1.21886u^{81} + 2.27336u^{80} + \dots - 12.9728u + 3.77127 \\ 0.286383u^{81} - 0.0733251u^{80} + \dots - 4.86257u + 4.17860 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.411067u^{81} - 0.288547u^{80} + \dots + 4.78352u - 3.00988 \\ -0.614218u^{81} + 1.70547u^{80} + \dots - 15.3414u + 6.51871 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0.318231u^{81} - 2.32467u^{80} + \dots + 24.6828u - 12.1894 \\ -1.92973u^{81} + 3.70643u^{80} + \dots - 27.3383u + 10.1543 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^3 \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -0.371191u^{81} + 0.108615u^{80} + \dots + 1.54552u + 0.653397 \\ -0.134364u^{81} + 0.768131u^{80} + \dots - 5.41326u + 3.53888 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.932035u^{81} - 1.61400u^{80} + \dots + 1.95754u + 0.0479519 \\ -0.335091u^{81} + 0.133733u^{80} + \dots + 9.76711u - 6.52731 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -0.854155u^{81} + 0.424449u^{80} + \dots + 5.52400u - 3.77735 \\ -0.0430260u^{81} + 1.07121u^{80} + \dots - 14.4429u + 9.10127 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-1.08647u^{81} + 2.72577u^{80} + \dots - 37.5801u + 26.3020$



(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_{11}$	$u^{82} + 38u^{81} + \dots + 171u + 49$
$c_2, c_6, c_8$ $c_{12}$	$u^{82} - 2u^{81} + \dots - 19u + 7$
$c_3, c_7$	$u^{82} + 2u^{81} + \dots + 653965u + 115507$
$c_4, c_5, c_9$	$(u^{41} - 2u^{40} + \dots + 4u + 2)^2$
$c_{10}$	$(u^{41} + 6u^{40} + \dots - 144u - 32)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_{11}$	$y^{82} + 14y^{81} + \dots + 65427y + 2401$
$c_2, c_6, c_8$ $c_{12}$	$y^{82} + 38y^{81} + \dots + 171y + 49$
$c_3, c_7$	$y^{82} - 10y^{81} + \dots - 231414356651y + 13341867049$
$c_4, c_5, c_9$	$(y^{41} - 38y^{40} + \dots - 32y - 4)^2$
$c_{10}$	$(y^{41} + 2y^{40} + \dots - 3456y - 1024)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.689028 + 0.715237I$ $a = 0.426260 - 0.243286I$ $b = 0.022676 - 0.162534I$	$-0.36156 + 5.69573I$	0
$u = 0.689028 - 0.715237I$ $a = 0.426260 + 0.243286I$ $b = 0.022676 + 0.162534I$	$-0.36156 - 5.69573I$	0
$u = -0.765330 + 0.659348I$ $a = -1.34566 - 0.92456I$ $b = 0.239119 + 0.976808I$	$4.65659 - 8.77727I$	0
$u = -0.765330 - 0.659348I$ $a = -1.34566 + 0.92456I$ $b = 0.239119 - 0.976808I$	$4.65659 + 8.77727I$	0
$u = -0.695472 + 0.747401I$ $a = -1.19111 - 0.96963I$ $b = 0.366764 + 1.155420I$	$2.83527 - 1.77985I$	0
$u = -0.695472 - 0.747401I$ $a = -1.19111 + 0.96963I$ $b = 0.366764 - 1.155420I$	$2.83527 + 1.77985I$	0
$u = -0.719446 + 0.634218I$ $a = 1.37551 + 0.99667I$ $b = -0.323967 - 0.941289I$	$6.76688 - 4.02505I$	$11.00664 + 3.97880I$
$u = -0.719446 - 0.634218I$ $a = 1.37551 - 0.99667I$ $b = -0.323967 + 0.941289I$	$6.76688 + 4.02505I$	$11.00664 - 3.97880I$
$u = 0.283270 + 1.031430I$ $a = 2.04178 - 0.89333I$ $b = -0.20075 + 1.91629I$	$2.83527 - 1.77985I$	0
$u = 0.283270 - 1.031430I$ $a = 2.04178 + 0.89333I$ $b = -0.20075 - 1.91629I$	$2.83527 + 1.77985I$	0

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.341629 + 1.027430I$ $a = -2.44843 + 0.21696I$ $b = 0.90934 - 1.82491I$	$2.46019 + 3.45470I$	0
$u = 0.341629 - 1.027430I$ $a = -2.44843 - 0.21696I$ $b = 0.90934 + 1.82491I$	$2.46019 - 3.45470I$	0
$u = 0.839192 + 0.351360I$ $a = -1.044020 - 0.844502I$ $b = 1.31623 - 1.40977I$	$2.88789 - 11.91530I$	$6.77003 + 7.12233I$
$u = 0.839192 - 0.351360I$ $a = -1.044020 + 0.844502I$ $b = 1.31623 + 1.40977I$	$2.88789 + 11.91530I$	$6.77003 - 7.12233I$
$u = 0.644899 + 0.881737I$ $a = 0.401320 - 0.122971I$ $b = 0.0900442 - 0.0322691I$	$-0.847371 - 0.579153I$	0
$u = 0.644899 - 0.881737I$ $a = 0.401320 + 0.122971I$ $b = 0.0900442 + 0.0322691I$	$-0.847371 + 0.579153I$	0
$u = -0.396078 + 1.023630I$ $a = 0.282828 + 1.206450I$ $b = -0.79733 - 1.30420I$	3.09696	0
$u = -0.396078 - 1.023630I$ $a = 0.282828 - 1.206450I$ $b = -0.79733 + 1.30420I$	3.09696	0
$u = -0.672412 + 0.878423I$ $a = 0.862261 + 0.794570I$ $b = -0.57402 - 1.37006I$	$2.46019 - 3.45470I$	0
$u = -0.672412 - 0.878423I$ $a = 0.862261 - 0.794570I$ $b = -0.57402 + 1.37006I$	$2.46019 + 3.45470I$	0

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.564931 + 0.954516I$ $a = -0.417859 - 0.016464I$ $b = -0.0477010 - 0.0604940I$	$0.44383 + 3.16653I$	0
$u = 0.564931 - 0.954516I$ $a = -0.417859 + 0.016464I$ $b = -0.0477010 + 0.0604940I$	$0.44383 - 3.16653I$	0
$u = -0.452391 + 1.015630I$ $a = -0.71504 - 1.98517I$ $b = -1.13769 + 1.76536I$	$-0.847371 - 0.579153I$	0
$u = -0.452391 - 1.015630I$ $a = -0.71504 + 1.98517I$ $b = -1.13769 - 1.76536I$	$-0.847371 + 0.579153I$	0
$u = 0.605854 + 0.628370I$ $a = -0.424775 + 0.321065I$ $b = 0.075036 + 0.153636I$	$1.40425 + 1.45669I$	$6.96953 - 5.06575I$
$u = 0.605854 - 0.628370I$ $a = -0.424775 - 0.321065I$ $b = 0.075036 - 0.153636I$	$1.40425 - 1.45669I$	$6.96953 + 5.06575I$
$u = -0.808418 + 0.297201I$ $a = 0.342419 - 0.461894I$ $b = -0.319219 - 1.185340I$	$-2.58795 + 8.05246I$	$2.39091 - 6.67607I$
$u = -0.808418 - 0.297201I$ $a = 0.342419 + 0.461894I$ $b = -0.319219 + 1.185340I$	$-2.58795 - 8.05246I$	$2.39091 + 6.67607I$
$u = -0.544403 + 1.015420I$ $a = -0.463853 - 0.980844I$ $b = 0.73592 + 1.33469I$	$5.94556 - 2.27206I$	0
$u = -0.544403 - 1.015420I$ $a = -0.463853 + 0.980844I$ $b = 0.73592 - 1.33469I$	$5.94556 + 2.27206I$	0

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.633782 + 0.965157I$ $a = -0.619693 - 0.846918I$ $b = 0.67438 + 1.36329I$	$5.78705 - 1.14285I$	0
$u = -0.633782 - 0.965157I$ $a = -0.619693 + 0.846918I$ $b = 0.67438 - 1.36329I$	$5.78705 + 1.14285I$	0
$u = 0.797763 + 0.273658I$ $a = -0.790370 - 0.865730I$ $b = 1.28854 - 1.12842I$	$0.33937 - 3.94176I$	$3.80485 + 2.05545I$
$u = 0.797763 - 0.273658I$ $a = -0.790370 + 0.865730I$ $b = 1.28854 + 1.12842I$	$0.33937 + 3.94176I$	$3.80485 - 2.05545I$
$u = -0.502229 + 1.050420I$ $a = 0.89797 + 1.74531I$ $b = 0.87575 - 1.84134I$	$-0.36156 - 5.69573I$	0
$u = -0.502229 - 1.050420I$ $a = 0.89797 - 1.74531I$ $b = 0.87575 + 1.84134I$	$-0.36156 + 5.69573I$	0
$u = -0.279574 + 1.135010I$ $a = -0.30915 - 1.50867I$ $b = -0.74203 + 1.28219I$	$-4.43409 + 0.19849I$	0
$u = -0.279574 - 1.135010I$ $a = -0.30915 + 1.50867I$ $b = -0.74203 - 1.28219I$	$-4.43409 - 0.19849I$	0
$u = 0.201185 + 1.156190I$ $a = 1.10226 - 0.88862I$ $b = 0.338911 + 1.367520I$	$0.33937 - 3.94176I$	0
$u = 0.201185 - 1.156190I$ $a = 1.10226 + 0.88862I$ $b = 0.338911 - 1.367520I$	$0.33937 + 3.94176I$	0

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.680761 + 0.963853I$ $a = 0.637175 + 0.746660I$ $b = -0.66131 - 1.39711I$	$3.75302 + 3.33055I$	0
$u = -0.680761 - 0.963853I$ $a = 0.637175 - 0.746660I$ $b = -0.66131 + 1.39711I$	$3.75302 - 3.33055I$	0
$u = 0.383840 + 1.124570I$ $a = -0.75917 - 1.43709I$ $b = 1.058920 + 0.664259I$	$-1.78976 + 3.63396I$	0
$u = 0.383840 - 1.124570I$ $a = -0.75917 + 1.43709I$ $b = 1.058920 - 0.664259I$	$-1.78976 - 3.63396I$	0
$u = 0.525005 + 1.078820I$ $a = -0.57133 - 3.05080I$ $b = 2.61883 + 1.84930I$	$3.75302 + 3.33055I$	0
$u = 0.525005 - 1.078820I$ $a = -0.57133 + 3.05080I$ $b = 2.61883 - 1.84930I$	$3.75302 - 3.33055I$	0
$u = 0.324132 + 1.156920I$ $a = 0.470124 + 1.324050I$ $b = -0.643195 - 0.862446I$	$-5.04218 - 0.52120I$	0
$u = 0.324132 - 1.156920I$ $a = 0.470124 - 1.324050I$ $b = -0.643195 + 0.862446I$	$-5.04218 + 0.52120I$	0
$u = 0.502544 + 1.098810I$ $a = -0.713487 - 0.031522I$ $b = -0.016767 - 0.335638I$	$-1.04581 + 3.83403I$	0
$u = 0.502544 - 1.098810I$ $a = -0.713487 + 0.031522I$ $b = -0.016767 + 0.335638I$	$-1.04581 - 3.83403I$	0

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.184539 + 1.194310I$ $a = -0.968047 + 0.860870I$ $b = -0.414774 - 1.294930I$	$-2.25867 - 8.98287I$	0
$u = 0.184539 - 1.194310I$ $a = -0.968047 - 0.860870I$ $b = -0.414774 + 1.294930I$	$-2.25867 + 8.98287I$	0
$u = -0.246275 + 1.183340I$ $a = 0.30446 + 1.42791I$ $b = 0.63553 - 1.29001I$	$-7.30150 + 4.90350I$	0
$u = -0.246275 - 1.183340I$ $a = 0.30446 - 1.42791I$ $b = 0.63553 + 1.29001I$	$-7.30150 - 4.90350I$	0
$u = -0.759560 + 0.170105I$ $a = 0.206959 - 0.563917I$ $b = -0.190983 - 1.102140I$	$-4.43409 + 0.19849I$	$-0.855132 - 0.263674I$
$u = -0.759560 - 0.170105I$ $a = 0.206959 + 0.563917I$ $b = -0.190983 + 1.102140I$	$-4.43409 - 0.19849I$	$-0.855132 + 0.263674I$
$u = 0.548764 + 1.094240I$ $a = 0.18219 + 2.93809I$ $b = -2.31640 - 2.17267I$	$4.65659 + 8.77727I$	0
$u = 0.548764 - 1.094240I$ $a = 0.18219 - 2.93809I$ $b = -2.31640 + 2.17267I$	$4.65659 - 8.77727I$	0
$u = 0.679190 + 0.367886I$ $a = 0.86819 + 1.43693I$ $b = -1.82727 + 1.10121I$	$6.76688 - 4.02505I$	$11.00664 + 3.97880I$
$u = 0.679190 - 0.367886I$ $a = 0.86819 - 1.43693I$ $b = -1.82727 - 1.10121I$	$6.76688 + 4.02505I$	$11.00664 - 3.97880I$



Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.447381 + 1.149980I$ $a = 0.883459 - 0.065760I$ $b = 0.005837 + 0.564784I$	$-5.04218 + 0.52120I$	0
$u = 0.447381 - 1.149980I$ $a = 0.883459 + 0.065760I$ $b = 0.005837 - 0.564784I$	$-5.04218 - 0.52120I$	0
$u = -0.440145 + 0.608096I$ $a = 0.95391 - 1.06892I$ $b = -1.052950 - 0.702852I$	$0.44383 - 3.16653I$	$4.71993 - 0.58973I$
$u = -0.440145 - 0.608096I$ $a = 0.95391 + 1.06892I$ $b = -1.052950 + 0.702852I$	$0.44383 + 3.16653I$	$4.71993 + 0.58973I$
$u = 0.712533 + 0.226602I$ $a = 0.563149 - 0.287019I$ $b = -0.383162 - 0.371369I$	$-1.04581 - 3.83403I$	$4.44538 + 2.12907I$
$u = 0.712533 - 0.226602I$ $a = 0.563149 + 0.287019I$ $b = -0.383162 + 0.371369I$	$-1.04581 + 3.83403I$	$4.44538 - 2.12907I$
$u = -0.551632 + 1.132560I$ $a = 0.85256 + 1.44076I$ $b = 0.67530 - 1.71516I$	$-2.58795 - 8.05246I$	0
$u = -0.551632 - 1.132560I$ $a = 0.85256 - 1.44076I$ $b = 0.67530 + 1.71516I$	$-2.58795 + 8.05246I$	0
$u = 0.735105 + 0.006056I$ $a = 0.436191 - 0.362330I$ $b = -0.791059 - 0.477947I$	$-1.78976 + 3.63396I$	$3.00355 - 4.41372I$
$u = 0.735105 - 0.006056I$ $a = 0.436191 + 0.362330I$ $b = -0.791059 + 0.477947I$	$-1.78976 - 3.63396I$	$3.00355 + 4.41372I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.512115 + 1.158870I$ $a = -0.74554 - 1.45277I$ $b = -0.70751 + 1.65463I$	$-7.30150 - 4.90350I$	0
$u = -0.512115 - 1.158870I$ $a = -0.74554 + 1.45277I$ $b = -0.70751 - 1.65463I$	$-7.30150 + 4.90350I$	0
$u = 0.585200 + 1.135380I$ $a = -0.22170 + 2.53693I$ $b = -1.73675 - 2.39250I$	$2.88789 + 11.91530I$	0
$u = 0.585200 - 1.135380I$ $a = -0.22170 - 2.53693I$ $b = -1.73675 + 2.39250I$	$2.88789 - 11.91530I$	0
$u = 0.556886 + 1.153190I$ $a = 0.00759 - 2.38243I$ $b = 1.66909 + 2.10879I$	$-2.25867 + 8.98287I$	0
$u = 0.556886 - 1.153190I$ $a = 0.00759 + 2.38243I$ $b = 1.66909 - 2.10879I$	$-2.25867 - 8.98287I$	0
$u = 0.592687 + 0.369522I$ $a = -0.61966 - 1.82844I$ $b = 2.04999 - 0.82047I$	$5.78705 + 1.14285I$	$9.35767 - 1.34968I$
$u = 0.592687 - 0.369522I$ $a = -0.61966 + 1.82844I$ $b = 2.04999 + 0.82047I$	$5.78705 - 1.14285I$	$9.35767 + 1.34968I$
$u = -0.532881 + 0.446002I$ $a = -0.675343 + 0.806391I$ $b = 0.633559 + 0.875574I$	$1.40425 + 1.45669I$	$6.96953 - 5.06575I$
$u = -0.532881 - 0.446002I$ $a = -0.675343 - 0.806391I$ $b = 0.633559 - 0.875574I$	$1.40425 - 1.45669I$	$6.96953 + 5.06575I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.552652 + 0.404350I$	$5.94556 + 2.27206I$	$8.68115 - 3.66498I$
$a = -1.98289 - 1.32692I$		
$b = 0.605079 + 0.596657I$		
$u = -0.552652 - 0.404350I$	$5.94556 - 2.27206I$	$8.68115 + 3.66498I$
$a = -1.98289 + 1.32692I$		
$b = 0.605079 - 0.596657I$		

$$\text{III. } I_3^u = \langle b + a + u, a^2 - 2a - 2u + 1, u^2 + u + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -u - 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u \\ u + 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -1 \\ u + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a \\ -a - u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} au + a - u \\ -u - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -au \\ u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} au - 3u - 1 \\ a + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -au - a + u \\ u + 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} au + a + 1 \\ -u - 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $8u + 12$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_8$ $c_{11}$	$(u^2 - u + 1)^2$
$c_3, c_6, c_7$ $c_{12}$	$(u^2 + u + 1)^2$
$c_4, c_5, c_9$ $c_{10}$	$(u^2 - 2)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_6, c_7, c_8$ $c_{11}, c_{12}$	$(y^2 + y + 1)^2$
$c_4, c_5, c_9$ $c_{10}$	$(y - 2)^4$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.500000 + 0.866025I$		
$a = 0.292893 - 1.224750I$	$4.93480 - 4.05977I$	$8.00000 + 6.92820I$
$b = 0.207107 + 0.358719I$		
$u = -0.500000 + 0.866025I$		
$a = 1.70711 + 1.22474I$	$4.93480 - 4.05977I$	$8.00000 + 6.92820I$
$b = -1.20711 - 2.09077I$		
$u = -0.500000 - 0.866025I$		
$a = 0.292893 + 1.224750I$	$4.93480 + 4.05977I$	$8.00000 - 6.92820I$
$b = 0.207107 - 0.358719I$		
$u = -0.500000 - 0.866025I$		
$a = 1.70711 - 1.22474I$	$4.93480 + 4.05977I$	$8.00000 - 6.92820I$
$b = -1.20711 + 2.09077I$		

$$\text{IV. } I_4^u = \langle b + u - 1, a + 1, u^2 - u + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ u - 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u \\ u - 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ u - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1 \\ -u + 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -1 \\ -u + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ -u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -1 \\ -u + 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u - 2 \\ -u + 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-8u + 4$



(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_6$ $c_7, c_{11}, c_{12}$	$u^2 - u + 1$
$c_2, c_8$	$u^2 + u + 1$
$c_4, c_5, c_9$ $c_{10}$	$u^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_6, c_7, c_8$ $c_{11}, c_{12}$	$y^2 + y + 1$
$c_4, c_5, c_9$ $c_{10}$	$y^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.500000 + 0.866025I$ $a = -1.00000$ $b = 0.500000 - 0.866025I$	$4.05977I$	$0. - 6.92820I$
$u = 0.500000 - 0.866025I$ $a = -1.00000$ $b = 0.500000 + 0.866025I$	$- 4.05977I$	$0. + 6.92820I$

$$\mathbf{V}. I_5^u = \langle b + a + 1, a^2 + 2au + 2a - u, u^2 + u + 1 \rangle$$

**(i) Arc colorings**

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -u - 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u \\ u + 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -1 \\ u + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a \\ -a - 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} au + a - 1 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -a - u + 1 \\ -u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} a - u \\ -au - a + 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -au - a + 1 \\ -u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} au + a - u - 1 \\ u \end{pmatrix}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes = 8**

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_8$ $c_{11}$	$(u^2 - u + 1)^2$
$c_3, c_6, c_7$ $c_{12}$	$(u^2 + u + 1)^2$
$c_4, c_5, c_9$ $c_{10}$	$(u^2 - 2)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_6, c_7, c_8$ $c_{11}, c_{12}$	$(y^2 + y + 1)^2$
$c_4, c_5, c_9$ $c_{10}$	$(y - 2)^4$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_5^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.500000 + 0.866025I$	4.93480	8.00000
$a = 0.207107 + 0.358719I$		
$b = -1.207110 - 0.358719I$		
$u = -0.500000 + 0.866025I$	4.93480	8.00000
$a = -1.20711 - 2.09077I$		
$b = 0.20711 + 2.09077I$		
$u = -0.500000 - 0.866025I$	4.93480	8.00000
$a = 0.207107 - 0.358719I$		
$b = -1.207110 + 0.358719I$		
$u = -0.500000 - 0.866025I$	4.93480	8.00000
$a = -1.20711 + 2.09077I$		
$b = 0.20711 - 2.09077I$		

$$\text{VI. } I_6^u = \langle b - u, a + u - 1, u^2 - u + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ u - 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u \\ u - 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ u - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u + 1 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u + 1 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 2 \\ u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u + 1 \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -2u + 1 \\ u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 6



(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_6$ $c_7, c_{11}, c_{12}$	$u^2 - u + 1$
$c_2, c_8$	$u^2 + u + 1$
$c_4, c_5, c_9$ $c_{10}$	$u^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_6, c_7, c_8$ $c_{11}, c_{12}$	$y^2 + y + 1$
$c_4, c_5, c_9$ $c_{10}$	$y^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_6^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.500000 + 0.866025I$	0	6.00000
$a = 0.500000 - 0.866025I$		
$b = 0.500000 + 0.866025I$		
$u = 0.500000 - 0.866025I$	0	6.00000
$a = 0.500000 + 0.866025I$		
$b = 0.500000 - 0.866025I$		

## VII. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_{11}$	$((u^2 - u + 1)^6)(u^{27} + 15u^{26} + \dots - 2u - 1)$ $\cdot (u^{82} + 38u^{81} + \dots + 171u + 49)$
$c_2, c_8$	$((u^2 - u + 1)^4)(u^2 + u + 1)^2(u^{27} - u^{26} + \dots + 2u - 1)$ $\cdot (u^{82} - 2u^{81} + \dots - 19u + 7)$
$c_3, c_7$	$((u^2 - u + 1)^2)(u^2 + u + 1)^4(u^{27} + u^{26} + \dots - 3u - 2)$ $\cdot (u^{82} + 2u^{81} + \dots + 653965u + 115507)$
$c_4, c_5, c_9$	$u^4(u^2 - 2)^4(u^{27} + 5u^{26} + \dots + 4u - 4)(u^{41} - 2u^{40} + \dots + 4u + 2)^2$
$c_6, c_{12}$	$((u^2 - u + 1)^2)(u^2 + u + 1)^4(u^{27} - u^{26} + \dots + 2u - 1)$ $\cdot (u^{82} - 2u^{81} + \dots - 19u + 7)$
$c_{10}$	$u^4(u^2 - 2)^4(u^{27} - 15u^{26} + \dots + 212u + 32)$ $\cdot (u^{41} + 6u^{40} + \dots - 144u - 32)^2$

### VIII. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_{11}$	$((y^2 + y + 1)^6)(y^{27} - y^{26} + \dots - 2y - 1)$ $\cdot (y^{82} + 14y^{81} + \dots + 65427y + 2401)$
$c_2, c_6, c_8$ $c_{12}$	$((y^2 + y + 1)^6)(y^{27} + 15y^{26} + \dots - 2y - 1)$ $\cdot (y^{82} + 38y^{81} + \dots + 171y + 49)$
$c_3, c_7$	$((y^2 + y + 1)^6)(y^{27} - 17y^{26} + \dots - 35y - 4)$ $\cdot (y^{82} - 10y^{81} + \dots - 231414356651y + 13341867049)$
$c_4, c_5, c_9$	$y^4(y - 2)^8(y^{27} - 25y^{26} + \dots + 48y - 16)$ $\cdot (y^{41} - 38y^{40} + \dots - 32y - 4)^2$
$c_{10}$	$y^4(y - 2)^8(y^{27} - 5y^{26} + \dots + 206224y - 1024)$ $\cdot (y^{41} + 2y^{40} + \dots - 3456y - 1024)^2$